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Micropile Design and Construction – Part II

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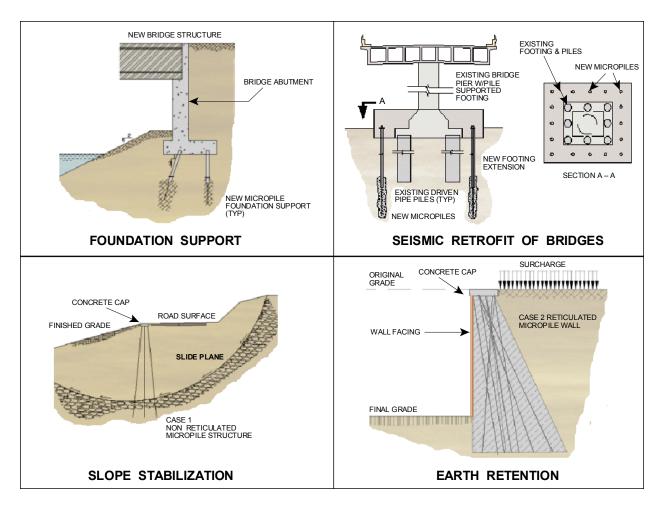
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Micropile Design and Construction

Reference Manual





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16. ABSTRACT The use of micropiles has grown significantly since their conception in the 1950s, and in particular since the mid-1980s. Micropiles have been used mainly as foundation support elements to resist static and seismic loads, and to a lesser extent, as in-situ reinforcements to provide stabilization of slopes and excavations. Many of these applications are for transportation structures. This manual is intended to be a "practitioner-oriented" document containing sufficient information on the geotechnical and structural design of micropiles for foundation support and for slope stabilization. Information is also provided on inspection and load testing procedures, cost data, and contracting methods to facilitate the safe and cost-effective use of micropiles on transportation projects. Two detailed design examples and a generic commentary guideline specification for micropiles is included in the manual.

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SI CONVERSION FACTORS				
	APPROXIMA	ATE CONVERSION	S FROM SI UNITS	
Symbol	When You Know	Multiply By	To Find	Symbol
		LENGTH		
mm m m km	millimeters meters meters kilometers	0.039 3.28 1.09 0.621 AREA	inches feet yards miles	in ft yd mi
mm² m² m² ha km²	square millimeters square meters square meters hectares square kilometers	0.0016 10.764 1.195 2.47 0.386 VOLUME	square inches square feet square yards acres square miles	in² ft² yd² ac mi²
ml l m³ m³	millimeters liters cubic meters cubic meters	0.034 0.264 35.71 1.307 MASS	fluid ounces gallons cubic feet cubic yards	fl oz gal ft³ yd³
g kg tonnes	grams kilograms tonnes	0.035 2.202 1.103 TEMPERATURE	ounces pounds tons	oz lb tons
°C	Celsius	1.8 C + 32	Fahrenheit	°F
		WEIGHT DENSITY		
kN/m³	kilonewton / cubic meter	6.36	poundforce / cubic foot	pcf
	FORCE and PRESSURE or STRESS			
N kN kPa kPa	newtons kilonewtons kilopascals kilopascals	0.225 225 0.145 20.9	poundforce poundforce poundforce / square inch poundforce / square foot	lbf lbf psi psf

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# CHAPTER 1 INTRODUCTION

#### 1.1 PURPOSE AND SCOPE OF MANUAL

The use of micropiles has grown significantly since their conception in the 1950s, and in particular since the mid-1980s. Micropiles have been used mainly as foundation support elements to resist static and seismic loads, and to a lesser extent, as in-situ reinforcements to provide stabilization of slopes and excavations. Many of these applications are for transportation structures.

In 1993, the Federal Highway Administration (FHWA) sponsored a project to review the state-of-the-practice of micropiles. The research group for this project included contractors, consultants, academics, and owners. The document produced from this project, entitled *Drilled and Grouted Micropiles – State-of-the-Practice Review* (FHWA, 1997) provided a comprehensive international review and detailed analysis of available research and development results, laboratory and field testing data, design methods, construction methodologies, site observations, and monitored case studies. As part of this study, the limitations and uncertainties in the state-of-the-practice were evaluated, and further research needs were assessed. One of the highlighted needs was a manual of design and construction guidelines intended for use by practicing highway agency geotechnical and structural engineers.

In response to this need, the FHWA sponsored the development of the manual *Micropile Design and Construction Guidelines, Implementation Manual* (FHWA, 2000). Funding and development of the manual was a cooperative effort between FHWA, U.S. micropile specialty contractors, and several state DOTs. The manual is intended to be a "practitioner-oriented" document containing sufficient information on micropile design, construction specifications, inspection and testing procedures, cost data, and contracting methods to facilitate the safe and cost-effective use of micropiles on transportation projects.

This manual is a revision to the 2001 Implementation Manual. The major revisions to the manual include:

#### Chapter 3:

• Existing case history information has been updated and additional case histories have been added which specifically address the evaluation of micropile feasibility for specific projects.

#### Chapter 4:

• A description of sonic drilling techniques has been added.

#### Chapter 5:

- Information on corrosion protection has been updated to reflect current FHWA practice regarding assessment of ground conditions and to include recommendations for levels of corrosion protection provided in the Deep Foundations Institute (DFI) "Guide to Drafting a Specification for High Capacity Drilled and Grouted Micropiles for Structural Support" (DFI, 2003).
- A design flowchart for micropiles used for structural support is provided. This flowchart addresses all appropriate structural and geotechnical strength and service limit states.
- Guideline information on recommended subsurface investigation (i.e., depth and spacing of geotechnical borings) has been added.
- The factor of safety for grout-ground bond has been reduced from 2.5 to 2.0 to reflect current practice. A discussion on the rationale for this modification is presented.
- Specific information on geotechnical strength limit states including vertical capacity (compression and uplift) and downdrag is provided for micropiles.
- Evaluation of combined axial compression and bending, and methods to evaluate
  potential micropile buckling have been added. Detailed information on lateral
  loading of micropiles and methods to evaluate the structural capacity at a threaded
  connection are included
- Structural design considerations for battered micropiles are included.
- Information on micropile group settlement and group lateral movement is included.
- A section on seismic considerations in the design of micropiles for seismic retrofit
  applications has been added. Relevant information from the FOREVER (2003)
  research project and design information from the current Japanese manual on seismic
  design of micropiles (Japanese Public Works Research Institute, 2002) is included.

#### Chapter 6:

- Detailed information on the feasibility of micropiles for slope stabilization projects is provided including guidance on the assessment of geotechnical parameters required for analyses. Specific information on the limitations of the design method is provided.
- Three detailed case histories on the use micropiles for slope stabilization have been added.
- The design method for micropiles used to stabilize slopes has been modified to include a step-by-step design approach with information concerning: (1) effect of micropile location on slope stability; (2) effect of passive resistance in front of micropile structure; (3) axial load transfer in a micropile used for slope stabilization; and (4) step-by-step approach to the iterative design involving the analysis of the portions of the micropiles above a potential slip surface and below a potential slip surface

#### Chapter 7:

- Guidance on the evaluations to be performed to develop a micropile load testing program for verification and proof testing are provided.
- Information is presented on the use of pile driver analyzing (PDA) techniques and Statnamic testing as a potential tool for micropile construction quality assurance.

#### Chapter 8:

• A micropile inspector responsibilities summary checklist and an updated micropile installation log are provided.

#### Chapter 10:

• Information on cost estimating is updated and includes specific information on major cost elements for micropiles including steel materials and labor costs. Information on load testing costs is also provided. Specific recommendations regarding typical measurement and payment items for a micropile project is provided.

#### 1.2 MICROPILE DEFINITION AND DESCRIPTION

A micropile is a small-diameter (typically less than 300 mm (12 in.)), drilled and grouted non-displacement pile that is typically reinforced. A micropile is constructed by drilling a borehole, placing steel reinforcement, and grouting the hole as illustrated in Figure 1-1. Micropiles can withstand relatively significant axial loads and moderate lateral loads, and may be considered a substitute for conventional driven piles or drilled shafts or as one component in a composite soil/pile mass, depending upon the design concept employed. Micropiles are installed by methods that cause minimal disturbance to adjacent structures, soil, and the environment. They can be installed where access is restrictive and in all soil types and ground conditions. Micropiles can be installed at any angle below the horizontal using the same type of equipment used for the installation of ground anchors and for grouting projects.

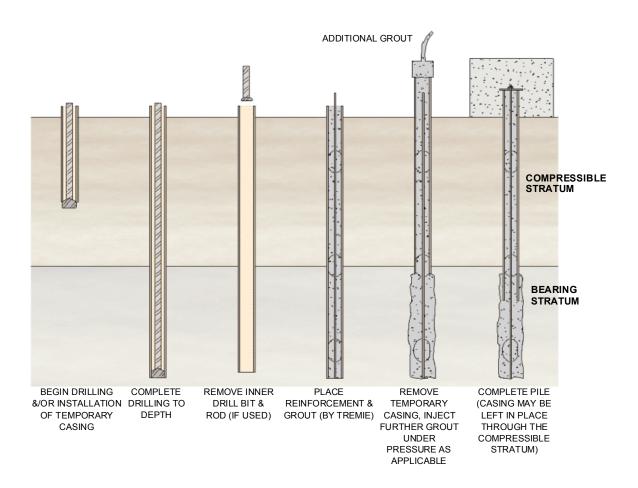


Figure 1-1. Micropile Construction Sequence.

Since the installation procedure causes minimal vibration and noise and can be used in conditions of low headroom, micropiles are often used to underpin existing structures. Specialized drilling equipment is often required to install the micropiles from within existing basement or other limited headroom facilities.

Most of the applied load on conventional cast-in-place drilled or non-displacement piles is structurally resisted by the reinforced concrete; increased structural capacity is achieved by increased cross-sectional and surface areas. Micropile structural capacities, by comparison, rely on high-capacity steel elements to resist most or the entire applied load. These steel elements may occupy as much as one-half of the drillhole cross section. The special drilling and grouting methods used in micropile installation allow for high grout/ground bond values along the grout/ground interface. The grout transfers the load through friction from the reinforcement to the ground in the micropile bond zone in a manner similar to that of ground anchors. Due to the small pile diameter, any end-bearing contribution in micropiles is generally neglected. The grout/ground bond strength achieved is influenced primarily by the ground type and grouting method used, i.e., pressure grouting or gravity feed. The role of the drilling method is also influential, although less well quantified.

#### 1.3 HISTORICAL BACKGROUND

Micropiles were conceived in Italy in the early 1950s, in response to the demand for innovative techniques for underpinning historic buildings and monuments that had sustained damage with time, and especially during World War II. A reliable underpinning system was required to support structural loads with minimal movement and for installation in access-restrictive environments with minimal disturbance to the existing structure. An Italian specialty contractor called Fondedile, for whom Dr. Fernando Lizzi was the technical director, developed the *palo radice*, or root pile, for underpinning applications. The *palo radice* is a small-diameter, drilled, cast-in-place, lightly reinforced, grouted pile. The classic arrangement of *pali radice* for underpinning is shown in Figure 1-2.

Although steel was in short supply in postwar Europe, labor was inexpensive, abundant, and often of high mechanical ability. Such conditions encouraged the development of these lightly reinforced, cast-in-place root pile elements, largely designed and installed by specialty contractors on a design-build basis. Load testing on these new root piles measured capacities in excess of 400 kN (90 kips), although the design capacity based on contemporary conventional bored pile design methodologies suggested capacities of less than 100 kN (23 kips). Direct full-scale load tests were performed at relatively little cost, fostering the

acquisition and publication of a wealth of testing information. No grout/ground bond failures were recorded during these early tests.

The use of root piles grew in Italy throughout the 1950s. Fondedile introduced the technology in the United Kingdom in 1962 for the underpinning of several historic structures, and by 1965, it was being used in Germany on underground urban transportation projects. For proprietary reasons, the term "micropile" replaced "root pile" at that time.

Initially, the majority of micropile applications were structural underpinning in urban environments. Starting in 1957, additional engineering demands resulted in the introduction of systems of *reticoli di pali radice* (reticulated root piles). Such systems comprise multiple vertical and inclined micropiles interlocked in a three-dimensional network, creating a laterally confined soil/pile composite structure (Figure 1-3). Reticulated micropile networks were used for slope stabilization, reinforcement of quay walls, protection of buried structures, and other soil and structure support and ground reinforcement applications.

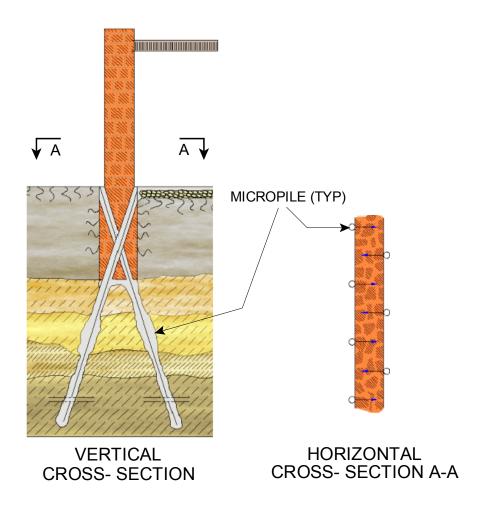


Figure 1-2. Arrangement of Root Piles (pali radice) for Underpinning.

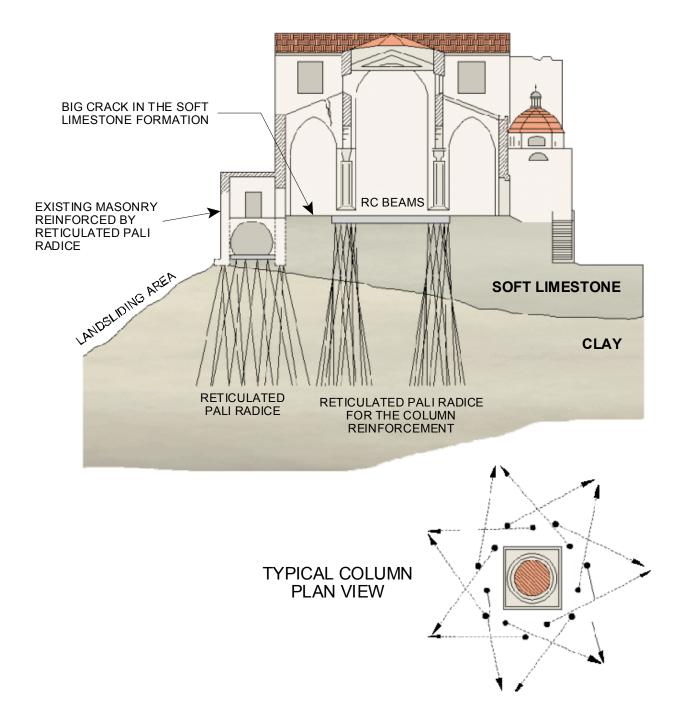


Figure 1-3. Typical Network of Reticulated (reticolo di pali radice) Micropiles.

Other proprietary micropiles were developed in Switzerland and Germany, and the technologies were quickly exported overseas by branches or licensees of the originating contractors. Portions of Asia soon became a major market.

Fondedile introduced the use of micropiles in North America in 1973 through a number of underpinning applications in the New York and Boston areas. The micropile technology did not grow rapidly in the United States, however, until the mid-1980s. At that time an abundance of successful published case histories, consistent influence by specialty contractors, and the growing needs of consultants and owners working in old urban environments overcame the skepticism and concerns of the traditional East Coast piling market (Bruce, 1988).

#### 1.4 REFERENCES

- Bruce, D. A. (1988), "Developments in Geotechnical Construction Processes for Urban Engineering", *Civil Engineering Practice*, Vol. 3, No. 1, Spring, pp. 49-97.
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# CHAPTER 2 MICROPILE CLASSIFICATION SYSTEM

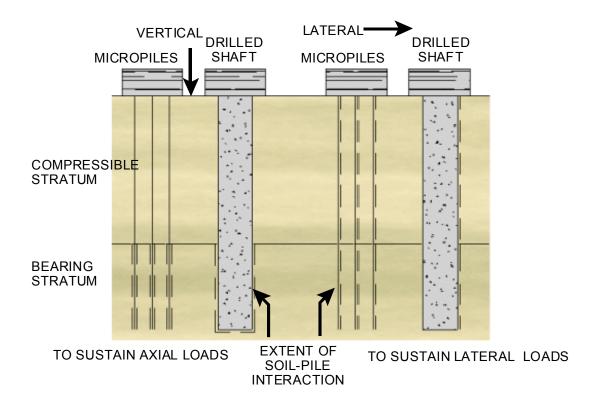
#### 2.1 INTRODUCTION

In 1997, the FHWA published a 4-volume report summarizing the state-of-the-practice for micopiles (FHWA-RD-96-016, -017, -018, and -019; 1997). In that report, a micropile classification system was developed. This system is based on two criteria: (1) philosophy of behavior (design); and (2) method of grouting (construction). The philosophy of behavior dictates the method employed in designing the micropile. The method of grouting defines the grout/ground bond strength (or side resistance), which generally controls micropile capacity. The classification system consists of a two-part designation: *a number*, which denotes the micropile behavior (design), and *a letter*, which designates the method of grouting (construction).

#### 2.2 DESIGN APPLICATION CLASSIFICATION

The design of an individual micropile or a group of micropiles differs greatly from that of a network of closely-spaced reticulated micropiles. This difference led to the definition of CASE 1 micropile elements, which are loaded directly and where the micropile reinforcement resists the majority of the applied load (Figure 2-1). CASE 2 micropile elements circumscribe and internally reinforce the soil to theoretically make a reinforced soil composite that resists applied loads (Figure 2-2). This is referred to as a reticulated micropile network.

CASE 1 micropiles can be used as an alternative to more conventional types of piles since they are used to transfer structural loads to a deeper, more competent or stable stratum. Such directly loaded piles, whether for axial (compression or tension) or lateral loading conditions, are referred to as CASE 1 elements. The load is primarily resisted structurally by the steel reinforcement and geotechnically by side resistance developed over a "bond zone" of the individual micropiles. At least 90 percent of all international applications to date, and virtually all of the projects in North America have involved CASE 1 micropiles. Such micropiles are designed to act individually, although, they may be installed in groups. Typical arrangements of CASE 1 micropiles are illustrated in Figure 2-3.



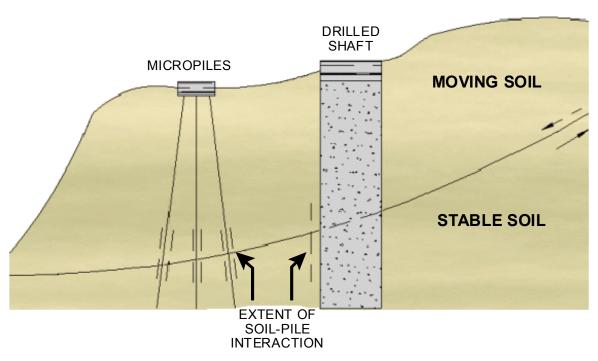


Figure 2-1. CASE 1 Micropiles.

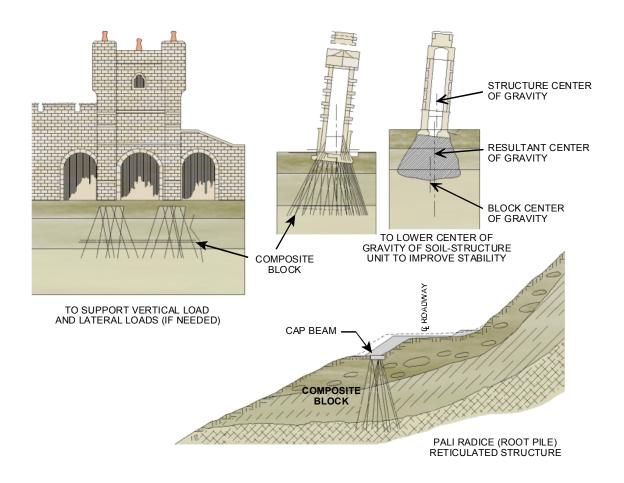
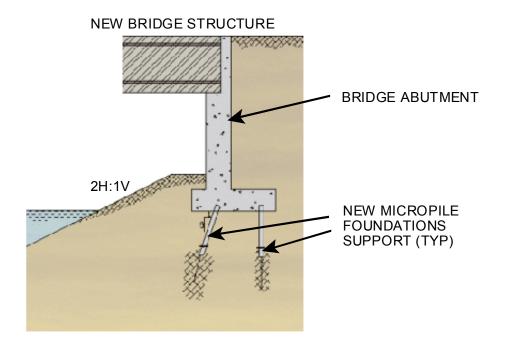
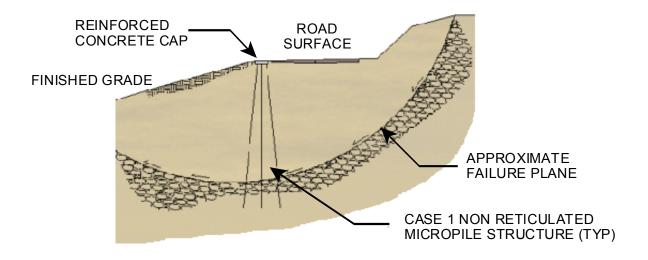


Figure 2-2. CASE 2 Micropiles – Reticulated Micropile Network.

The remaining micropile applications involve networks of reticulated micropiles as components of a reinforced soil mass which is used to provide stabilization and support. These micropiles are referred to as CASE 2 elements. Structural loads are applied to the entire reinforced soil mass, as compared to individual micropiles (as for CASE 1 micropiles). CASE 2 micropiles are lightly reinforced because they are not individually loaded. A conceptual application of a network of reticulated micropiles is illustrated in Figure 2-4.



#### **FOUNDATION SUPPORT**



#### **SLOPE STABILIZATION**

Figure 2-3. CASE 1 Micropile Arrangements.

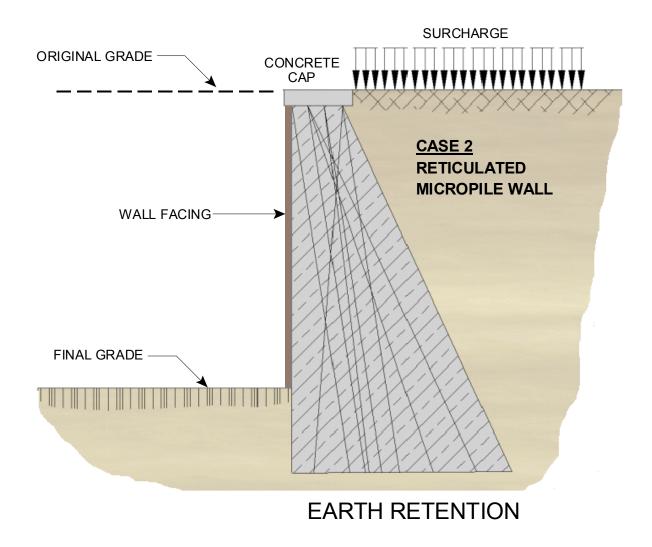


Figure 2-4. CASE 2 Micropile Arrangements.

This philosophy of behavior (design) of an individual CASE 1 micropile is the same as that of a group of CASE 1 micropiles. A group of CASE 1 elements is defined as a closely spaced (typically parallel) arrangement of micropiles, each of which will be loaded directly. Design methodologies for individual CASE 1 elements and groups of CASE 1 elements are discussed in Chapters 5 and 6. The behavior and design approach of a group of CASE 1 elements should not be confused with those of a reticulated network (i.e., CASE 2 micropiles), although their geometries may appear to be similar.

Very few CASE 2 micropile applications have been constructed in the U.S. Given the current general trend of using high capacity micropiles, the use of CASE 2 micropiles on

future U.S. projects appears to be quite limited. Also, the use of CASE 2 micropiles, especially for public sector projects, will likely be disallowed until such time that an appropriate database of performance data becomes available for these micropiles to allow for a technically sound and safe design procedure to be developed.

#### 2.3 CONSTRUCTION TYPE CLASSIFICATION

The method of grouting is typically the most sensitive construction process influencing grout/ground bond capacity. Grout/ground bond capacity varies directly with the grouting method. The second part of the micropile classification consists of a letter designation (A through D) based primarily on the method of placement and pressure under which grouting is performed during construction. The use of drill casing and reinforcement define subclassifications. The classification is shown schematically in Figure 2-5 and is described subsequently.

- **Type A:** For Type A micropiles, grout is placed under gravity head only. Sand-cement mortars or neat cement grouts can be used. The micropile excavation may be underreamed to increase tensile capacity, although this technique is not common or used with any other micropile type.
- **Type B:** Type B indicates that neat cement grout is placed into the hole under pressure as the temporary drill casing is withdrawn. Injection pressures typically range from 0.5 to 1 MPa (72 to 145 psi) to avoid hydrofracturing the surrounding ground or causing excessive grout takes, and to maintain a seal around the casing during its withdrawal, where possible.
- Type C: Type C indicates a two-step process of grouting including: (1) neat cement grout is placed under gravity head as with Type A; and (2) prior to hardening of the primary grout (after approximately 15 to 25 minutes), similar grout is injected one time via a sleeved grout pipe without the use of a packer (at the bond zone interface) at a pressure of at least 1 MPa (145 psi). This pile type appears to be used only in France, and is referred to as IGU (Injection Globale et Unitaire).

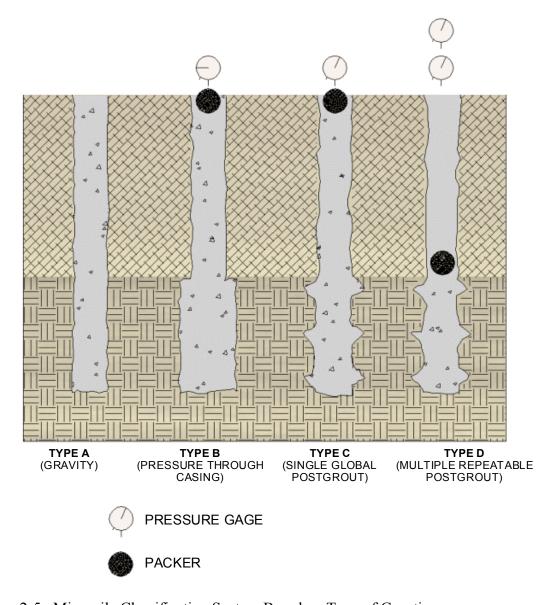


Figure 2-5. Micropile Classification System Based on Type of Grouting.

• Type D: Type D indicates a two-step process of grouting similar to Type C. With this method, neat cement grout is placed under gravity head (as with Types A and C) and may be pressurized (as for Type B). After hardening of the initially placed grout, additional grout is injected via a sleeved grout pipe at a pressure of 2 to 8 MPa (290 to 1,160 psi). A packer may be used inside the sleeved pipe so that specific horizons can be treated several times, if required. This pile type is used commonly worldwide, and is referred to in France as the IRS (Injection Répétitive et Sélective).

Table 2-1 provides additional information on Type A, B, C, and D micropiles. Subclassifications (e.g., A1, A2, and A3) are included in Table 2-1 to indicate the type of drill casing and reinforcement used for each method of grouting. These sub-classifications also represent the type of reinforcement required by design (e.g. reinforcing bar, casing, none). Therefore, the combined micropile classification system is based on design application (i.e., Case 1 or Case 2), micropile type (i.e., Type A, B, C, or D) and grouting method (i.e., 1, 2, or 3). It is emphasized that Table 2-1 is intended to present a classification system based on the type of micropile construction. It is not intended to be used in contract specifications.

#### 2.4 REFERENCES

FHWA (1997), "Drilled and Grouted Micropiles, State-of-Practice Review", Bruce, D. A. and Juran, I., Reports No. FHWA-RD-96-016, 017, 018, and 019.

Pearlman, S. L., and Wolosick, J. R. (1992), "Pin Piles for Bridge Foundations," *Proceedings, 9th Annual International Bridge Conference*, Pittsburgh, Pennsylvania, June 15-17.

Table 2-1. Details of Micropile Classification Based on Type of Grouting (after Pearlman and Wolosick, 1992).

Micropile Type and Grouting Method	Sub- type	Drill Casing	Reinforcement	Grout	
	A1	Temporary or unlined (open hole or auger)	None, single bar, cage, tube or structural section	Sand/cement mortar or neat cement grout tremied to base of hole (or casing), no excess	
Type A  Gravity grout only	A2	Permanent, full length	Drill casing itself	pressure applied	
	A3	Permanent, upper shaft only	Drill casing in upper shaft, bar(s) or tube in lower shaft (may extend full length)		
Type B	В1	Temporary or unlined (open hole or auger)	Monobar(s) or tube (cages rare due to lower structural capacity)	Neat cement grout is first tremied into drill casing/auger. Excess pressure (up to 1 MPa (145 psi) typically) is applied to additional grout injected during withdrawal of casing/auger	
Pressure - grouted through the casing or auger during	B2	Permanent, partial length	Drill casing itself		
withdrawal	В3	Permanent, upper shaft only	Drill casing in upper shaft, bar(s) or tube in lower shaft (may extend full length)		
Type C Primary grout placed	C1	Temporary or unlined (open hole or auger)	Single bars or tube (cages rare due to lower structural capacity)	Neat cement grout is first tremied into hole (or casing/auger). Between 15 to 25 minutes later, similar grout	
under gravity head, then one phase of	C2 1	Not conducted	-	injected through tube (or	
secondary "global" pressure grouting	С3	Not conducted	-	reinforcing pipe) from head, once pressure is greater than 1 MPa (145 psi)	
Type D  Primary grout placed	D1	Temporary or unlined (open hole or auger)	Single bars or tube (cages rare due to lower structural capacity)	Neat cement grout is first tremied (Type A) and/or pressurized (Type B) into hole or casing/auger. Several hours later, similar grout injected through sleeved pipe (or sleeved reinforcement) via packers, as many times as	
under gravity head (Type A) or under pressure (Type B). Then one or more phases of secondary	D2	Possible only if regrout tube placed full-length outside casing	Drill casing itself		
"global" pressure grouting	D3	Permanent, upper shaft only	Drill casing in upper shaft, bar(s) or tube in lower shaft (may extend full length)	necessary to achieve bond	

# CHAPTER 3 MICROPILE APPLICATIONS IN TRANSPORTATION PROJECTS

#### 3.1 INTRODUCTION

Micropiles are currently used in two general application areas: (1) structural support; and (2) in-situ reinforcement (Figure 3-1). Structural support includes new foundations, underpinning of existing foundations, seismic retrofitting applications and foundation support for earth retaining structures. In-situ reinforcement is used for slope stabilization and earth retention; ground strengthening; settlement reduction; and structural stability. Table 3-1 summarizes the typical design behavior and micropile construction type for each application.

Selection factors influencing the choice of micropiles for a project application are described herein. Example micropile applications for structural support and in-situ reinforcement for transportation projects and other civil engineering projects are described.

#### 3.2 FEASIBILITY OF MICROPILES

#### 3.2.1 Overview

Micropiles have specific advantages compared to more conventional support systems. In general, micropiles may be feasible under the following project-specific constraints:

- project has restricted access or is located in a remote area;
- required support system needs to be in close pile proximity to existing structures;
- ground and drilling conditions are difficult (e.g., karstic areas, uncontrolled fills, boulders);
- pile driving would result in soil liquefaction;
- vibration or noise needs to be minimized;
- hazardous or contaminated spoil material will be generated during construction; and
- adaptation of support system to existing structure is required.

Limitations and cost information for micropiles are also presented in this section.

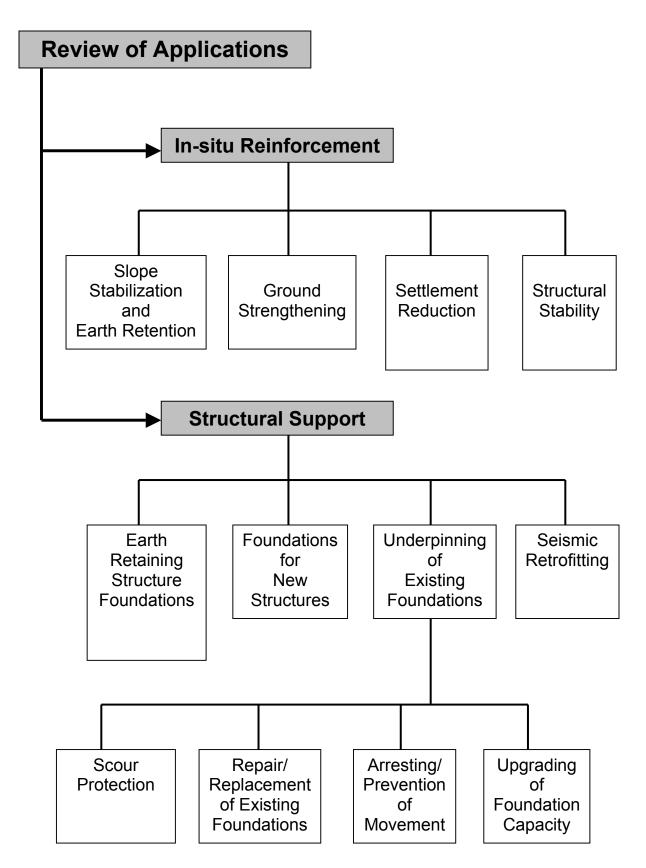


Figure 3-1. Classification of Micropile Applications.

Table 3-1. Relationship Between Micropile Application, Design Behavior and Construction Type (modified after FHWA, 1997).

	STRUCTURAL SUPPORT	IN-SITU EARTH REINFORCEMENT			
Application	Underpinning of Existing Foundations, New Foundations, and Seismic Retrofitting	Slope Stabilization and Earth Retention	Ground Strengthening	Settlement Reduction	Structural Stability
Design Behavior	CASE 1	CASE 1 and CASE 2	CASE 2 with minor CASE 1	CASE 2	CASE 2
Construction Type	Type A (bond zones in rock or stiff clays) Type B, C, and D in soil	Type A and Type B in soil	Types A and B in soil	Type A in soil	Type A in soil
Frequency of Use	Probably 95 percent of total world applications	0 to 5 percent			

## 3.2.2 Physical Considerations

The drilling and grouting equipment used for micropile installation is relatively small and can be mobilized in restrictive areas that would prohibit the entry of conventional pile installation equipment. Figure 3-2 shows micropiles being installed in low headroom conditions, illustrating the maneuverability of the equipment.

Micropiles can be installed in close proximity to existing walls or foundations, provided that there is space above for the drill-head and safe work zone or the micropiles are battered to provide this space. Micropile installation is not as affected by overhead power lines or other obstructions as are conventional pile installation systems. The equipment can be mobilized up steep slopes and in remote locations. Also, drilling and grouting procedures associated with micropile installations do not cause damage to adjacent existing structures or affect adjacent ground conditions when proper drilling and grouting procedures are utilized.



Figure 3-2. Low Headroom Micropile Installation.

#### 3.2.3 Subsurface Conditions

Micropiles can be installed in areas of particularly difficult, variable, or unpredictable geologic conditions such as ground with cobbles and boulders, fills with buried utilities and miscellaneous debris, and irregular lenses of competent and weak materials. Soft clays, running sands, and high groundwater not conducive to conventional drilled shaft systems cause minimal impacts to micropile installations. Micropiles are commonly used in karstic limestone formations.

## 3.2.4 Environmental Conditions

Micropiles can be installed in hazardous and contaminated soils. Because of their small diameter, drilling results in less spoil than would be produced by conventional drilled piles. Also, the flush effluent can be controlled easily at the ground surface through containerization or the use of lined surface pits. These factors greatly reduce the potential for surface contamination and handling costs.

Grout mixes can be designed to withstand chemically aggressive groundwater and soils. Special admixtures can be included in the grout mix design to reduce and avoid deterioration from acidic and corrosive environments. For example, a micropile "screen" was constructed from the installation of overlapping (secant) micropiles adjacent to an existing concrete

diaphragm wall of an underground parking garage in Barcelona, Spain (Bachy, 1992). The existing wall was physically deteriorating due to extremely aggressive ground water (i.e., presence of chlorides and sulfates and pH values as low as 1.7) originating from an adjacent metallurgical plant (Figure 3-3). No trace of acid was detected in samples of the diaphragm wall collected after construction of the micropile screen.

Micropiles can be installed in environmentally sensitive areas, including areas with fragile natural settings. The installation equipment is not as large or as heavy as conventional pile driving or shaft drilling equipment and can be used in swampy areas or other areas of wet or soft surface soils with minimal impacts to the environment. Portable drilling equipment is frequently used in areas of restricted access.

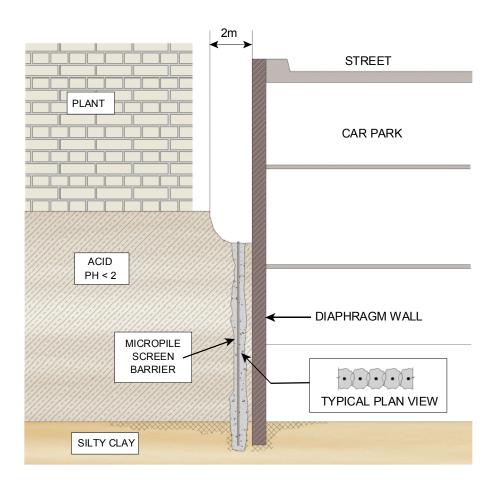


Figure 3-3. Protection of an Existing Diaphragm Wall with a Secant Micropile Screen using Anti-acid Mortar (after Bachy, 1992).

Micropile installations cause less noise and vibration than conventional piling techniques, especially driven piles. The vibration from pile driving is imparted to the soil and can be transferred through the soil to adjacent structures. The use of micropiles in old urban environments and industrial/manufacturing areas can prevent this potential damage to adjacent sensitive structures and equipment.

Micropiles can be installed in areas where there is a contaminated aquifer overlying a bearing strata. Unlike driven piles that may produce a vertical conduit for contaminate migration, micropiles can be installed in a manner preventing contamination of lower aquifers.

## 3.2.5 Existing Structure Adaptation

Micropiles can be added to an existing pile cap, thereby eliminating the need for an increased footing size. With this approach, the additional compression, tension and moment resistance associated with increased structural loads can be resisted effectively. Oftentimes adjacent utilities and/or structures restrict the possibility of enlarging the existing pile caps, thus eliminating more traditional piling systems. With this approach, design analyses need to consider the relative stiffness of the micropiles and the existing piles to estimate individual loads.

## 3.2.6 Micropile Limitations

Vertical micropiles may be limited in lateral capacity and cost effectiveness. The ability of micropiles to be installed on an incline, however, significantly enhances their lateral capacity. Because of their high slenderness ratio (length/diameter), micropiles may not be acceptable for conventional seismic retrofitting applications in areas where liquefaction may occur due to concerns of buckling resulting from loss of lateral support.

The use of micropiles for slope stabilization continues to increase. However, it is recommended that performance data be collected on such projects as experience and detailed design procedures continue to evolve.

## 3.2.7 Economics of Micropiles

The lineal cost of micropiles usually exceeds that of conventional piling systems, especially driven piles. A detailed discussion on micropile costs is provided in Chapter 10.

Cost effectiveness of micropiles depends on many factors. It is important to assess the cost of using micropiles based on the physical, environmental, and subsurface factors previously described. For example, for an open site with soft, clean, uniform soils and unrestricted

access, micropiles will likely not be a competitive solution. However, for the delicate underpinning of an existing bridge pier in a heavily trafficked old industrial or residential area, micropiles can provide the most cost-effective solution.

Care should be taken to clearly define the true final cost of a solution based on micropiles. Cost analysis should be based on all related costs for the entire project and not just the unit cost of the piling system. As with other pile systems, it would be beneficial to consider micropile costs in terms of \$/kN of axial capacity when evaluating deep foundation alternatives. Micropile costs are associated with:

- right-of-way acquisition;
- right-of-way agreements;
- utility realignment;
- excavation, shoring and backfill requirements;
- footing construction;
- hazardous material handling;
- dewatering;
- erosion control;
- access restrictions;
- ground improvement; and
- owner and neighbor disruption.

#### 3.3 STRUCTURAL SUPPORT

#### 3.3.1 Overview

Micropile applications for structural support include foundations for new structures, underpinning of existing structures, scour protection, and seismic retrofitting of existing structures. Many of these applications have been used for transportation projects. In this section, case histories involving these applications are provided.

#### 3.3.2 New Foundations

Micropiles are applicable in new bridge construction in areas that require deep foundation alternatives or in difficult ground (cobbles/boulders obstructions) where installation of conventional piles or drilled shafts is very difficult and/or expensive.

For the I-78 dual highway bridge which crosses the Delaware River between Pennsylvania and New Jersey (Bruce, 1988b), all of the original bridge piers were founded either on driven piles or spread footings on rock, with the exception of Pier E-6. At the Pier E-6 location, bedrock was encountered below the anticipated depth and was found to be karstic. Micropiles and drilled shafts were proposed as alternative foundations for the project. Micropiles were chosen as an alternative because of their lower cost and faster installation in deep karstic regions. However, because micropiles were a fairly new technology in 1988, micropile load testing was performed during the design phase to evaluate the feasibility of micropiles for this application. Load test results indicated that micropiles were feasible and micropiles were therefore used for Pier E-6.

The replacement of a two-span bridge over the Mahoning Creek in Armstrong County, Pennsylvania (Pearlman and Wolosick, 1992) required a support system to be built for new abutments (see Figure 3-4). The original stone abutment foundations were constructed in cofferdams and founded on erodible soils overlying competent sandstone. The alternatives for the project were anchored caisson walls, ground anchors, and micropiles. Micropiles were the least expensive alternative for the project. Also, micropiles could be conveniently drilled through the existing stone footings and founded in the underlying sandstone.



Figure 3–4. Micropiles Used Under New Abutments for Bridge Over Mahoning Creek, Armstrong County, PA (after Pearlman and Wolosick, 1992).

The use of micropiles allows new bridge foundations to be constructed in areas of existing overhead restrictions, while maintaining traffic flow. A major improvement project was undertaken to replace the deck of the Brooklyn-Queens Expressway in the Borough of Brooklyn, New York (Bruce and Gemme, 1992). As a part of this project, a new center lane and several new entry/exit ramps were required. Micropiles were the only alternative for the new viaduct and the ramp construction because of low headroom restrictions and stringent vibration restrictions during construction. Due to low headroom conditions, micropile casing were left full length in the ground. Also, traffic flow was maintained during construction. Although the site comprised variable fluvioglacial deposits, this did not affect the rapid installation of the micropiles.

Other micropile applications used for structural support include buildings, earth retaining structures, and soundwalls. Figure 3-5 shows typical arrangements of micropiles for support of common transportation-related structures.

## 3.3.3 Underpinning of Existing Foundations

Micropiles were originally developed for underpinning existing structures. The underpinning of existing structures may be performed for many purposes, including:

- arresting and preventing structural movement;
- for upgrading load-bearing capacity of existing structures;
- repair and replacement of deteriorating or inadequate foundations;
- to provide scour protection for erosion-sensitive foundations;
- raising previously settled foundations; and
- providing a means to transfer loads to deeper strata.

Micropiles can be installed through and bonded within existing structures providing direct connection with competent underlying strata without the need for new pile caps, while at the same time reinforcing the structure internally.

Construction can be executed without reducing the existing foundation capacity. The West Emerson Street Viaduct project in Seattle, Washington (Figure 3-6) required additional foundation support to be built at the existing bents. The additional foundation support had to be designed for both tension and compression loads. The conditions at the site included tight access and low headroom. Low headroom caissons and micropiles were the alternatives for the project. Micropiles were chosen to be added on five existing bents because of their considerable low cost compared to low headroom caissons.

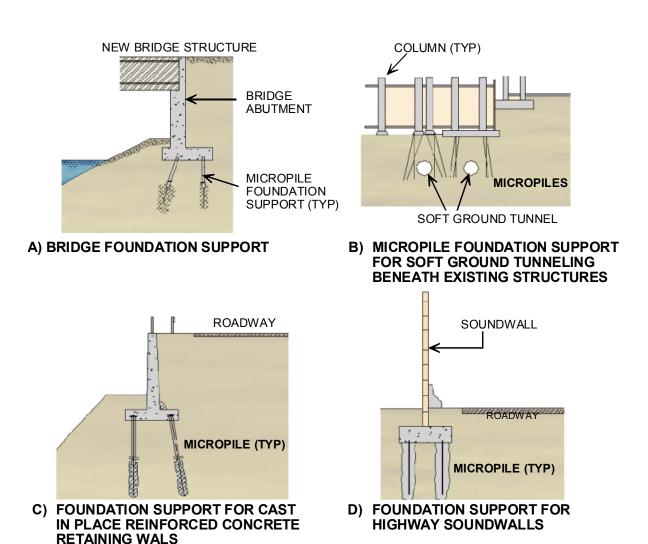


Figure 3-5. Micropiles for Foundation Support of Transportation Applications.

Structural movements can be caused by a variety of factors, including compressible ground beneath the existing foundation, dewatering activities, groundwater elevation fluctuations, deterioration of existing foundations, and adjacent deep excavations and tunneling activities. Micropiles can mitigate this structural movement by being installed to deeper, more competent bearing strata, thus providing improved structural support. Increased load-bearing capacity of an existing foundation may be required for several reasons.

Additional vertical, lateral, or vibratory loads may be applied to the foundation due to expansion of the existing structure, increased magnitude of applied loads, or the addition of vibrating machinery.



Figure 3-6. Underpinning of West Emerson Street Viaduct, Seattle, Washington.

The 75-year-old Pocomoke River Bridge in Maryland was rehabilitated when the capacity of the original wooden piles of the pier foundations was compromised by exposure to river scour (Bruce et al., 1990). Any alternative foundations system would need to be constructed in the middle of the river. The improved foundation system for the bridge was required to be preloaded before connecting to the existing structure to prevent additional settlement of the sensitive structure. Micropiles and caissons were considered for this project, and micropiles were selected for the project and installed through the existing foundation. The underpinning arrangement for the Pocomoke Bridge using micropiles is shown in Figure 3-7.

Another underpinning example is the expansion of the Exton Square Mall in Chester County, Pennsylvania (Cadden et al., 2001). The mall site is underlain by dolomitic limestone, which is defined by Pennsylvania Department of Environmental Resources as a hazardous rock due to its susceptibility to solutioning and sinkhole development. Deep foundations had to be used in order to support column loads up to 4,450 kN (1,000 kips). The alternatives evaluated for the project included drilled shafts, driven piles, and micropiles. Project constraints included performing the work while most of the stores remained open and performing all the interior work at night when the mall was closed. Micropiles were chosen as an alternative because they were judged to be best suited to the tight access, low headroom, logistical restrictions, irregular rock mass quality, and high individual pile working loads. Driven piles were not feasible because they would likely become damaged during installation.

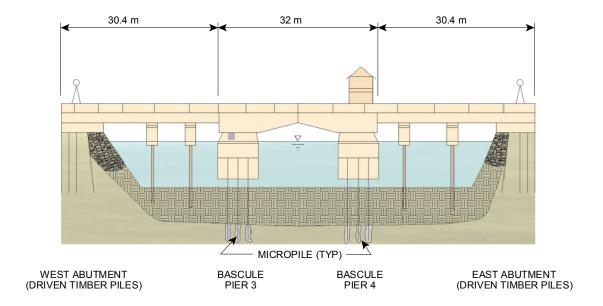


Figure 3-7. Underpining Arrangement for Pocomoke River Bridge, Maryland (after Bruce et al., 1990).

#### 3.3.4 Seismic Retrofit

Micropiles are being used increasingly for seismic retrofitting of existing highway structures, especially in California. Micropiles exhibit near equal tension and compression capacities, therefore optimizing the additional foundation support elements used (Bruce and Chu, 1995). Micropiles may be economically feasible for bridge foundation retrofits having one or more of the following constraints:

- restrictions on footing enlargements;
- vibration and noise restrictions;
- low headroom clearances;
- difficult access:
- high axial load demands in both tension and compression;
- difficult drilling/driving conditions; and
- hazardous soil sites

Micropiles were used as part of a seismic retrofit project for California Department of Transportation's earthquake retrofit project at I-110 in Los Angeles (Pearlman et al., 1993).

Micropiles were used at the north connector over-crossing (Figure 3-8). Initially drilled shafts were chosen for the project; however, difficult drilling conditions, including buried concrete obstructions and water-bearing flowing sand layers, low overhead conditions, and limited right-of-way access prohibited the use of drilled shafts. Micropiles were chosen for the project due to their lower cost and ability to be installed under difficult access conditions. Micropiles for this project were designed for tension and compression and were connected to the existing structure.

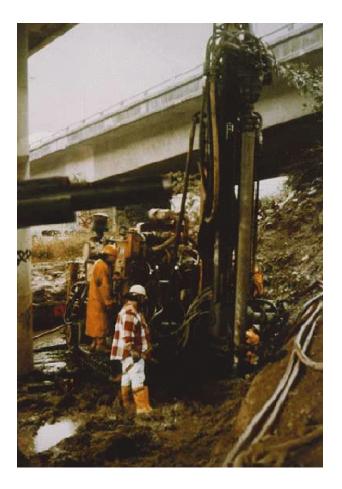


Figure 3-8. Seismic Retrofit of I-110, North Connector, Los Angeles, California.

Micropiles were used to upgrade existing foundations for a highway bridge along Route 57 near Cairo, Illinois. The seismicity for this area of southern Illinois is controlled by the New Madrid Seismic Source Zone. Micropiles were designed to withstand lateral and vertical forces from the design earthquake. The site soils consist of approximately 7.5 m (25 ft) of silty clay overlying sands. The existing pier and abutment foundations include short, vertical and batter timber piles deriving resistance from the sandy soils. The installation of a total of 240 micropiles occurred under low headroom conditions (under the bridge deck) and required excavation around the existing pier foundations. Ten micropiles were installed just

outside the perimeter of each foundation. Reinforcing steel was doweled into the existing footing and a new pile cap was poured.

Micropiles have also been used for earthquake retrofit of major bridges in the San Francisco Bay area and New York City.

#### 3.4 IN-SITU REINFORCEMENT

Micropiles are used in two different ways to stabilize slopes. Lizzi (1982) suggests that micropiles be used as reticulated network systems (CASE 2), which creates a stable, reinforced-soil, "gravity-retaining wall". In CASE 2 systems the reinforced soil gravity mass supplies the essential resisting force, and the micropiles, encompassed by the soil, supply additional resistance to the tensile and shear forces acting on the "wall". Alternately, Pearlman and Wolosick (1992) and Palmerton (1984) suggest that groups of individual inclined micropiles could be used to stabilize the slope because they serve to connect the moving zone (above the failure surface) to the stable zone (below the failure surface). These micropiles provide reinforcement to resist the shearing forces that develop along the failure surface. Typical configurations of inclined micropile groups for slope stabilization and earth retention are shown in Figure 3-9.

For rocky, stiff, or dense materials, the shear resistance of the micropiles across the failure surface, i.e., individual capacity; is critical (CASE 1). For loose materials, the micropiles and soil are mutually reinforcing and creating a gravity wall, so the individual micropile capacities are not as significant (CASE 2).

Micropiles were used to stabilize a portion of State Road 4023 in Armstrong County, Pennsylvania (Bruce, 1988a). A 75-m (250-ft) long section of this road and railroad tracks located upslope were experiencing damage from slope movements towards an adjacent river. Rock anchors and tangent drilled shafts extending into rock were the proposed techniques for in-situ reinforcement. However, alternative bidding was allowed in the project. During bidding, inclined micropile groups were proposed as an alternative to proposed techniques and were accepted due to significant cost savings. The resultant savings was approximately \$1 million compared to the lowest bid for the anchored drilled shaft wall design. The wall included four rows of micropiles extending across the failure plane and into competent rock (Figure 3-10).

Micropiles were used to provide temporary excavation support for a project involving improvements to State Highway 82 near Aspen, Colorado (Macklin et al., 2004). In this

mountainous region, construction is hampered by difficult site access and slope instability risks. This site consists of loose to very dense silty to gravelly sand with cobbles and boulders, which were deposited as debris flow, sheet wash, and colluvium over dense alluvial sandy gravel with cobbles. Originally, temporary shoring using combinations of soil nails and tiebacks was considered for the project. However, in an effort to improve the construction schedule and phasing, micropiles were selected as an alternative temporary shoring system. The micropile shoring implemented on this project was essentially a hybrid between a soldier beam and lagging system and a soil nail stabilization system (Figure 3-11). Phasing of the project required constructing a number of bridges in a specific sequence. The micropile shoring system allowed the contractor to transition access road grades where convenient, depending upon the excavation and access requirements for any phase of the work.

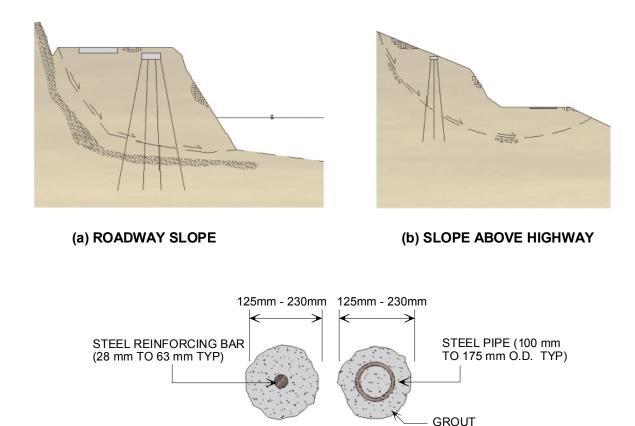


Figure 3-9. Typical Configurations for Inclined Micropile Walls.

(c) PILE SECTIONS

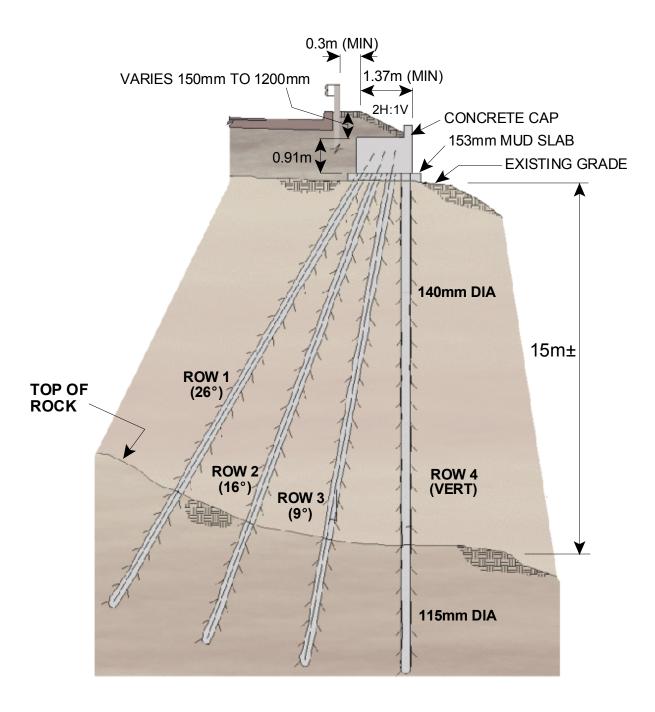


Figure 3-10. State Road 4023 Micropile Slope Stabilization, Armstrong County, Pennsylvania (after Bruce, 1988a).

The Portland Westside Light-Rail Project in Portland, Oregon is an example of the use of micropiles to provide permanent earth retention (Ueblacker, 1996). Wall 600 extends from the east portal of the Westside Light-Rail cut and cover tunnel approximately 183 m (600 ft) to just beneath the Vista Avenue Bridge. Cut heights along the retaining wall ranged from 4 to 9.5 m (13 to 30 ft). The original design included a counterfort concrete retaining wall supported on a driven pile foundation. The micropile wall was accepted as a contractor-proposed value engineering alternate, largely because it was an alternate solution that could be constructed within the available right-of-way. Micropiles were installed vertically and inclined (Figure 3-12). Shotcrete was used for a temporary facing with the permanent facing comprising an architecturally treated cast-in-place concrete.

An early example of slope stabilization using reticulated micropiles was for Forest Highway 7 in Mendocino National Forest, California (Palmerton, 1984). This project was one of the two reticulated micropiles built in U.S. at the time. The site could have been stabilized using either cantilever or anchored walls; however, there was an interest in this relatively new technology and micropiles were therefore selected as part of a demonstration project. The two-lane road of Forest Highway 7 was constructed across a landslide where slide movement had occurred as a result of excessive rainfall (Figure 3-13). A 94-m (305-ft) long section of the road was stabilized using reticulated micropiles (Figure 3-14).

Feasibility evaluation for micropiles is discussed further in Chapter 5 for structural support applications and Chapter 6 for slope stabilization applications.

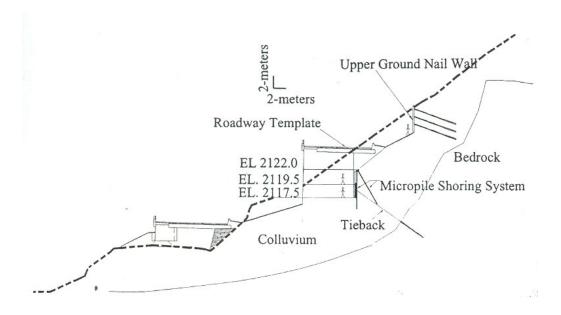


Figure 3-11. Cross Section Showing Steep Canyon Slope and Temporary Micropile Shoring (after Macklin et al., 2004).

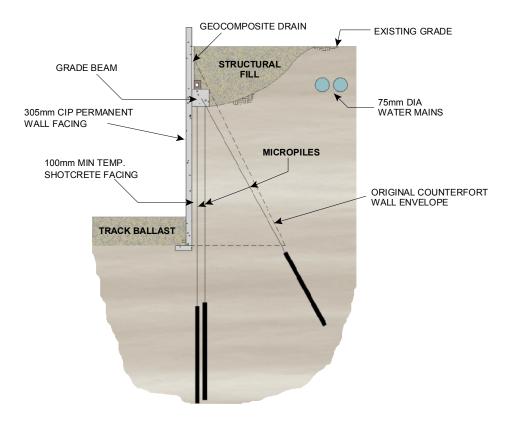


Figure 3-12. Wall 600 Permanent Earth Retention, Portland, Oregon (after Ueblacker, 1996).



Figure 3-13. Photo of Slope Stabilization at FH-7 Project in Mendocino National Forest, California.

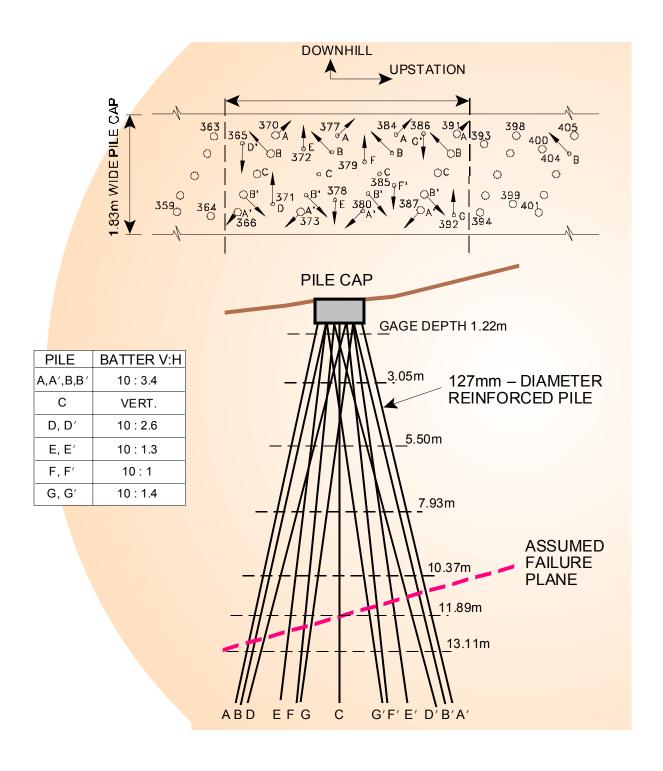


Figure 3-14. Schematic of Slope Stabilization at FH-7 Project in Mendocino National Forest, California.

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# CHAPTER 4 CONSTRUCTION TECHNIQUES AND MATERIALS

#### 4.1 INTRODUCTION

The purpose of this chapter is to familiarize design engineers and construction personnel with the different techniques and materials utilized in the construction of micropiles. Specifically, information is provided on: (1) types of drill rigs used for micropile drilling; (2) various techniques used for overburden and open hole drilling; (3) grout types with methods of mixing and placing; and (4) types of micropile reinforcement. The construction of a micropile involves a succession of processes, the most significant of which are drilling, placing the reinforcement, and grouting. There are a large number of drilling systems available for both overburden and rock and many are used for micropile construction.

The typical construction sequence for simple Type A and B micropiles (Figure 4-1) includes drilling the pile shaft to the required tip elevation, placing the steel reinforcement, placing the initial grout by tremie, and placing additional grout under pressure (for Type B). In general, the drilling and grouting equipment and techniques used for the micropile construction are similar to those used for the installation of soil nails, ground anchors, and grout holes.

#### 4.2 DRILLING

#### 4.2.1 Overview

Most drilling methods selected by the specialty contractor for a micropile project are likely to be acceptable on a particular project, provided they can form a stable hole of the required dimensions and within the stated tolerances, and without detriment to their surroundings. It is important not to exclude a particular drilling method because it does not suit a predetermined concept of how the project should be executed. It is equally important that the drilling contractor be knowledgeable of the project ground conditions, and the effects of the drilling method chosen. Drilling within a congested urban site in close proximity of older buildings or deteriorating foundations has very different constraints than drilling for new foundations on an open field site.

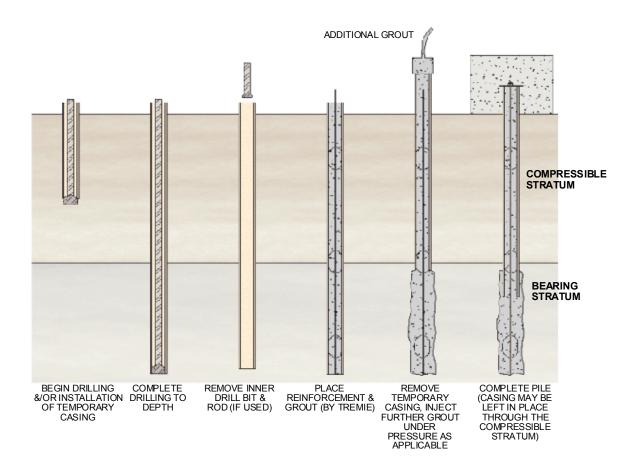


Figure 4-1. Typical Micropile Construction Sequence Using Casing.

The act of drilling and forming the pile excavation may disturb the surrounding ground for a certain time and over a certain distance. The drilling method selected by the contractor should avoid causing an unacceptable level of disturbance to the site and its facilities, while providing for installation of a micropile that supports the required capacities in the most cost-effective manner. Vigorous water flushing can increase drilling rates and increase the removal of the fine components of mixed soils, enlarging the effective diameter in the bond zone and aiding in grout penetration and micropile capacity. Conversely, the use of higher flush flow rates and pressures should be approached with caution, with consideration to the risks of creating voids and surface settlement, and the risks of hydrofracturing the ground which could result in ground heave.

Drilling, installation of the reinforcement, and grouting of a particular micropile should be completed in a series of continuous processes and executed as expeditiously as possible. Longer durations between completion of drilling and placing of the reinforcement and grout can be detrimental to the integrity of the surrounding soil. Some materials, such as overconsolidated clays and clay shales, can deteriorate, relax, or soften as a result of

exposure, resulting in a loss of interfacial bond capacity. In these cases, installation of a micropile bond zone should be completed within one day to avoid a pile hole remaining open overnight.

Other site-specific conditions may affect selection of the drilling method and flush type. The use of water flush may require the supply, handling, and disposal of large quantities of water. In areas where the water supply may be scarce, a series of ponds or tanks for settlement and recirculation of the water may be necessary. Requirements for cleanliness or lack of space for water handling and disposal may dictate the use of air flush or augers for hole drilling. The presence of hazardous materials in the ground and the need for careful control and disposal of the soil cuttings may also necessitate the use of augers for micropile installation.

## 4.2.2 Drill Rigs

Drill rigs typically used for micropile installation are hydraulic rotary (electric or diesel) power units. They can be track mounted allowing for maneuverability on difficult and sloped terrain. The size of the track-mounted drills can vary greatly, as seen in Figure 4-2 and 4-3, with the larger drill allowing use of long sections of drill rods and casing in areas without overhead restrictions and the smaller drill allowing work in lower overhead and harder-to-reach locations. The drill mast can be mounted on a frame allowing work in limited-access and low-overhead areas, such as building basements.

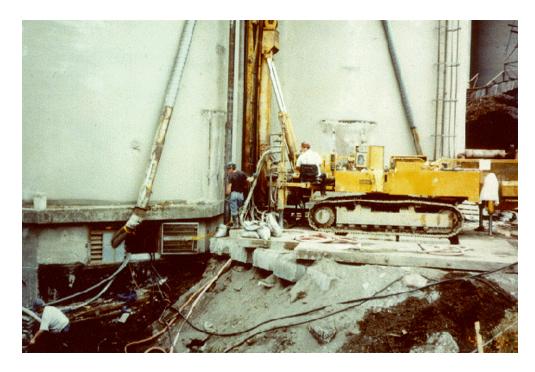


Figure 4-2. Large Track-Mounted Rotary Hydraulic Drill Rig.



(a)



(b)

Figure 4-3. Low Headroom Track-Mounted Rotary Hydraulic Drill Rig (a) not Mounted and (b) Mounted for Drilling.

A frame-mounted drill such as the one shown in Figure 4-4 can be connected with long hoses to a separate hydraulic rotary power unit. This allows placement of the power unit outside the area of work, thus reducing space requirements, noise in the work area, and problems with exhaust removal. The drill frame can be moved and supported with a fork lift or moved by hand with winches and supported by bolting to a concrete floor, and/or bridge footing or bracing from a ceiling or bridge soffit.

The rotary head that turns the drill string (casing, augers, or rods) can be extremely powerful on even the smallest of rigs, allowing successful installation in the most difficult ground conditions. Shortening of the drill mast and the use of short jointed sections of drill string and micropile reinforcement allows pile installation with less than 3 m (10 ft) of overhead clearance. For a vertical micropile, the micropile centerline can be located within approximately 375 mm (15 in.) of the face of an adjacent wall. This distance may need to increase for micropiles larger than approximately 175 mm (7 in.) in diameter.



Figure 4-4. Small Frame-Mounted Rotary Hydraulic Drill Rig.

## 4.2.3 Drilling Techniques

The drilling method is selected with the objective of causing minimal disturbance or upheaval to the ground and structure while being the most efficient, economic, and reliable means of penetration. Micropiles must often be drilled through an overlying weak material to reach a more competent bearing stratum. Therefore, construction typically requires the use of overburden drilling techniques to penetrate and support weak and unconsolidated soils and fills. In addition, unless the bearing stratum is a self-supporting material, such as rock or a cohesive soil, the drill hole may need temporary support for its full length, e.g. through the use of temporary casing (Figure 4-5) or suitable drilling fluid. If self-supporting material is present for the full depth of the micropile, the drillhole can possibly be formed by open hole techniques, i.e., without the need for temporary hole support by drill casing or hollow stem auger.

Alternative drilling methods are required to penetrate through an existing structure (Figure 4-6). Concrete coring techniques may be used to provide an oversized hole in existing slabs and footings to allow the subsequent drill casing to pass through. In some cases, conventional rock drilling methods involving rotary percussive techniques can be used to penetrate existing lightly-reinforced footings and structures. Rotary percussive (Figure 4-7) or rotary duplex (Figure 4-8) techniques may be used to first penetrate an initial obstruction layer, such as concrete rubble, with more conventional single-tube advancement drilling used for completion of the micropile shaft in the soil layers below.

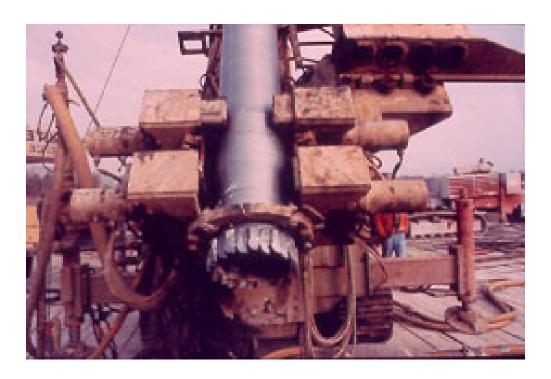


Figure 4-5. Casing with Heavy Duty Casing Crown.

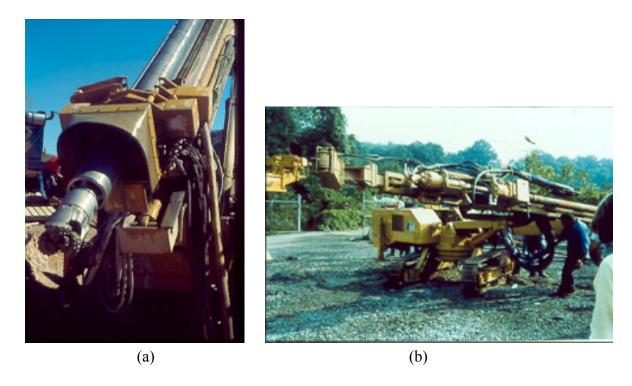


Figure 4-6. Drill Rigs Equipped (a) with Tricone Roller Bit and (b) for Double Head Drilling.

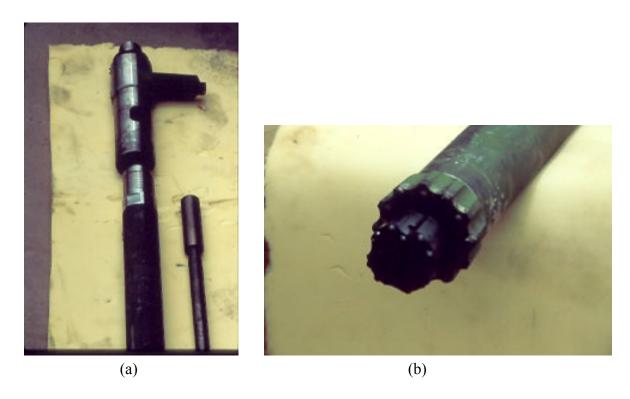


Figure 4-7. Rotary Percussive Drilling (a) Drive Head and (b) Drive Bit and Shoe.

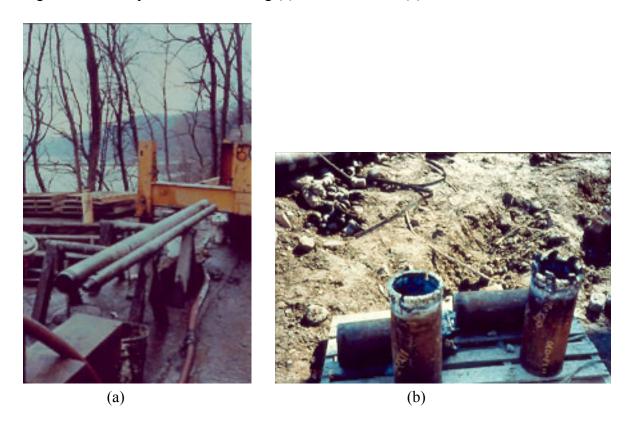


Figure 4-8. Rotary Duplex Drilling (a) Drill Rods and (b) Various Casing Shoes.

Water is the most common medium for cleansing and flushing the hole during drilling, followed by air, drill slurries, and foam. Caution should be exercised while using air flush to avoid injection of the air into the surrounding ground, causing fracturing and heaving. The use of bentonite slurries to stabilize and flush holes will impair grout-to-ground bond capacity by creating a skin of clay at the interface; however, this is not an uncommon choice in Italian and French practice with Type D piles. Polymer drilling muds have been used successfully in micropile construction in all types of ground. This slurry type reduces concern for impairment of the bond capacity, and allows for easier cleanup and disposal versus bentonite slurry.

## 4.2.4 Overburden Drilling Techniques

There is a large number of proprietary overburden drilling systems sold by drilling equipment suppliers worldwide. In addition, specialty contractors often develop their own variations in response to local conditions and demands. The result is large selection of systems and methods. However, seven generic methods have been identified which are common for piles with diameters less than 300 mm (12 in) to depths less than 60 m (200 ft). The following is a brief discussion of these seven methods. These seven methods are also summarized in Table 4-1, and simply represented in Figure 4-9.

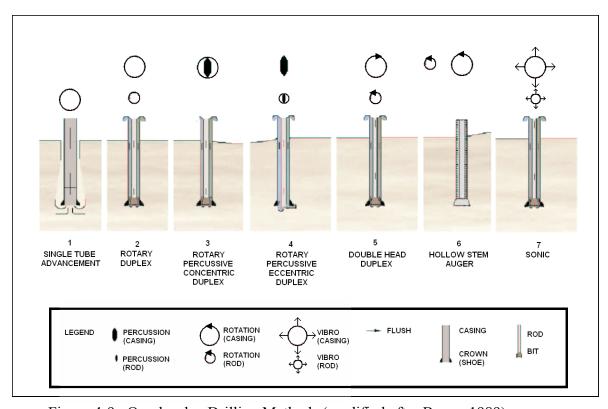


Figure 4-9. Overburden Drilling Methods (modified after Bruce, 1989).

Table 4-1. Overburden Drilling Methods (after Bruce, 1989).

	<b>Drilling Method</b>	Principle	Common Diameters and Depths	Notes
1	Single-tube advancement a) Drive drilling	Casing with "lost point" percussed without flush	50-100 mm to 30 m (2-4 in. to 100 ft)	Obstructions or very dense soil problematic.
	b) External flush	Casing, with shoe, rotated with strong water flush.	100-250 mm to 60 m (4-10 in. to 200 ft)	Needs high torque head and powerful flush pump.
2	Rotary duplex	Simultaneous rotation and advancement of casing plus internal rod, carrying flush. Rod may have down-the-hole hammer.	100-220 mm to 70 m (4-8.75 in. to 230 ft)	Used only in very sensitive soil/site conditions. Needs positive flush return. Needs high torques. (Internal flushing only)
3	Rotary percussive concentric duplex	As 2, except casing and rods percussed as well as rotated.	89-175 mm to 40 m (3.5-7 in. to 130 ft)	Useful in obstructed/rocky conditions. Needs powerful top rotary percussive hammer.
4	Rotary percussive eccentric duplex	As 2, except eccentric bit on rod cuts oversized hole to ease casing advance.	89-200 mm to 60 m (3.5-8 in. to 200 ft)	Expensive and difficult system used for difficult overburden. Rod can be percussive at top, or may have down-the-hole hammer above bit.
5	"Double head" duplex	As 2 or 3, except casing and rods may rotate in opposite directions.	100-150 mm to 60 m (4-6 in. to 200 ft)	Powerful, new system for fast, straight drilling in very difficult ground. Need significant hydraulic power. Casing can be percussed by top hammer. Rod may be percussed by top hammer or may have down-the-hole hammer above bit.
6	Hollow-stem auger	Auger rotated to depth to permit subsequent introduction of grout and/or reinforcement through stem.	100-400 mm to 30 m (4-16 in. to 100 ft)	Obstructions problematic; care must be exercised in cohesionless soils. Prevents application of higher grout pressures.
7	Sonie	Casing is excited by a variable frequency, variable amplitude, sonic head	100 to 300 mm to 100 m (4-12 in. to 330 ft)	No or minimal flush needed. Full length sample of soil recovered for each hole.

Note: Drive drilling, being purely a percussive method, is not described in the text as it has no application in micropile construction.

• Single-Tube Advancement-External Flush (Wash Boring): The toe of the drill casing is fitted with an open crown or bit and the casing is advanced into the ground by rotation of the drill head. Water flush is pumped continuously through the casing, which washes debris out and away from the crown. The water-borne debris typically escapes to the surface around the outside of the casing, but may be lost into especially loose and permeable strata. Care must be exercised below sensitive structures in order that uncontrolled washing does not damage the structure by causing cavitation.

Air flush is not normally used with this system due to the danger of accidentally over pressurizing the ground in an uncontrolled manner which can cause ground disturbance. Conversely, experience has shown that polymer drill flush additives can be very advantageous in certain ground conditions, in place of water alone (Bruce, 1992). These do not appear to detrimentally affect grout-to-soil bond development as may be the case with bentonite slurries.

- Rotary Duplex: The drill rod with a suitable drill bit is placed inside the drill casing. It is attached to the same rotary head as the casing, allowing simultaneous rotation and advancement of the combined drill and casing string. The flushing fluid, usually water or polymer flush, is pumped through the head down through the central drill rod to exit from the flushing ports of the drill bit. The flush-borne debris from the drilling then rises to the surface along the annulus between the drill rod and the casing. At the surface, the flush exits through ports in the drill head. Air flush must be used with caution because blockages within the annulus can allow high air pressures to develop at the drill bit and cause ground disturbance.
- Rotary Percussive Duplex (Concentric): Rotary percussive duplex systems are a development of rotary duplex methods, whereby the drill rods and casings are simultaneously percussed, rotated, and advanced. The percussion is provided by a top-drive rotary percussive drill head. This method requires a drill head of substantial rotary and percussive energy.
- Rotary Percussive Duplex (Eccentric or Lost Crown): Originally sold as the Overburden Drilling Eccentric (ODEX) System, this method involves the use of rotary percussive drilling combined with an eccentric underreaming bit. The eccentric bit undercuts the drill casing, which is then pushed into the oversized drill hole with much less rotational energy or thrust than is required with the concentric method. The drill casing does not require an expensive cutting shoe and suffers less wear and abrasion. The larger diameter options, of more than 127 mm (5 in.) in diameter, often involve the use of a down-the-hole hammer acting on a drive shoe at

the toe of the casing so that the casing is effectively pulled into the borehole as opposed to being pushed by a top hammer.

- **Double Head Duplex:** With the double head duplex method, the rods and casings are rotated by separate drill heads mounted one above the other on the same carriage. These heads provide high torque (and so enhanced soil- and obstruction-cutting potential), but at the penalty of low rotational speed. However, the heads are geared such that the lower one (rotating the outer casing), and the upper one (rotating the inner drill string) turn in opposite directions. The resulting aggressive cutting and shearing action at the bit permits high penetration rates, while the counter-rotation also minimizes blockage of the casing/rod annulus by debris carried in the exiting drill flush. In addition, the inner rods may operate by either purely rotary techniques or rotary percussion using top-drive or down-the-hole hammers. The counter-rotation feature promotes exceptional hole straightness and penetrability, even in the most difficult ground conditions.
- Hollow-Stem Auger: Hollow-stem augers are continuous flight auger systems with a central hollow core similar to those commonly used in auger-cast piling or for subsurface investigation. These are installed by purely rotary heads. When drilling down, the hollow core is closed off by a cap on the drill bit. When the hole has been drilled to depth, the cap is knocked off or blown off by grout pressure, permitting the pile to be formed as the auger is withdrawn. Such augers may be used for drilling cohesive materials, very soft rocks, and are commonly used in sands. If used in sands with minimal cohesion or adhesion, there is a danger of loosening or cavitating the soil, especially in inclined holes. Post grouting is essential (Type D).

Various forms of cutting shoes or drill bits can be attached to the lead auger, but heavy obstructions, such as old foundations and cobble and boulder soil conditions, are difficult to penetrate economically with this system. In addition, great care must be exercised when using augers as uncontrolled penetration rates or excessive "hole cleaning" may lead to excessive spoil removal, thereby risking soil loosening or cavitation in certain circumstances.

• Sonic: Sonic drilling is a dual cased drilling system that employs high frequency mechanical vibration to take continuous core samples of overburden and most bedrock formations, and to advance casing into the ground. Other names for sonic drilling include rotosonic, rotasonic, sonicore, vibratory or resonant sonic drilling. The entire drill string is vibrated at a frequency of between 50 and 150 hertz and evenly distributes the energy and wear at the drill bit face. The rig uses a specially

designed hydraulically powered drill head or oscillator that is attached directly to the core barrel, drill pipe or outer casing. The vibrations are sent down through the drill steel to the face of the drill bit creating displacement, fracturing or shearing action depending on the material being drilled.

## 4.2.5 Open Hole Drilling Techniques

When a micropile can be formed in stable and free-standing conditions, the advancement of casing may be suspended and the hole continued to final depth by open-hole drilling techniques. There is a balance in cost between the time lost in changing to a less-expensive open-hole system and continuing with a more expensive overburden drilling system for the full hole depth. Open-hole drilling techniques may be classified as follows:

• Rotary Percussive Drilling: Particularly for rocks of high compressive strength, rotary percussive techniques using either top-drive or down-the-hole hammers are utilized. For the small hole diameters used for micropiles, down-the-hole techniques are the most economical and common. Air, air/water mist, or foam is used as the flush.

Top-drive systems can also use air, water, or other flushing systems, but have limited diameter and depth capacities, are relatively noisy, and may cause damage to the structure or foundation through excessive vibration.

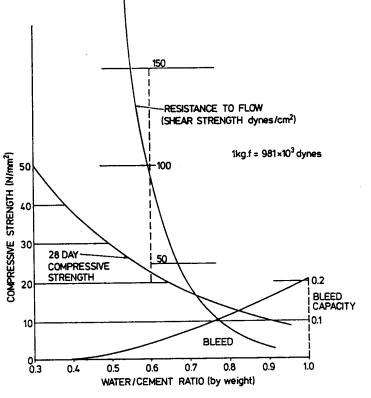
- Solid Core Continuous Flight Auger: In stiff to hard clays without boulders and in some weak rocks, drilling may be conducted with a continuous flight auger. Such drilling techniques are rapid, quiet, and do not require the introduction of a flushing medium to remove the spoil. There may be the risk of lateral decompression or wall remolding/interface smear, either of which may adversely affect grout-to-ground bond. Such augers may be used in conditions where the careful collection and disposal of drill spoils are particularly important.
- Underreaming: Various devices have been developed to enlarge or underream open holes in cohesive soils or soft sediments, especially when the micropiles are to act in tension. These tools can be mechanically or hydraulically activated and will cut or abrade single or multiple underreams or "bells." However, this is a time-consuming process, and it is rarely possible or convenient to verify its effectiveness. In addition, the cleaning of the underreams is often difficult; water is the best cleaning medium, but may cause softening of the ground. For all these reasons, it is rare to find underreaming used in typical micropile practice.

#### 4.3 GROUTING

#### 4.3.1 General

As described in Chapter 2, the grouting operations have a major impact on micropile capacity. Details of each type of grouting operation vary somewhat throughout the world, depending on the origins of the practice and the quality of the local resources. However, as general observations, it may be noted that:

- Grouts are designed to provide high strength and stability (i.e., bleed), but must also be pumpable. As shown in Figure 4-10, this implies typical water/cement (w/c) ratios in the range of 0.40 to 0.50 by weight for micropile grout. In Figure 4-10, bleed capacity is defined as amount of free water that develops at final set. For example, for a w/c ratio of 1.0, 100 liters of grout would develop 20 liters of free water.
- Grouts are produced with potable water, to reduce the danger of reinforcement corrosion.



 $1 \text{ N/mm}^2 = 145 \text{ psi}$  $1 \text{ dyne/cm}^2 = 1.45 \times 10^{-5} \text{ psi}$ 

Figure 4-10. Effect of Water Content on Grout Compressive Strength and Flow Properties (after Littlejohn and Bruce, 1977).

- Type I/II cement conforming to ASTM C150/AASHTO M85 is most commonly used, supplied either in bagged or bulk form depending on site condition, job size, local availability, and cost.
- Neat cement-water grout mixes are most commonly used, although sand is a common additive in certain countries (e.g., Italy, Britain). Bentonite (which reduces grout strength) is used in primary mixes only with extreme caution, while additives are allowed only for cases where improved pumpability is required as for pumping over long distances and/or in hot conditions (e.g., high-range water reducers).
- Design compressive strengths of 28 to 35 MPa (4,000 to 5,000 psi) can be attained with properly produced neat cement grouts.
- If admixtures and/or additives are used, it is essential that they are chemically compatible. This is best achieved by using only one chemical supplier, and <u>not</u> by "mixing and matching".

The placed grout is required to serve a number of purposes, as described below.

- It transfers the imposed loads between the reinforcement and the surrounding ground.
- It may form part of the load-bearing cross section of the micropile.
- It serves to protect the steel reinforcement from corrosion.
- Its effects may extend beyond the confines of the drill hole by permeation, densification, and/or fissuring.

The grout, therefore, needs to have adequate properties of fluidity, strength, stability, and durability. The need for grout fluidity can mistakenly lead to an increase in water content which has a negative impact on the other three properties. Of all the factors that influence grout fluidity and set properties, the water/cement ratio is the most important. Again, Figure 4-10 illustrates why this ratio is limited to a range of 0.40 to 0.50, although even then, additives may be necessary to ensure adequate pumpability for ratios less than 0.40.

It is essential to the integrity of the micropile that upon completion of the grouting operation, there is no significant loss of grout from any part of the micropile that will be relied upon for load bearing or corrosion protection. This condition can be achieved by grouting to refusal during micropile formation, i.e. continue grouting until no more grout take occurs. Problems with grout loss may necessitate the use of a filler such as sand for plugging the permeable layer, or may require pre-grouting the hole and redrilling and regrouting after set of the initial grout. Loss of grout is judged simply by observing the level of grout which remains in the hole after the grout has stiffened. For general guidance, a grout take over twice the "neat"

hole volume is indicative of voided or very permeable conditions warranting special attention.

For a Type B micropile, it may not always be possible to attain the desired pressures during grouting; the soil seal around the casing may not always be adequate to contain the pressurized grout. This may occur after partial pressure grouting of the bond length. If this occurs, the grout should be pumped until the level reaches the top of pile, at which time grouting is discontinued. Maintaining grout pressures at a reasonable level (0.70 MPa (100 psi) or less) will help prevent this from occurring. If the bond lengths of the test micropiles (that verified the geotechnical capacity) are grouted full length with the desired pressure, questions may be raised as to the adequacy of micropiles that are grouted under partial pressure. One benefit of conducting micropile tests to typically 150 to 200 percent of the design load or greater is that it helps to determine if the micropiles have excess geotechnical capacity. Production proof tests (described in Chapter 7) may be conducted on the suspect micropiles.

Because the grout is such a vital component of the micropile, close attention must be paid to the control and quality of the product. A grout quality control plan, which at a minimum should include cube or cylinder compression testing and grout density (water /cement ratio) testing, is discussed in Chapter 8.

Comprehensive guides to cement grout mix design, performance, and equipment are provided in Littlejohn (1982), Gourlay and Carson (1982), and Houlsby (1990). Similar issues relating solely to the similar demands of prestressed ground anchors are summarized by Littlejohn and Bruce (1977).

## 4.3.2 Grout Equipment

In general, any plant suitable for the mixing and pumping of fluid cementitious grouts may be used for the grouting of micropiles. The best quality grouts, in terms of both fluid and set properties, are produced by high-speed, high-shear colloidal mixers (see Figure 4-11) as opposed to low-speed, low-energy mixers, such as those that depend on paddles (Figure 4-12). High speed mixers are faster and produce a homogeneous grout mix (see Section 4.3.3). Mixing equipment can be driven by air, diesel, or electricity, and is available in a wide range of capacities and sizes from many manufacturers.

For grout placement, lower pressure injection (up to 2 MPa (290 psi)) and up to 200 liters/min (52 gal/min)) is usually completed using constant pressure, rotary-screw type pumps (e.g., Moyno pumps), while higher pressure grouting, such as for Type C or D

micropiles, usually requires a fluctuating pressure piston or ram pump, which can deliver up to 8 MPa (1,160 psi) at up to 50 liters/min (13 gal/min).

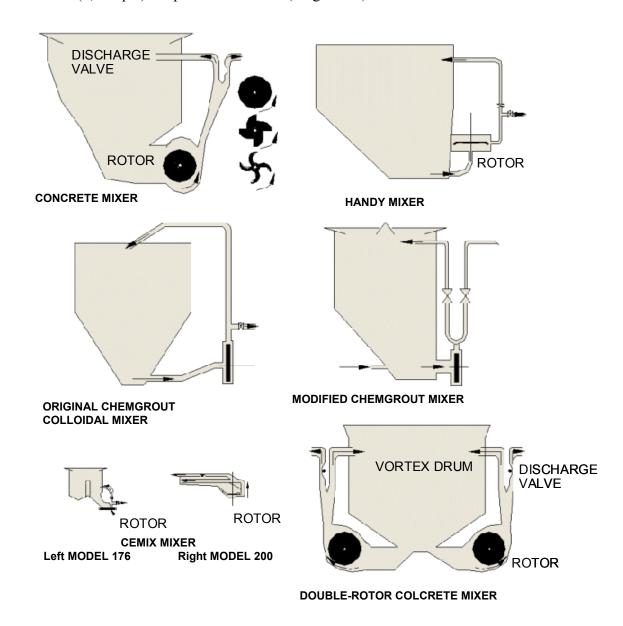


Figure 4-11. Various Types of High Speed, High Shear "Colloidal" Mixers.

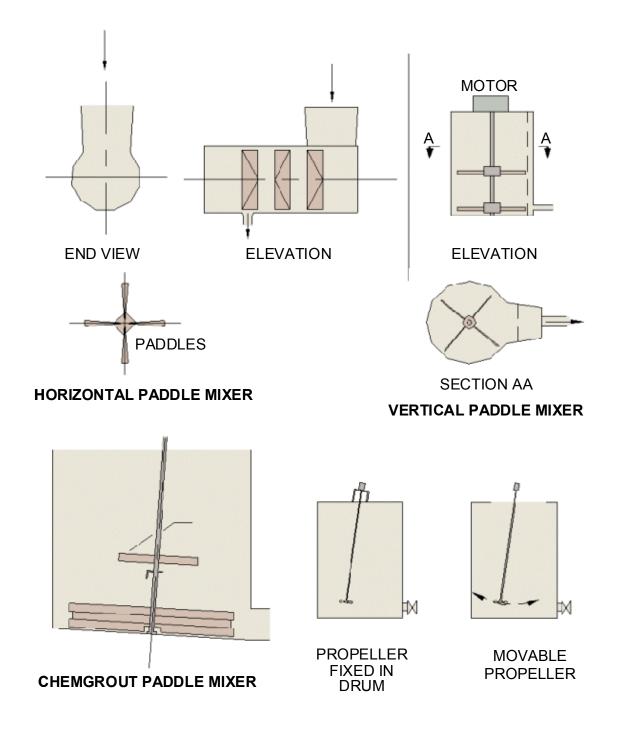


Figure 4-12. Various Types of Paddle Mixers.

## 4.3.3 Grout Mixing

During mixing, a measured volume of water is usually added to the mixer first, followed by cement and then aggregate or filler (if applicable). It is generally recommended that grout be mixed for a minimum of two minutes and that thereafter the grout is kept in continuous slow agitation in a holding tank prior to being pumped to the micropile. Only in cases where exceptionally large grout takes are anticipated should ready-mix grout be considered. The grout should be injected within a certain maximum time after mixing. This "safe workability" time should be determined on the basis of on-site tests, but is typically not in excess of one hour. There is no question that high speed high shear mixers produce higher quality, more consistent grout more quickly than do paddle mixers. Bearing in mind the relatively large cement particle surface area to be "wetted" (measured in "football fields" per single 43 kg bag), and that this must be accomplished with less than 20 liters of water, the intimate blending generated by the high speed mixer is essential for efficient hydration.

Water is typically batched into the mixer by means of a calibrated tank or flow meter. Cement is typically batched by weight, either in bags or by bulk from a silo. Sand or fillers are also batched by weight from premeasured bags or more commonly, by using a gage box that has previously been checked and weighed. For bulk material, some method must be provided for controlling the quantities of components (volume or weight measurement) added to the mix. Admixtures are usually provided ready-proportioned to a single bag of cement, or the dosage can be adjusted by the mixer operator.

## 4.3.4 Grout Placement Techniques

## 4.3.4.1 Gravity Fill Techniques (Type A Micropiles)

For Type A micropiles, the hole is drilled to depth and it is then filled with grout and the reinforcement is placed. Grout should always be introduced into the drill hole through a tremie pipe exiting at the bottom of the hole. Grout is pumped into the bottom of the hole until grout of similar quality to that being injected is freely flowing from the mouth of the borehole. No excess pressure is applied. This type and phase of grouting is referred to as the *primary treatment*.

The grout usually comprises a neat cement mix with w/c ratio between 0.45 and 0.50 by weight. Additionally, sanded mixes of up to 1:1 or 2:1 sand:cement ratio have been used in European practice, but they are becoming less common due to a growing trend towards the use of higher grouting pressures involving neat cement grouts. Gravity fill techniques tend now to be used only when the pile is founded in rock, or when low-capacity piles are being installed in stiff or hard cohesive soils, and pressure grouting is unnecessary (Bruce and

Gemme, 1992). For sanded mixes, the w/c ratio is often extended to 0.60, assuming the resultant mix remains stable (i.e., bleed less than 5 percent and sand does not segregate) (Barley and Woodward, 1992). In the U.S., sanded mixes are only used for pregrouting, e.g., in karst terrains, for economic reasons.

## 4.3.4.2 Pressure Grouting Through the Casing (Type B Micropiles)

For Type B micropiles, additional grout is injected under pressure after the primary grout has been tremied, and as the temporary casing is being withdrawn. The aim is to enhance the grout-to-ground bond characteristics. This operation can be limited to the load transfer length within the design-bearing stratum, or may be extended to the full length of the pile where appropriate.

Pressure grouting is usually conducted by attaching a pressure cap to the top of the drill casing (this is often the drilling head itself) and injecting additional grout into the casing under controlled pressure. In the past, pressurization of the grout was achieved by applying compressed air through the grout line, since contemporary drill head details and grout pump technology could not accommodate the relatively viscous, sand-cement mortars. This method has now been rendered obsolete by the developments in pump capabilities, combined with the trend to use stable, neat cement grouts without sand.

Grout pressures are measured as close to the point of injection as possible, to account for line losses between pump and hole. Commonly, a pressure gauge is mounted on the drill rig and monitored by the driller as a guide for rate of casing withdrawal during the pressurization phase. Alternatively, if a grouting cap is used and the casing is being extracted by means other than the drill rig (e.g., by hydraulic jacks), it is common to find a pressure gauge mounted on the cap itself. Practitioners acknowledge that there will be line losses in the system, but typically record the pressure indicated on the pressure gauge without the correction, reasoning that such losses are compensated by the extra pressure exerted by the grout column due to its weight in the borehole. The recommended method is to install a pressure gauge on the drill rig or on the line just at the cap.

American practice is to inject additional grout at a typical average pressure between 0.5 to 1 MPa (72 to 145 psi), with the aim of reinstating in-situ lateral soil pressures that may have been reduced by the drilling process and achieving permeation into coarser grained granular soils or fractured rocks. The maximum applied injection pressures (typically 20 kPa per meter (18 psi per ft) of depth in loose soils and 40 kPa per meter (36 psi per ft) of depth in dense soils) are dictated by the following factors:

need to avoid ground heave or uncontrolled loss of grout;

- nature of the drilling system (permissible pressures are lower for augers due to leakage at joints and around the flights);
- ability of the ground to form a "seal" around the casing during its extraction and pressure grouting;
- need to avoid "seizing" the casing by flash setting of the grout due to excessive pressure, preventing proper completion of the pile;
- required grout-to-ground bond capacity; and
- total micropile depth.

The injection of grout under pressure is aimed at improving grout-to-ground skin friction, thus enhancing the load-carrying capacity of the micropile. Extensive experience with ground anchors has confirmed the effect of pressure grouting on ultimate load-holding capacity.

When pressure grouting in granular soils, a certain amount of permeation and displacement (i.e., slight redensification or compaction occurs to "repair" the soil locally loosened during drilling) of loosened soils takes place. Additionally, a phenomenon known as pressure filtration occurs, wherein the applied grout pressure forces some of the integral mixing water out of the cement suspension and into the surrounding soil. This process leaves behind a grout of lower water content than was injected and is thus quicker setting and of higher strength. It also causes the formation of cake-like cement paste along the grout/soil interface that improves bond. In cohesive soils, some lateral displacement, compaction, or localized improvement of the soil can occur around the bond zone, although the improvement is generally less than for cohesionless soils.

Pressure grouting also appears to cause a recompaction or redensification of the soil around the borehole and increases the effective diameter of the pile in the bond zone. These mechanisms effectively enhance grout/soil contact, leading to higher skin friction values and improved load/displacement performance. Such pressure grouting may also mechanically improve the soil between piles.

#### 4.3.4.3 Postgrouting (Type C and D Micropiles)

It may not be possible to exert sufficiently high grout pressures during the casing removal stage due to potential ground hydrofracture or leakage around the casing. In addition, some micropile construction methods may not use or need a temporary drill casing, and so pressure grouting of the Type B method is not feasible. These circumstances have led to the development of post-grouting techniques, whereby additional grout can be injected via special grout tubes some time after the placing of the primary grout (Figure 4-13). Such grouts are always neat cement-water mixes (for the ease of pumpability through the rubber

valves) and may therefore have higher w/c ratios than the primary grout, being in the range of 0.50 to 0.75 by weight. It is reasoned that excess water from these mixes is expelled by pressure filtration during passage into the soil, and so the actual placed grout has a lower water content (and therefore higher strength).

As described in the following paragraphs, high postgrouting pressures are typically applied, locally, for quite restricted periods; it may only take a few minutes to inject a sleeve. However, higher grout-to-ground bond capacity may, in fact, be more efficiently achieved in Type B micropiles, where grouting pressures are lower but are exerted over a larger area and a much longer period.

Postgrouting techniques Type C and Type D micropiles are described below.

• **Type C:** Neat cement grout is placed in the hole as done for Type A micropiles. Between 15 and 25 minutes later, and before hardening of this primary grout, similar grout is injected once from the head of the hole without a packer, via a 38- to 50-mm (1.5- to 2-in.) diameter preplaced sleeved grout pipe through the reinforcement at a pressure of at least 1 MPa (145 psi) (Figure 4-14).

**Type D:** Neat cement grout is placed in the hole as done for Type A micropiles. When this primary grout has hardened, similar grout is injected via a preplaced sleeved grout pipe. Several phases of such injection are possible at selected horizons and it is typical to record pressures of 2 to 8 MPa (290 to 1,160 psi), especially at the beginning of each sleeve treatment when the surrounding primary grout must be ruptured for the first time. There is usually an interval of at least 24 hours before successive phases. Three or four phases of injection are not uncommon, contributing additional grout volumes of as much as 250 percent of the primary volume.

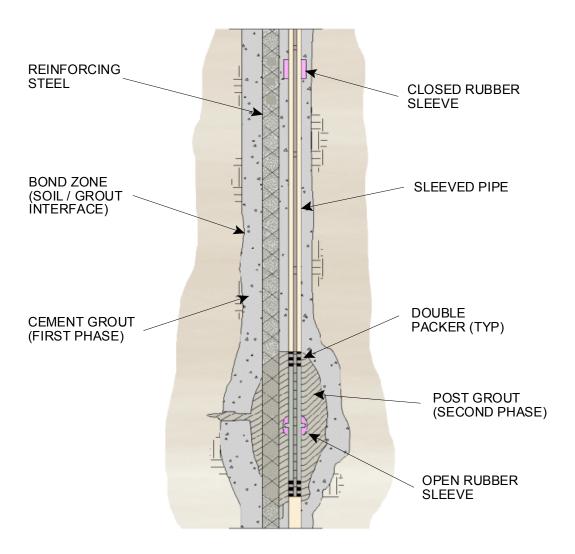


Figure 4-13. Principle of the Tube á Manchette Method of Postgrouting Injection.

The postgrout tube can be a separate 25- or 38-mm (1- or 1.5-in.) diameter sleeved plastic pipe (tube à manchette) placed together with the steel reinforcement (Figure 4-13), or it can be the reinforcement tube itself, suitably sleeved (Figure 4-14). In each of these cases, a double packer may be used to grout through the tubes from the bottom sleeve upwards.

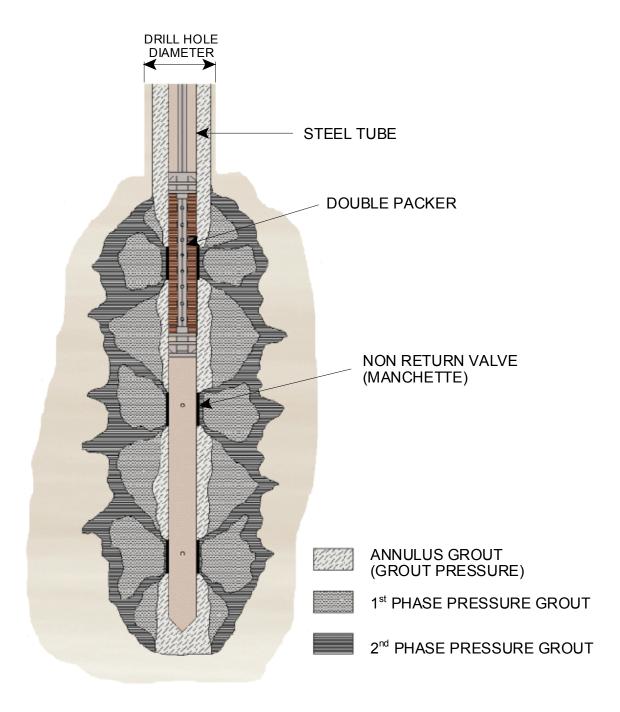


Figure 4-14. Use of Reinforcement Tube as a Tube á Manchette Postgrouting System.

Alternatively, pressure grouting can be conducted from the surface via a circulating-loop arrangement. By this method, grout is pumped around the system and the pressure is increased steadily by closing the pressurization value on the outlet side. At the critical "break out" pressure, dictated by the lateral resistance provided by the adjacent grout, the

grout begins to flow out of the tube through one or more sleeves and enters the ground at that horizon. When using the loop method, it is assumed that with each successive phase of injection that a different sleeve opens ultimately resulting in treatment over the entire sleeved length (a feature guaranteed by the tube à manchette method using double packers) (Figure 4-15).

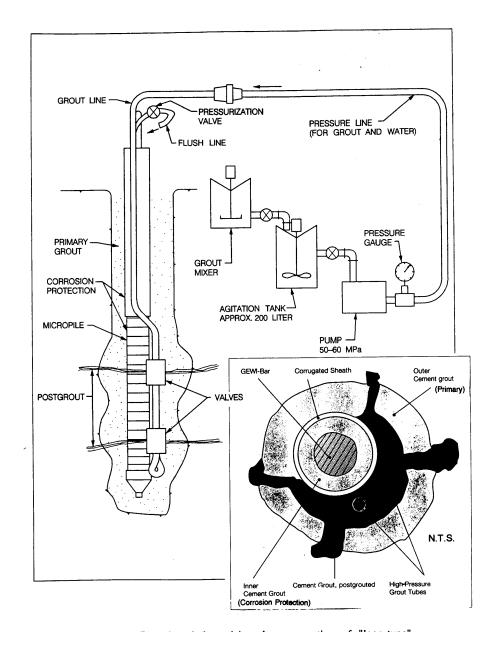


Figure 4-15. Circulating Loop Arrangement for Pressure Grouting (DSI, 1992).

Where micropile structural capacity depends on the compressive strength of the grout, the use of low-strength bentonite primary grouts to reduce "break out" pressures should be avoided.

## 4.3.5 Top-Off (Secondary) Grouting

Due to slow grout seepage, bleed, or shrinkage, it is common to find that the grout level drops slightly prior to stiffening and hardening. In ground anchorage practice, this is simply rectified by topping off the hole with the lowest water-content grout practical, at some later phase. However, in micropile practice where a permanent casing for reinforcement of the upper micropile length is not used, such a cold joint should be avoided since the grout column should be continuous for load holding and corrosion protection reasons. Topping off is therefore best conducted during the stiffening phase to ensure integrity. Where particularly high interfacial bond stresses must be resisted between the micropile and an existing structure, the use of a high-strength non-shrink grout may be considered.

#### 4.4 REINFORCING STEEL

#### 4.4.1 General

The amount of steel reinforcement placed in a micropile is determined by the loading it supports and the stiffness required to limit elastic displacements. Reinforcement may consist of a single reinforcing bar, a group of reinforcing bars, a steel pipe casing or rolled structural steel. In American practice, the use of a single reinforcing bar and/or a high-strength steel casing is commonly used.

#### 4.4.2 Placement of Reinforcement

Reinforcement may be placed either prior to grouting, or placed into the grout-filled borehole before the temporary support (if used) is withdrawn. It must be clean of deleterious substances such as surface soil and mud that may contaminate the grout or coat the reinforcement, impairing bond development. Suitable centralizers should be firmly fixed to maintain the specified grout cover. Pile cages and reinforcement groups, if used, must be sufficiently robust to withstand the installation and grouting process and the rotation and withdrawal of the temporary casing.

## 4.4.3 Reinforcement Types

A description of the various types of reinforcement is provided in this section.

• Concrete Reinforcing Steel Bars (rebar): Standard reinforcing steel (Table 4-2), conforming to ASTM A615/AASHTO M31and ASTM A706, with yield strengths of 420 and 520 MPa (60 and 75 ksi), is typically used. Bar sizes range in diameter from 25 mm to 63 mm (1 to 2.5 in.). A single bar is typically used, but bar groups have been used. For a bar group, the individual bars can be separated by the use of spacers or tied to the helical reinforcement, to provide area for grout to flow between the bars and ensure adequate bonding between the bars and grout (Figure 4-16). Alternatively, bars can be bundled as long as adequate development length for the bundle is provided.

Table 4-2. Dimensions, Yield, and Ultimate Strengths for Standard Reinforcing Bars.

Steel Grade	Rebar Size, mm (in)	Area, mm ² (in. ² )	Yield Strength, kN (kip)
	19 (#6)	284 (0.44)	117 (26)
Grade 420 ⁽¹⁾	22 (#7)	387 (0.60)	160 (36)
	25 (#8)	510 (0.79)	211 (47)
Grade 520 ⁽²⁾	19 (#6)	284 (0.44)	147 (33)
	22 (#7)	387 (0.60)	200 (45)
	25 (#8)	510 (0.79)	264 (59)
	29 (#9)	645 (1.0)	334 (75
	32 (#10)	819 (1.27)	424 (95)
	36 (#11)	1006 (1.56)	520 (117)
	43 (#14)	1452 (2.25)	751 (169)
	57 (#18)	2581 (4.0)	1335 (3000)
Grade 550 ⁽³⁾	63 (2.5 in)	3168 (4.91)	1747 (393)

Notes: (1)Grade 420 steel has yield stress of  $f_y$ = 420 MPa (60 ksi) and tensile strength of  $f_u$  = 620 MPa (92 ksi)

 $^{^{(2)}}$ Grade 520 steel has yield stress of  $f_y$ = 520 MPa (75 ksi) and tensile strength of  $f_u$  = 690 MPa (102 ksi)

 $^{^{(3)}}$ Grade 550 steel has yield stress of  $f_y$  = 550 MPa (80 ksi) and tensile strength of  $f_u$  = 700 MPa (104 ksi)

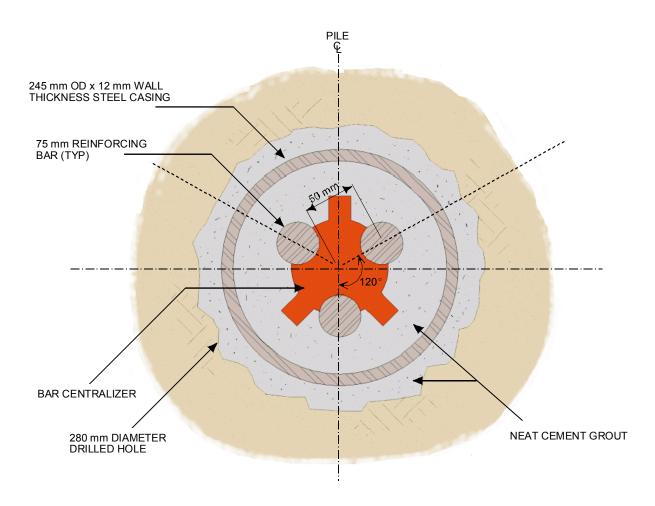


Figure 4-16. Multiple Bar Reinforcement with Bar Centralizer/Spacer.

For low overhead conditions where placement of full-length bars is not feasible, mechanical couplers can be used. Field adjustment of individual bar lengths can be difficult if the coupler type requires shop fabrication.

• Continuous-Thread Steel Bars: Steel reinforcing bars may be fabricated with a continuous full-length thread, such as the Dywidag Systems International (DSI) Threadbar or the Williams All-Thread Bar.

The DSI Threadbar system, which is also referred to as a GEWI Threadbar (Figure 4-17 and Table 4-3), is a common choice throughout the world for micropile reinforcement. The bar has a coarse pitch, continuous ribbed thread rolled on during production. It is available in diameters ranging from 19 mm to 63 mm (3/4 to 2-1/2 in.) in steel conforming to ASTM A615/AASHTO M 31, with yield strengths of 420,

520, and 550 MPa (60, 75, and 80 ksi). The size range of 32 mm to 63 mm (1-1/4 to 2-1/2 in.) is most commonly used. Higher strength bars of steel conforming to ASTM A722/AASHTO M 275 with an ultimate strength of 1,035 MPa (150 ksi) are also available, in diameters of 26, 32, and 36 mm (1, 1-1/8, and 1-3/8 in.).

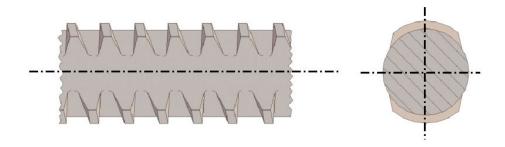


Figure 4-17. Details of DSI Threadbar (DSI, 1993).

Table 4-3. Dimensions and Yield Strength for DSI Threadbar.

Steel Grade	Bar Diameter mm (in)	Area mm² (in²)	Yield Strength kN (kip)	Diameter over Threads mm (in.)	Bar Weight kg/m (lbs/lf)
520 ⁽¹⁾	32 (#10)	819 (1.27)	424 (95)	36.3 (1.43)	6.41 (4.30)
	36 (#11)	1006 (1.56)	520 (117)	40.9 (1.61)	7.91 (5.31)
	43 (#14)	1452 (2.25)	751 (169)	47.2 (1.86)	11.39 (7.65)
	57 (#18)	2581 (4.0)	1335 (300)	63.5 (2.5)	20.24 (13.6)
550 ⁽²⁾	63 (2.5in)	3168 (4.91)	1747 (393)	69.1 (2.72)	24.86 (16.7)

Notes: (1)Grade 500 steel has yield stress of  $f_y$ = 520 MPa (75 ksi) and tensile strength of  $f_u$  = 690 MPa (100 ksi).

The Williams All-Thread Bar is available in diameters ranging from 20 to 89 mm (0.8 to 3.5 in.) in steel conforming to ASTM A615/AASHTO M 31 and from 26 to 65 mm (1 to 2.5 in.) in steel conforming to ASTM A722/AASHTO M 275, with an ultimate strength of 1,035 MPa (150 ksi). The bar has a finer thread than used on the Dywidag bar.

The thread on the bars not only ensures grout-to-steel bond, but also allows the bar to be cut at any point and joined with a coupler to restore full tension/compression capacity. The continuous thread also simplifies pile-to-structure connections where

⁽²⁾Grade 550 steel has yield stress of  $f_y$ = 552 MPa (80 ksi) and tensile strength of  $f_u$  = 700 MPa (102 ksi).

the bar is connected to an anchor plate. A hex nut is used to connect the plate, with the continuous thread allowing easy adjustment of the plate location.

• Continuous-Thread Hollow-Core Steel Bars: Steel reinforcing bars that have a hollow core and a continuous full-length thread include the Dwyidag, Ischebeck Titan, MAI International, and Chance IBO Injection Boring Rods. Typical sizes of hollow-core steel bars are shown in Table 4-4. It should be noted that additional sizes are available. Hollow-core steel bars offer the advantages of continuous thread, and the hollow core allows the bar to be used to drill the micropile hole. A drill bit is mounted on the tip of the bar, and the bar is drilled in with grout flush pumped to the bit through the hollow core of the bar. Alternately, an air or water flush can be used, with the grout placed through the bar after drilling to the final depth.

The continuous thread allows the bar to be cut to length and coupled, and allows the use of a hex nut for the pile top connection. The main drawback of this type of reinforcement is the higher cost.

• Steel Pipe Casing: With the trend towards micropiles that can support higher loads at low displacements and for the requirement to sustain lateral loads, steel-pipe reinforcement has become more common. Pipe reinforcement can provide significant steel area for support of high loading and contribution to the micropile stiffness, while providing high shear and reasonable bending capacity to resist the lateral loads.

Pipe reinforcement is placed by either using the drill casing as permanent reinforcement, or by placing a smaller diameter permanent pipe inside the drill casing. Use of the drill casing for full-length reinforcement is typical only for micropiles founded in rock, where extraction of the casing for pressure grouting is not necessary. The length of the pipe sections used is dictated by the length of the drill mast and by the available overhead clearance. Casing sections are typically joined by a threaded connection, which is machined into the pipe. The reduced area of the threaded joint should be considered in the structural design of the pile, particularly for the capacity in tension and bending. Methods exist for reinforcement of the threaded joints that can provide a strength equivalent to the full casing section.

Table 4-4. Dimensions and Yield Strength of Common Hollow Injection Bars.

INNER DIAMETER DIAMETER					
	Rod Size Yield kN (kip)	Ultimate Capacity kN (kip)	Diameter		Weight
Rod Size			Inner mm (in.)	Outer mm (in.)	kg/m (lb/ft)
MAI R25N	150 (33.7)	200 (45)	14 (.55)	25 (1.0)	2.6 (1.74)
MAI R32N	230 (51.7)	280 (63)	18.5 (.73)	32 (1.25)	3.4 (2.28)
MAI R38N	400 (90)	500 (112.4)	19 (.75)	38 (1.5)	6.0 (4.0)
MAI R51N	630 (141.6)	800 (179.8)	33 (1.3)	51 (2.0)	8.4 (5.64)
IBO- TITAN 30/16	180 (40.5)	220 (49.5)	16 (.63)	30 (1.18)	2.7 (1.8)
IBO-	244 (54.0)	201 (64.5)	20 (70)	22 (1.26)	2.2 (2.15)
TITAN 32/20	244 (54.9)	291 (64.5)	20 (.79)	32 (1.26)	3.2 (2.15)
IBO- TITAN 40/16	525 (118)	660 (148.4)	16 (.63)	40 (1.57)	7.0 (4.63)
TITAN 73/53	970 (218.1)	1,160 (260.8)	53 (2.09)	73 (2.87)	12.3 (8.3)
TITAN 103/78	1,800 (404.6)	2,282 (513)	78 (3.07)	103 (4.05)	24.9 (16.7)

Pipe in the sizes typically used for micropile construction are available in steel conforming to ASTM A53, A519, A252 and A106 with typical yield strengths of 241 MPa (36 ksi). Availability of the desired pipe size may determine the grade of steel used. The main drawback of using these pipe grades is the relatively low yield strength and very high unit cost per linear meter.

American Petroleum Institute (API) 5CT or 5L (N-80) casing may be used. The high yield strength of 552 MPa (80 ksi) greatly aids in the ability of the micropile to support high loads, and improves the strength of threaded joints machined into the

pipe wall. The pipe is also readily available in the form of mill secondary material at a reasonable unit cost. The overwhelming majority of higher capacity micropiles installed to date in the United States have used the N-80 casing. The casing should be specified to meet the tensile requirements of ASTM A252, Grade 3 with a minimum elongation of 15 percent, except the minimum specified yield strength should be consistent with that used for design. A minimum of two representative coupon samples or mill certificates (if available) for each truckload of casing delivered to project should be submitted.

Due to the high strength and typical chemical composition of the API N-80 casing, weldability of the casing sections requires special welding procedures. Welding should be performed in accordance with American Welding Society (AWS) D1.1 "Structural Welding Code – Steel" or alternate methods or materials can be described on an AWS weld procedure form and that method should be approved by a welding specialist. Prior to welding the N-80 casing, welding procedures must be submitted to the owner for approval. Special welding procedures are not required for minor welds which do not carry structural loads.

Pipe dimensions and yield strengths, for various grades of steel, are presented in Table 4-5.

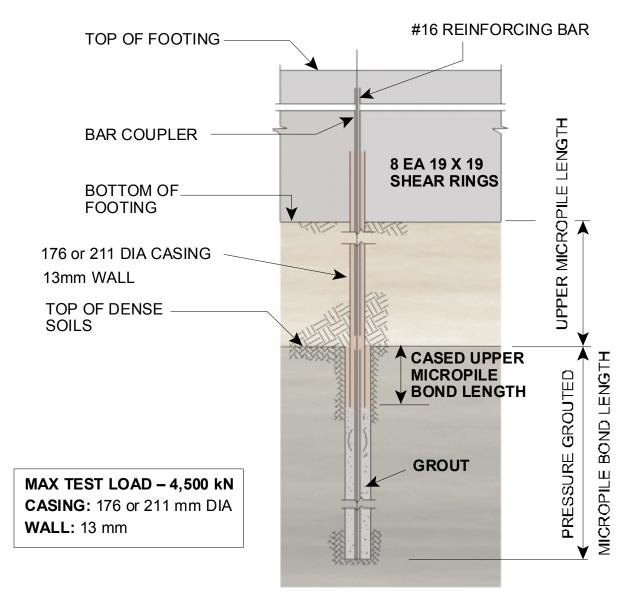
• Composite Reinforcement: For micropiles with partial length permanent drill casing (Type 1C, 2C and 4C), the use of a steel bar for reinforcement of the bottom portion of the pile is common, resulting in a composite reinforced pile (example shown in Figure 4-18). The reinforcing bar may be extended to the top of the micropile for support of tension loading. The use of varying reinforcement adds complexity to the pile structural analysis, with particular attention needed for the location and capacity of reinforcement transition.

Table 4-5. Dimensions and Yield Strength of Common Micropile Pipe Types and Sizes.

API N-80 Pipe – Common Sizes					
Casing OD Wall ⁽¹⁾ , mm (in.)	139.7 (5.500)	139.7 (5.500)	177.8 (7.000)	177.8 (7)	244.5 (9.625)
Wall Thickness ⁽¹⁾ , mm (in.)	9.17 (0.361)	10.5 (0.415)	12.6 (0.498)	18.5 (0.73)	12.0 (0.472)
Area ⁽²⁾ , mm ² (in. ² )	3760 (5.83)	4280 (6.63)	6560 (10.2)	9280 (14.4)	8760 (13.6)
Yield Strength ⁽³⁾ , kN (kip)	2,070 (466)	2,360 (530)	3,620 (814)	5,120 (1,151)	4,830 (1,086)
ASTM A519, A106 Pipe – Common Sizes ⁽⁵⁾					
Casing OD Wall ⁽¹⁾ , mm (in.)	139.7 (5.50)	168.3 (6.625)	203.2 (8.00)	273.1 (10.75)	-
Wall Thickness ⁽¹⁾ , mm (in.)	12.7 (0.50)	12.7 (0.50)	12.7 (0.50)	16 (0.625)	-
Area ⁽²⁾ , mm ² (in. ² )	5,067 (7.85)	6,208 (9.62)	7,600 (11.8)	12,850 (19.9)	-
Yield Strength ⁽³⁾ , kN (kip)	1,270 (286)	1,540 (346)	1,890 (425)	3,190 (717)	-

Notes:  $^{(1)}$ Casing outside diameter (OD) and wall thickness (t) are nominal dimensions.  $^{(2)}$ Steel area is calculated as  $A_s = (\pi/4) \times (OD^2 - ID^2)$ .  $^{(3)}$ Nominal yield stress for API N-80 steel is  $F_y = 552$  MPa (80 ksi).  $^{(4)}$ Nominal yield stress for ASTM A519 & A106 steel is  $F_y = 241$  MPa (36 ksi).  $^{(5)}$ 

⁽⁵⁾Other pipe sizes are manufactured but may not be readily available. Check for availability through suppliers.



**NOTE: ALL DIMENSIONS IN MILLIMETERS** 

Note: 1 mm = 0.040 in and 1 kN = 0.224 kips

Figure 4-18. Details of Example Composite High-Capacity Type 1B Micropiles.

#### 4.5 REFERENCES

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# CHAPTER 5 DESIGN OF MICROPILES FOR STRUCTURE FOUNDATIONS

#### 5.1 INTRODUCTION

A typical micropile cross section used for structural foundation support is shown on Figure 5-1. This micropile consists of an upper length reinforced with a permanent steel casing with a center steel reinforcing bar and a lower grouted bond length reinforced with the center reinforcing bar.

The geotechnical load capacity of a micropile is sensitive to the process used during micropile construction, especially the techniques used for drilling the micropile shaft, flushing the drill cuttings, and grouting the micropile. Therefore, verification of the shaft resistance developed at the grout – ground interface assumed in design via micropile load testing is essential to confirm structure safety; load testing should therefore be considered a part of the design.

The basic philosophy of micropile design differs little from that for a drilled shaft. The system must be capable of sustaining the anticipated loading conditions with the micropile components operating at safe stress levels, and with resulting displacements being within tolerable (or allowable) limits. For conventional drilled shafts, where the large cross sectional area results in high structural capacity and stiffness, the design is normally governed by the geotechnical load capacity, i.e., side and base resistance. Because micropiles have a relatively small cross sectional area, the design is usually controlled by structural considerations. Moreover, the high grout to ground capacities that can be developed using pressure grouting techniques will typically result in high geotechnical load capacities.

The purpose of this chapter is to present a step-by-step generalized method for the design of micropiles used for structural foundations. The major steps and substeps in this design method are outlined in Table 5-1. Detailed information for each of these steps is presented in this chapter and a complete design is shown in Sample Problem No. 1.

Table 5-1. Design Steps for Micropiles used for Structural Foundations.

- 1. Identify project requirements and evaluate micropile feasibility
- 2. Review available information and perform subsurface exploration and laboratory testing program
- 3. Develop all loading combinations
- 4. Preliminary design of micropiles
  - spacing
  - length
  - cross section
- 5. Evaluate allowable structural capacity of cased length
- 6. Evaluate allowable structural capacity of uncased length
- 7. Compare design loads to structural capacity from Steps 5 and 6 and modify structural section, if necessary
- 8. Evaluate geotechnical capacity of micropile
  - evaluate suitable ground stratum for bond zone
  - select bond stress and calculate bond length required to resist design load
  - evaluate micropile group capacity for compression and tension (i.e., uplift)
- 9. Estimate micropile group settlement
- 10. Design micropile to footing connection at pile cap
- 11. Develop load testing program
- 12. Prepare Drawings and Specifications

## **Other Design Considerations**

- 1. Corrosion Protection**
- 2. Plunge Length
- 3. End Bearing Micropiles
- 4. Downdrag
- 5. Lateral Loads on Single Vertical Micropiles
- 6. Lateral Loads on Micropile Groups
- 7. Buckling
- 8. Seismic

^{**} Corrosion protection is a critical component of all micropile designs.

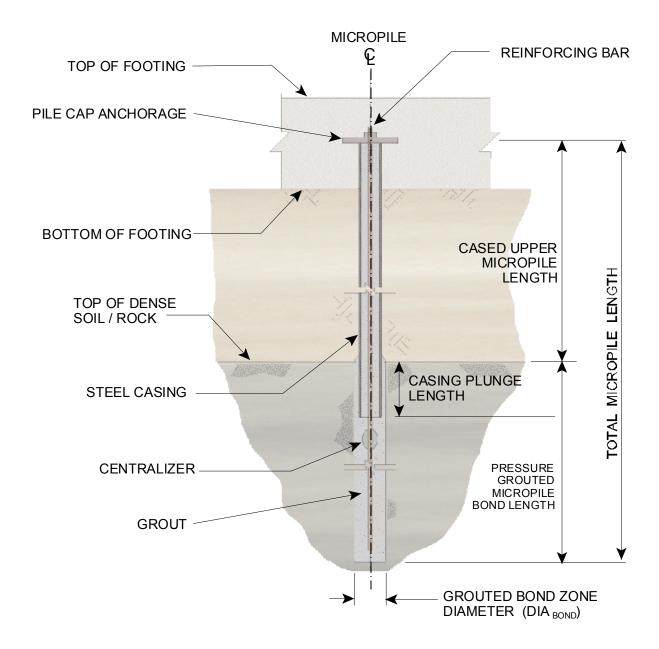


Figure 5-1. Detail of a Composite Reinforced Micropile.

## 5.2 STEP 1: EVALUATE PROJECT REQUIREMENTS AND MICROPILE FEASIBILITY

It is essential to systematically consider various foundation types and to select the optimum alternative based on the superstructure requirements, the subsurface conditions, and foundation cost. Foundation types may include shallow foundations consisting of spread

footing or mat foundations with or without ground improvement; or deep foundations consisting of driven piles, drilled shafts, or micropiles.

The feasibility of using spread footings for foundation support should be considered in any foundation selection process. Spread footings are generally more economical than deep foundations; spread footings in conjunction with ground improvement techniques should also be considered. Deep foundations should not be used indiscriminately for all subsurface conditions and for all structures. Feasibility evaluations considering shallow foundations, driven piles, and drilled shafts is provided in FHWA NHI-05-042 (2005).

Where deep foundations have been judged to be the most appropriate foundation alternative (as compared to shallow foundations), micropiles should be compared to driven piles and drilled shafts. On some projects, construction of driven piles and/or drilled shafts may be feasible though subsurface conditions or other project constraints will increase cost. Cost effectiveness of micropiles should be investigated for such projects. Bidding of alternative foundation systems may provide the most cost-effective option.

In assessing micropile feasibility for a specific project, micropiles will most often be compared to drilled shafts and/or driven piles. In many cases, either driven piles or drilled shafts will be more cost-effective than micropiles, therefore the cost-effective use of micropiles will be limited to projects with specific technical constraints that make the construction of drilled shafts or driven piles difficult to impossible. In general, micropiles may be cost-effective at project locations where:

- subsurface conditions would make the installation of driven piles or drilled shafts difficult (and expensive) such as ground containing significant amounts of boulders, cobbles, or other large debris;
- difficult access or limited overhead clearance is available for constructing deep foundations (e.g., working inside existing structures or underneath bridge decks);
- subsurface voids may exist (e.g., potentially collapsible ground, karstic formations, underground mines, etc.);
- vibration limits would preclude the use of conventional deep foundation installation equipment; or
- underpinning or retrofitting of existing foundations requires strict control of vibrations or settlements.

It is noted, however, that micropile capacities continue to increase as additional experience with this technology is obtained. Currently, micropiles in rock have been tested to ultimate loads as high as 4,500 kN (1,000 kips). For high capacity micropiles, the cost per unit of

capacity may be comparable to that for driven piles. A process to evaluate micropile project costs is described in Chapter 10. The user of this manual is also specifically referred to FHWA NHI-05-042 (2005) for information on developing cost per unit capacity for driven piles.

## 5.3 STEP 2: REVIEW AVAILABLE INFORMATION AND GEOTECHNICAL DATA

The subsurface exploration, laboratory testing, and evaluation of geotechnical design parameters for the design of micropiles used for structural foundation support is similar to that for either driven piles (see FHWA NHI-05-042 (2005) or drilled shafts (see FHWA-HI-99-025, 1999). Specific elements that should precede the actual exploration program include a search and review of published and unpublished information at and near the site, a visual site inspection, and design of the subsurface exploration program. For guidance regarding the planning and conduct of subsurface exploration programs, refer to AASHTO Manual on Subsurface Investigations (1988), FHWA NHI-01-031 Manual on Subsurface Investigations (2001), and Geotechnical Engineering Circular 5 (GEC 5), Evaluation of Soil and Rock Properties (2002).

As a minimum, the information gathering and subsurface exploration and laboratory testing program should obtain information to analyze foundation stability and settlement with respect to:

- regional and local geology;
- discussion of site history which may include information on mining, previous excavations, problems with previous construction, construction methods used for adjacent utilities or basements or foundations, possible occurrence of potentially contaminated materials, etc.;
- logs of soil borings that includes description and classification of the soil strata encountered, unit weights, moisture contents, standard penetration tests (SPT) or cone penetrometer test (CPT) values, and description of groundwater conditions;
- if rock is encountered, logs with rock classifications, penetration rates, degree of weathering and fracturing, recovery and RQD measurements, and driller's observations should be provided;
- laboratory testing results including Atterberg limits information (for silty or clayey soils) and grain size analyses;
- a subsurface soil profile along the alignment of the structure developed from the soil boring information presenting soil type, ground water elevations, and SPT values as a minimum;

- estimated soil and/or rock shear strength and compressibility parameters;
- determination and discussion of the presence of hazardous, contaminated, and/or corrosive conditions, if applicable; indicators of corrosive conditions include low soil resistivity, the presence of lead, sulfates, and chlorides, and observations of corrosion of existing site features; and
- project-specific considerations including, for example, liquefiable soil layers, expansive or dispersive soil deposits, underground voids from solution weathering or mining activity, etc.

Some minimum guidelines for boring spacing and depth are provided in Table 5-2. This table should be used only as a first step in estimating the number of borings for a particular design, as actual boring spacing and depth will depend upon the project type, geologic environment, and variability encountered during the field investigation.

Table 5-2. Guidelines for Minimum Number of Investigation Points and Depth of Investigation (Modified after FHWA-IF-02-034, 2002).

Application	Minimum Number of Investigation Points and	Minimum Depth of Investigation
Application  Deep Foundations (Micropiles for Structural Support)	Investigation Points and Location of Investigation Points  For substructure (e.g., bridge piers or abutments) widths less than or equal to 30 m (100 ft), a minimum of one investigation point per substructure. For substructure widths greater than 30 m (100 ft), a minimum of two investigation points per substructure. Additional investigation points should be provided if erratic subsurface conditions are encountered.	In soil, depth of investigation should extend below the anticipated micropile tip elevation a minimum of 6 m (20 ft), or a minimum of two times the maximum micropile group dimension, whichever is deeper. All borings should extend through unsuitable strata such as unconsolidated fill, peat, highly organic materials, soft fine-grained soils, and loose coarse-grained soils to reach hard or dense materials.  For micropiles bearing on rock, a minimum of 3 m (10 ft) of rock core shall be obtained at each investigation point location to verify that the boring has not terminated on a boulder.  For micropiles supported on or extending into rock, a minimum of 3 m (10 ft) of rock core, or a length of rock core equal to at least three times the micropile diameter for isolated micropiles or two times the maximum micropile group dimension, whichever is greater, shall be extended below the anticipated micropile tip elevation to determine the physical characteristics of rock within the zone of foundation
Structural	minimum of one investigation point per substructure. For substructure widths greater than 30 m (100 ft), a minimum of two investigation points per substructure. Additional investigation points should be provided if erratic subsurface	dimension, whichever is deeper. All borings should extend through unsuitable strata such as unconsolidated fill, peat, highly organic materials, soft fine-grained soils, and loose coarse-grained soils to reach hard or dense materials.  For micropiles bearing on rock, a minimum of 3 m (10 ft) of rock core shall be obtained at each investigation point location to verify that the boring has not terminated on a boulder.  For micropiles supported on or extending into rock, a minimum of 3 m (10 ft) of rock core, or a length of rock core equal to at least three times the micropile diameter for isolated micropiles or two times the maximum micropile group dimension, whichever is greater, shall be extended below the anticipated micropile tip elevation to determine the physical

In areas underlain by heterogeneous soil deposits and/or rock formations, it will likely be necessary to exceed the minimum guidelines provided in Table 5-2 to evaluate variations in soil and/or rock types and to assess consistency across the site area. For situations where micropiles will be installed in karstic formations, it may be necessary to advance a boring at the location of each micropile. Where battered micropiles may be used, the location of the micropile bond length will be offset from the footing location. Borings should be located so that information on bond zone soils is obtained.

In general, all geotechnical data interpretations should be provided. The basic character and extent of the soil strata determined from the geotechnical investigation can be verified during pile installation by monitoring and logging of the penetration rates, drilling action, flush return, and soil cuttings.

#### 5.4 STEP 3: DEVELOP APPLICABLE LOADING COMBINATIONS

For state DOT projects, reference will typically be made to AASHTO Standard Specification for Highway Bridges (when using allowable stress design (ASD) or load factor design (LFD)) or to AASHTO LRFD Bridge Design Specifications (when using load and resistance factor design) for loadings, load combinations, and load terminology. Under any of these design approaches, various individual loads will be added together to develop a series of load combinations to be checked as part of the design. The required loads for consideration in design (e.g., maximum compression load, maximum tension load, and maximum transverse and longitudinal overturning moments) will usually be provided by the structural engineer as part of a design criteria package. Other loading cases that may be considered include lateral loads, seismic loads, and loads due to downdrag.

For most applications, it is sufficiently accurate to assume that the foundation cap is perfectly rigid, i.e., the cap is free to rotate about all axes but will not bend. With this, the so-called "rigid cap" method can be used to distribute axial forces resulting from overturning moments to individual foundation elements. However, for large pile groups, relatively thin pile caps, and/or widely spaced foundation elements, a more sophisticated soil-structure interaction analysis may be required. Moreover, since micropiles are often used with pre-existing foundation elements, the potential differences in the stiffness of the elements may require that such sophisticated analyses be used. Additional discussion on available soil-structure interaction analysis methods is provided in Section 5.19.3.

#### 5.5 STEP 4: PRELIMINARY DESIGN OF MICROPILES

## 5.5.1 <u>Selection of Micropile Spacing</u>

In all cases, the center-to-center spacing between individual micropiles should be at least 760 mm (30 in.) or 3 micropile diameters, whichever is greater. This spacing criterion was originally developed for driven piles and it allows for potential deviations in drilling over significant depths and reduces group effects between adjacent micropiles

The spacing of micropiles for structural foundation support will also depend on the specific application. For example, the spacing of micropiles used to improve (or retrofit) an existing foundation (or footing) will be based on the condition of the existing footing, access to the existing footing, and the magnitude of the loads that need to be resisted by the micropiles. Where relatively small design loads are involved (e.g. less than 450 kN (100 kips)), it may be feasible to drill and install micropiles through the existing foundation and still develop sufficient load transfer between the micropiles and the existing foundation to provide adequate capacity. Where larger loads are required or where the existing foundation has deteriorated, a new footing may need to be constructed around the existing footing and positively connected to the existing footing using steel dowels or other devices to provide the required capacity.

Micropile spacing and layout can either be selected by the Owner and included in the Plans or the Specifications may allow for the Contractor to select the number of micropiles and layout. The latter provides the Contractor with the flexibility to consider whether fewer higher capacity micropiles may be used as compared to a baseline configuration with a greater number of lower capacity micropiles.

#### 5.5.2 Selection of Micropile Length

The total length of an individual micropile will be selected such that the required geotechnical capacity is developed by skin friction (or side resistance) between the grout and the ground over a suitable length in an appropriate stratum. The evaluation of this suitable length is described in Section 5.9.

The total length will also be controlled by required penetration depths to resist downdrag and uplift forces and to provide additional lateral resistance where scour is a consideration or where other sources of lateral load need to be considered in the design.

The maximum length of a micropile that can be achieved using common track-drilling equipment is greater than 90 m (300 ft). Typically, however, micropiles of such lengths

would be very expensive and a practical limit for most projects may be on the order of 30 m (100 ft).

## 5.5.3 <u>Selection of Micropile Cross Section</u>

To carry required axial loads, it is not uncommon for up to one half of the cross sectional area of the micropile to comprise steel casing and/or steel reinforcing rod (s). The use of common casing sizes is preferred to avoid delays associated with material availability. Currently, the most common casing sizes in the U.S. are 141 mm (5-1/2 in.), 178 mm (7 in.), and 245 mm (9-5/8 in.) with a nominal yield stress of 552 MPa (80 ksi), with the 178 mm casing being the most common. These sizes refer to the outside diameter of the casing. Tables 4-2, 4-3, 4-4, and 4-5 provide material properties for common micropile reinforcement.

In general, it is preferable to install fewer higher capacity micropiles as compared to a larger number of lower capacity micropiles to resist a given set of foundation loads. With this approach, less total drilling is required thus reducing overall costs. Also, it is more efficient to resist lateral loads, minimize lateral deflections, and/or achieve relatively high axial load capacities using steel casing as compared to steel reinforcing bars alone. For example, a 178 mm (7-in.) diameter steel casing has about 2.5 times as much steel area as a 2.25-in. diameter reinforcing bar. Therefore, for allowable axial loads greater than approximately 900 kN (200 kips), it is likely that steel casing would be required as compared to a micropile only reinforced with steel reinforcing bars.

The bond between the cement grout and the reinforcing steel bar allows the composite action of the micropile, and is the mechanism for transfer of the pile load from the reinforcing steel to the ground. Typical ultimate bond values range from 1.0 to 1.75 MPa (145 to 254 psi) for smooth bars and pipe, and 2.0 to 3.5 MPa (290 to 508 psi) for deformed bars (ACI 318). Flaky rust on bars lowers the bond strength, but wiping off the loosest rust produces a rougher surface which develops a bond equal to or greater than the unrusted bar. The loose powdery rust appearing on bars after short exposures does not have a significant effect on grout-reinforcing bar bond.

In the majority of cases, grout-to-steel bond does not govern the pile design. In general, the allowable load of a micropile is controlled by the structural strength of the micropile cross section. The procedure to calculate allowable loads in a micropile based on structural considerations is provided as part of Design Step 5 and 6.

## 5.5.4 Selection of Micropile Type

A description of the various micropile types (Type A, B, C, and D) is provided in Chapter 4 of this manual. The selection of the micropile type should be left to the discretion of the Contractor. As part of the request for bid, however, the Owner should require that the Contractor provide information on their proposed methods of drilling and grouting. Based on previous project experience, the Owner may wish to disallow certain drilling techniques based on project-specific constraints. For example, the need to limit surface ground movements for a project involving sandy ground may preclude the use of certain drilling techniques known to increase the potential for soil caving. The Owner should provide specific performance criteria (e.g., movements of structures) as part of the bid package so that the Contractor can select an appropriate industry-accepted drilling and grouting procedure.

#### 5.6 STEP 5: STRUCTURAL DESIGN OF MICROPILE CASED LENGTH

1) Evaluate Allowable Compression Load for Cased Length

The allowable compression load for the cased length of a micropile is given as:

$$P_{c-allowable} = \left[0.4 f_{c-grout}' \times A_{grout} + 0.47 F_{v-steel} \left(A_{bar} + A_{ca \sin g}\right)\right]$$
(Eq. 5-1)

where

 $P_{c-allowable}$  = allowable compression load;

 $f_c$  = unconfined compressive strength of grout (typically a 28-day strength);

A_{grout} = area of grout in micropile cross section (inside casing only, discount grout outside the casing);

 $F_{v-steel}$  = yield stress of steel;

A_{bar} = cross sectional area of steel reinforcing bar (if used); and

 $A_{casing} = cross sectional area of steel casing.$ 

## Strain Compatibility between Grout, Casing, and Reinforcing Rod

Strain compatibility under compression loads is considered for the steel components and grout by limiting allowable compressive stresses to the minimum allowable for any individual component (i.e., steel casing, steel reinforcement, or grout). Therefore, the maximum yield stress of steel to be used in Eq. 5-1 is the minimum of: (1) yield stress of casing; (2) yield stress of steel reinforcing rod; and (3) maximum stress based on considerations of grout failure. Additional explanation for the maximum stress based on grout failure is provided below.

According to Section 8.16.2.3 of AASHTO (2002), "the maximum usable strain at the extreme concrete compression fiber is equal to 0.003". Therefore, if the grout is limited to a compression strain of 0.003, the steel components must also be limited to this value. The stress in the steel at this strain level is equal to the Young's modulus of steel, E, multiplied by strain (i.e., 0.003). For a typical E for steel of 200,000 MPa (29,000 ksi), the allowable steel yield stress is then 200,000 MPa  $\times$  0.003 = 600 MPa (87 ksi). Therefore, the maximum stress based on considerations of grout failure is 600 MPa (87 ksi).

For example, for a micropile with a casing yield strength of 241 MPa (36 ksi), a reinforcing rod yield strength of 520 MPa (75 ksi), and a grout failure controlled maximum stress of 600 MPa (87 ksi), a value of 241 MPa (36 ksi) would be used for the term  $F_{v\text{-steel}}$  in Eq. 5-1.

An example of the evaluation of  $P_{c-allowable}$  is described for the micropile shown in Figure 5-2.

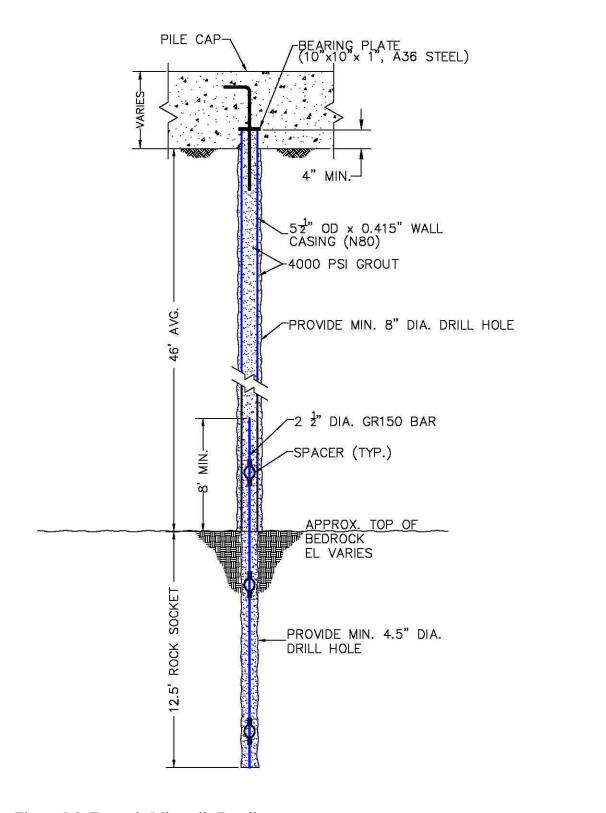


Figure 5-2 Example Micropile Detail.

$$\begin{split} P_{c-allowable} &= \left[ 0.4 \, f_{c-grout}^{'} \times A_{grout} + 0.47 \, F_{y-ca \sin g} \, A_{ca \sin g} \, \right] \\ A_{ca \sin g} &= \frac{\pi}{4} (OD^2 - ID^2) \\ ID &= OD - 2 \, t_w = 5.5 \, in. - 2 \, (0.415 \, in.) = 4.67 \, in \\ A_{ca \sin g} &= \frac{\pi}{4} (5.5 \, in.^2 - 4.67 \, in.^2) = 6.63 \, in.^2 \\ A_{grout} &= \frac{\pi}{4} (D_{drillhole})^2 - A_{ca \sin g} = \frac{\pi}{4} (5.5 \, in.)^2 - 6.63 \, in.^2 = 17.13 \, in.^2 \\ F_{y-ca \sin g} &= \min \left( F_{y-ca \sin g}, grout \, crushing \, strength \right) \\ F_{y-ca \sin g} &= \min \left( 80 \, ksi, 87 \, ksi \right) = 80 \, ksi \\ \therefore P_{c-allowable} &= 0.4 \, (4 \, ksi) \, (17.13 \, in.^2) + 0.47 \, (80 \, ksi) \, (6.63 \, in.^2) = 276 \, kips \end{split}$$

## Effect of Coupled Sections on Compression Capacity

As previously discussed in Chapter 3, steel reinforcing bars and casing are installed in coupled sections. For installation of micropiles in very low overhead clearance conditions, the length of individual casing sections may be 1 meter or shorter. Reinforcing bar couplers can typically provide a minimum axial capacity of 125 percent of the intact reinforcing bar yield strength, therefore the strength properties of an intact reinforcing bar can be used.

A common method for coupling individual casing lengths for micropiles is to machine a thread into the wall of the casing at the section ends. If the joint is properly designed and if the casing is filled with grout (as is commonly done), the joint can provide compressive capacity approximately equivalent to the strength of the full intact casing section. The grout provides support, preventing the male half of the joint from deforming inward.

From a practical standpoint, the strength of coupled sections of reinforcing bars and/or casing sections is confirmed via proof testing and verification testing.

#### Allowance for Corrosion

For evaluation of the allowable compression capacity of the cased length, the outside diameter of the steel casing is reduced to account for assumed losses in section resulting from corrosion over the design life. The specific losses depend on the agressivity of the ground in which the micropile is constructed. It is noted here, that the cross sectional area of the reinforcing bar is not reduced (for purposes of

calculating allowable compression capacity). Typical reinforcement coatings (e.g., epoxy-coating) and minimum specified grout cover thickness are selected to provide sufficient protection against corrosion.

Detailed information on corrosion protection for micropiles including recommended losses due to corrosion for micropiles loaded in compression is provided in Section 5.14.

## Buckling of Cased Length of Micropile

In some cases, the cased length of the micropile may be formed within, for example, very weak ground or in a karstic zone. In such cases, the allowable compression load calculated above may need to be reduced to account for bucking over this length of the micropile. Section 5.20 provides information on project conditions which may require that buckling be considered and structural calculations for evaluating the allowable compression load of the cased length accounting for micropile buckling.

## 2) Evaluate Allowable Tension Load for Cased Length

For projects in which the micropiles will be subject to tensile loads, the allowable tension load  $P_{t-allowable}$  for the cased length of a micropile can be calculated as:

$$P_{t-allowable} = 0.55 F_{y-steel} \times \left( A_{bar} + A_{ca \sin g} \right)$$
 (Eq. 5-2)

where F_{v-steel} is the minimum yield stress of the bar and casing.

#### Allowance for Corrosion

For aggressive ground conditions (as defined in Section 5.14), it may be conservatively assumed that the steel casing is not effective in carrying tensile loads, i.e., assume  $A_{casing} = 0$  in Eq. 5-2. In this case, the central reinforcing steel should be designed to carry the entire tension design load. Detailed information on corrosion protection for micropiles loaded in tension is provided in Section 5.14.

## Effect of Coupled Sections on Tensile Capacity

Unlike compressive stresses, tension stresses have a greater impact on the integrity of the casing at the joint location primarily because of the reduced thickness of the casing over the length of the threaded area. Currently, no specific testing standard exists for evaluating the tension capacity of a threaded casing joint appropriate for micropile applications.

If tension loads greater than 25 percent of the allowable tension load on the intact casing are proposed to be resisted by a casing with flush joint threaded connections, the Owner should require the contractor to provide data demonstrating the adequacy of the proposed joint detail. Since a common testing method does not exist, testing procedures and test data will need to be reviewed by a qualified engineer. As projects involving micropiles subject to relatively large tensile forces become more commonplace, a means to evaluate allowable tensile stresses for threaded joints will become necessary, especially since many casing providers in the U.S. have a slightly different proprietary threading detail.

## 3) Evaluate Combined Axial Compression and Bending of Cased Length

The application of lateral loads or overturning moments (from the superstructure) at the ground surface create bending stresses in the micropile. These bending stresses cause additional compressive stresses (above those from vertical compression loads alone) in the micropile. Allowable stresses in the cased length of the micropile are evaluated using a combined stress evaluation.

As for other deep foundation elements subject to lateral loads and/or overturning moments, the bending moments in the pile can be evaluated using a laterally loaded pile analysis program such as LPILE (Reese et al., 2005). With these analyses, the maximum bending moment in the pile,  $M_{max}$ , is calculated and used in the combined stress evaluation.

The details of performing laterally loaded micropile analyses are provided in Section 5.18. Herein, it is assumed that  $M_{max}$  has been evaluated and the structural capacity of the cased length can be evaluated.

The combined stress evaluation is based on the method described in Section 10.36 of AASHTO (2002) for structural steel sections. The design check for combined stresses (appropriate for micropiles) is

$$\frac{f_a}{F_a} + \frac{f_b}{\left(1 - \frac{f_a}{F_e'}\right)} \le 1.0$$
 (Eq. 5-3)

where

- $f_a$  is the axial stress =  $P_c/A_{casing}$ ;
- $f_b$  is the bending stress =  $M_{max}/S$  where S is the elastic section modulus of the steel casing;
- F_a is the allowable axial stress that would be permitted if axial force alone existed = 0.47 F_{y-casing} (see AASHTO Table 10.32.1.A);
- $F_b$  = is the allowable bending stress that would be permitted if bending moment alone existed = 0.55  $F_{y\text{-casing}}$  (see AASHTO Table 10.32.1.A); and
- F'_e is the Euler buckling stress.

The contribution of a central reinforcing bar to bending strength is small compared to that of the casing, hence its effects on bending strength are ignored in Eq. 5-3. In Eq. 5-3, it is conservatively assumed that the maximum axial compression load,  $P_c$ , is carried by the steel casing only and the yield stress of the steel casing is used. Section properties required for the analysis are calculated as:

$$A_{ca \sin g} = \frac{\pi}{4} (OD^2 - ID^2)$$
 (Eq. 5-4a)

$$S = \frac{I_{ca \sin g}}{(OD/2)}$$
 (Eq. 5-4b)

$$I_{ca \sin g} = \frac{\pi}{64} (OD^4 - ID^4)$$
 (Eq. 5-4c)

The Euler buckling stress is calculated as:

$$F_e' = \frac{\pi^2 E}{FS (Kl/r)^2}$$
 (Eq. 5-5)

where

- E = elastic modulus of the steel casing (typically assumed to be 200,000 MPa (29,000 ksi));
- FS is a factor of safety equal to 2.12;
- K = effective length factor (assumed equal to 1.0);
- L = unsupported length of the micropile; and
- $r = radius of gyration of the steel casing = (I_{casing}/A_{casing})^{1/2}$ .

The effective length factor, K, depends on the rotational restraint at the ends of the micropile and the means available to resist lateral movements. This value is typically assumed equal to 1.0 for micropile designs.

The assumption that the entire axial load is carried by the steel casing is conservative. Richards and Rothbauer (2004) proposed a combined stress check that can account for the contribution of the grout inside the casing to compression capacity. This method assumes that buckling potential is negligible. The Richards and Rothbauer combined stress check can be written as:

$$\frac{P_c}{P_{c-allowable}} + \frac{M_{\text{max}}}{M_{allowable}} \le 1.0$$
 (Eq. 5-6)

where

- P_c = maximum axial compression load;
- P_{c-allowable} is determined from Eq. 5-1;
- $M_{max}$  = maximum bending moment in the micropile; and
- $M_{allowable} = F_b (=0.55 F_{y-casing}) \times S.$

More advanced methods which consider composite action between the steel casing and the grout inside the casing in carrying these axial loads could be used, but are beyond the scope of this manual.

## 5.7 STEP 6: STRUCTURAL DESIGN OF MICROPILE UNCASED LENGTH

The allowable compression load for the uncased length of a micropile is given as:

$$P_{c-allowable} = \left(0.4f_c^{'} \times A_{grout} + 0.47F_{y-bar} \times A_{bar}\right)$$
 (Eq. 5-7)

For the uncased portion of the pile, the reinforcing bar yield stress used in the calculations in compression is assumed to not exceed 600 MPa (87 ksi) (i.e., to prevent grout crushing at an assumed strain of 0.003 unless data is provided demonstrating that the confined grout can sustain higher strain levels without crushing).

The allowable tension load for the uncased length of a micropile is given as:

$$P_{t-allowable} = 0.55 F_{y-bar} \times A_{bar}$$
 (Eq. 5-8)

In Eq. 5-8, the actual yield stress of the bar is used.

It is noted that a combined stress evaluation (see Step 5 Part 3) is not performed for the uncased length since micropiles are designed so that bending stresses are negligible within the uncased portion of the micropile. In other words, the steel casing will be placed to a sufficient depth so that bending moments below that depth are negligible.

# 5.8 STEP 7: REVISE MICROPILE DESIGN

Based on the calculations performed in Steps 5 and 6, the micropile cross section should be modified if the allowable compression or tension load (for either the cased or uncased length) is not sufficient to carry the compression or tension design loads provided as part of Step 3. Possible modifications include using more micropiles, increasing the size of the drill hole, using a larger diameter reinforcing bar, replacing a single reinforcing bar with two bars, and/or increasing the steel area of the casing.

## 5.9 STEP 8. EVALUATE GEOTECHNICAL CAPACITY OF MICROPILE

#### 5.9.1 Establish Stratum for Bond Zone

The maximum compression and tension loads applied at the top of the micropile must be resisted through grout to ground bond over a specific length of the micropile. This length is referred to as the bond zone or bond length. This length can be formed in most soil and rock strata with the major differences being in the grout to ground bond strength that can be developed in a given ground type. The objective for design is to evaluate the length of this bond zone required to resist the applied tension and compression loads with a prescribed factor of safety (discussed subsequently).

As part of this design step, all borings should be reviewed to identify strata appropriate for the micropile bond zone and to identify significant variations in subsurface conditions. Like ground anchors, certain soil deposits are not generally suitable as the location for the micropile bond zone, including (1) organic soils; (2) cohesive soils with an average liquidity index greater than 0.2; (3) cohesive soils with an average plastic index greater than 20. Micropiles installed in these deposits may be

susceptible to excessive creep deformations at testing and working loads. If used, however, for the bond zone, comprehensive testing is recommended and higher factors of safety for geotechnical capacity should be used, as discussed subsequently.

# 5.9.2 Select Ultimate Bond Stress and Calculate Bond Length

The allowable geotechnical bond capacity, P_{G-allowable}, is calculated as:

$$P_{G-allowable} = \frac{\alpha_{bond}}{FS} \times \pi \times D_b \times L_b$$
 (Eq. 5-9)

where:

 $\alpha_{bond}$  = grout to ground ultimate bond strength;

FS = factor of safety applied to the ultimate bond strength;

 $D_b$  = diameter of the drill hole; and

 $L_b = bond length$ 

In most cases, Eq. 5-9 will be used to calculate the estimated bond length to resist the maximum compression load and/or maximum tension (i.e., uplift) load based on load information provided as part of Step 3. To this end, Eq. 5-9 can be rearranged as:

$$L_b = \frac{P_{G-allowable} \times FS}{\alpha_{bond} \times \pi \times D_b}$$
 (Eq. 5-10)

where, for Eq. 5-10,  $P_{G-allowable}$  is equal to the maximum compression or tension load for design.

Table 5-3 provides guidance for estimating the values for grout-to-ground ultimate bond strengths. The table includes ranges for the four methods of grouting (Type A, Type B, Type C, and Type D) in a variety of ground conditions.

For most micropile projects, the contract documents will provide a minimum bond length. This bond length will be based on the evaluation provided in Eq. 5-10. Unless the design engineer has previous experience in similar ground, values no greater than average values (i.e., middle of range reported) for  $\alpha_{bond}$  from Table 5-3 should be used. The design engineer may wish to consider lower bound values where granular materials are loose or for medium to high plasticity cohesive materials. Although the specific type of micropile (i.e., Type A, B, C, or D) will be selected by the Contractor, the design engineer should assume a Type A micropile

will be constructed for microple bond zones in rock and a Type B micropile will be constructed for bond zones in soil.

Ranges of values provided in Table 5-3 and additional information on estimating grout-to-ground bond capacities is available in the following publications:

- "GEC No. 4, Ground Anchors and Anchored Structures", FHWA Report No. FHWA-IF-99-015, (1999).
- "Post-Tensioning Institute (PTI) Recommendations for Prestressed Rock and Soil Anchors", (2004).
- "Construction, Carrying Behavior, and Creep Characteristics of Ground Anchors," H. Ostermayer, Conference on Diaphragm Walls and Anchorages, Institute of Civil Engineers, London, (1975).
- "Ground Control and Improvement" by P.P. Xanthakos, L.W. Abramson, and D.A. Bruce, (1994).
- "Drilled and Grouted Micropiles State-of-the-Practice Review", FHWA Report Nos. RD-96-016/017/018/019; Volumes I IV, (1997).
- "Tiebacks", FHWA Report No. FHWA/RD-82/047, (1982).
- "Permanent Ground Anchors", FHWA Report No. FHWA-DP-68-1R, (1988).

Table 5-3. Summary of Typical  $\alpha_{bond}$  (Grout-to-Ground Bond) Values for Micropile Design.

Soil / Rock Description	Grout-to-Ground Bond Ultimate Strengths, kPa (psi)			
Son' Rock Bescription	Type A	Type B	Type C	Type D
Silt & Clay (some sand) (soft, medium plastic)	35-70 (5-10)	35-95 (5-14)	50-120 (5-17.5)	50-145 (5-21)
Silt & Clay (some sand) (stiff, dense to very dense)	50-120 (5-17.5)	70-190 (10-27.5)	95-190 (14-27.5)	95-190 (14-27.5)
Sand (some silt) (fine, loose-medium dense)	70-145 (10-21)	70-190 (10-27.5)	95-190 (14-27.5)	95- 240 (14-35)
Sand (some silt, gravel) (fine-coarse, medvery dense)	95-215 (14-31)	120-360 (17.5-52)	145-360 (21-52)	145-385 (21-56)
Gravel (some sand) (medium-very dense)	95-265 (14-38.5)	120-360 (17.5-52)	145-360 (21-52)	145-385 (21-56)
Glacial Till (silt, sand, gravel) (medium-very dense, cemented)	95-190 (14-27.5)	95-310 (14-45)	120-310 (17.5-45)	120-335 (17.5-48.5)
Soft Shales (fresh-moderate fracturing, little to no weathering)	205-550 (30-80)	N/A	N/A	N/A
Slates and Hard Shales (fresh- moderate fracturing, little to no weathering)	515-1,380 (75-200)	N/A	N/A	N/A
<b>Limestone</b> (fresh-moderate fracturing, little to no weathering)	1,035-2,070 (150-300)	N/A	N/A	N/A
Sandstone (fresh-moderate fracturing, little to no weathering)	520-1,725 (75.5-250)	N/A	N/A	N/A
Granite and Basalt (fresh- moderate fracturing, little to no weathering)	1,380-4,200 (200-609)	N/A	N/A	N/A

Type A: Gravity grout only

Type B: Pressure grouted through the casing during casing withdrawal

Type C: Primary grout placed under gravity head, then one phase of secondary "global" pressure grouting

Type D: Primary grout placed under gravity head, then one or more phases of secondary "global" pressure grouting

For all highway projects, some amount of site-specific load testing of micropiles must be performed and the scope of this load testing is used to define the factor of safety applied to the ultimate bond strength for design. Herein, a factor of safety of 2.0 is recommended provided the following load testing is performed:

- At least one ultimate or verification test is conducted prior to beginning
  production micropile installation, and then one or more additional ultimate
  or verification tests must be conducted in each significantly different
  ground type encountered as construction proceeds. A larger number of
  ultimate, or verification, tests may be specified for larger projects.
- During installation of production micropiles, proof testing must be conducted on a specified number of the total production piles installed. In general, proof tests may be performed on 5 percent of production micropiles. Specific proof testing requirements are discussed in Chapter 7.

For projects in which the micropile bond zone is formed in potentially creeping soils, high plasticity soils, weak rock, or any other ground type considered to be marginal or for which previous experience in similar ground is limited, a factor of safety value of 2.5 should be used to estimate the bond length and as the basis for the maximum load in an ultimate or verification load test. For micropiles installed in soils susceptible to creep, load testing will include measuring micropile deformations during an extended period of time at one or more test loads. The measured movement is compared to a maximum allowable creep movement (see Chapter 7 for details on sustained load (creep) testing).

# 5.9.3 Evaluate Micropile Group Compression Capacity

Micropile Groups in Cohesive Soils

The efficiency of a micropile group installed in cohesive soils is a function of the center-to-center spacing of the micropiles, s, and contact condition between the bottom of the micropile footing cap and the soil near the ground surface (see Table 5-4).

Table 5-4. Efficiency Factors for Micropile Groups in Cohesive Soils.

Case	Efficiency Factor, η		
If cap is in firm contact with the ground	1.0		
If cap is not in firm contact with the ground	1.0		
and the ground is stiff (i.e., undrained shear			
strength of the soil is greater than 95 kPa (1			
ton per square ft (tsf))			
If the cap is not in firm contact with the			
ground and the ground is relatively soft			
(i.e., undrained shear strength of the soil is			
less than 95 kPa (1 tsf)) or is disturbed			
• $s = 2.5 D_b$	0.65		
$\bullet  S = 3.0 D_b$	0.70		
$\bullet \qquad s = 6.0 \ D_b$	1.0		
• $3.0 D_b < s < 6.0 D_b$	Interpolate between 0.70 and 1.0		

At small micropiles spacings, however, the potential for the micropile group to fail as a "block" should be evaluated. For a micropile group of width  $B_{\rm g}$  and length  $L_{\rm g}$  and depth D (as shown in Figure 5-3), the ultimate capacity of the micropile group,  $Q_{\rm g}$ , is given by:

$$Q_g = (2B_g + 2L_g)D \times \overline{s_u} + B_g L_g \times N_c s_u$$
 (Eq. 5-11)

where  $\overline{s_u}$  is the average undrained shear strength along the depth of penetration of the micropiles and  $s_u$  is the undrained shear strength at the base of the micropile group. For this analysis, it is assumed that the pile cap provides no resistance.

The bearing capacity factor used in Eq. 5-11 is calculated according to the following:

$$N_c = 5 \left( 1 + \frac{0.2 B_g}{L_g} \right) \left( 1 + \frac{0.2 D}{B_g} \right)$$
 for  $\frac{D}{B_g} \le 2.5$  (Eq. 5-12)

$$N_c = 7.5 \left( 1 + \frac{0.2 B_g}{L_g} \right)$$
 for  $\frac{D}{L_g} > 2.5$  (Eq. 5-13)

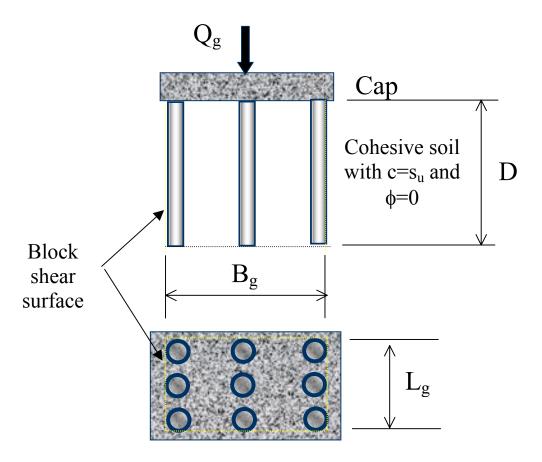


Figure 5-3. Block Failure Model for Micropile Group in Cohesive Soil with Cap in Contact with Ground.

The group capacity to be used for design is evaluated using the following steps:

Step 1: Calculate ultimate group capacity as:

$$Q_{g} = (\alpha_{bond} \times \pi \times D_{b} \times L_{b}) \times no. of micropiles in group \times \eta$$
 (Eq. 5-14)

where n is obtained from Table 5-4.

<u>Step 2:</u> Calculate ultimate group capacity according to Eq. 5-14 and use lower value (i.e., from Step 1 and Step 2) for design.

Step 3: Use a FS value of 2.0 to calculate an allowable group capacity.

Micropile Groups in Cohesionless Soils

As long as the center-to-center spacing of micropiles in a group is greater than three times the diameter of the grouted body (i.e.,  $s > 3D_b$ ), the capacity of a micropile group in cohesionless soils may be calculated as the sum of the resistance of all the individual micropiles in the group, i.e., use Eq. 5-14 with  $\eta$ =1.0. For example, for pressure grouted micropiles installed in cohesionless soils with a typical grouted diameter of 200 mm and typical minimum center-to-center spacing in the range of 750 to 1,000 mm, it is therefore unnecessary to consider a reduction in micropile capacity as a result of group effects.

For the case of micropiles installed in strong soil (which may be cohesionless soil) over weak or compressible soil, an alternate method to evaluate micropile group capacity is used, as described below.

Micropile Groups in Strong Soil Overlying a Weak or Compressible Soil

If a micropile group is embedded in a strong soil deposit overlying a weaker soil deposit, then the potential for a "punching" shear failure of the micropile group into the weaker soil stratum should be considered during design.

The method proposed herein to evaluate the potential for punching shear failure of micropile groups is the same as that which has been developed to address this same issue for drilled shaft groups (see FHWA-IF-99-025, 1999). This approach requires that the capacity of the block of micropiles meet the following condition to assure safety against punching shear failure:

$$\frac{Q_g}{B_g L_g} = q_p \le q_o + \frac{H}{10 B_g} [q_1 - q_o] \le q_1$$
 (Eq. 5-15)

where:

- Q_g, B_g, and L_g are as defined on Figure 5-3;
- q_o is the ultimate unit base resistance at the depth of the top of the lower (i.e., weaker) layer using the shear strength parameters of the lower layer;
- q₁ is the ultimate unit base resistance at the depth of the top of the upper (i.e., stronger) layer using the shear strength parameters of the upper layer;
- $q_p$  is the ultimate unit base resistance at the depth of the micropile tips; and
- H is the distance from the tip elevation of the micropiles to the elevation of the top of the weaker lower soil layer.

If the piles are battered, the values for  $B_g$  and  $L_g$  should be based on the plan area of the pile group at the base of the piles. Satisfaction of the condition prescribed in Eq. 5-15 should preclude the potential for a punching shear failure of the micropile group (see Figure 5-4).

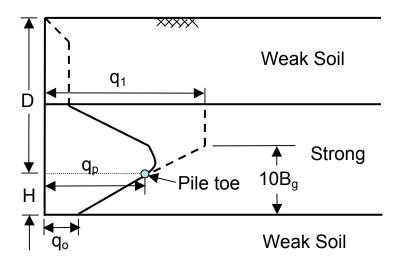


Figure 5-4. End-bearing Resistance of Piles in Layered Soils (after Meyerhof, 1976).

# 5.9.4 Evaluate Micropile Group Uplift Capacity

The design of micropile groups subject to uplift forces follows the method described in FHWA NHI-05-042 (2005) for uplift capacity for driven piles in cohesionless soils and for driven piles in cohesive soils.

Micropile Groups in Cohesive Soils

For micropile groups in cohesive soil, the group uplift capacity may be calculated based upon the undrained shear strength of the block of soil enclosed by the group plus the effective weight of the pile cap and pile-soil block as shown on Figure 5-5. This may be expressed as:

$$Q_{ug} = 2Z \times (X + Y) \times \overline{s_u} + W_g$$
 (Eq. 5-16)

where  $\overline{s_u}$  is the average undrained soil shear strength over the depth of micropile embedment along the group perimeter and  $W_g$  is the effective weight of the pile/soil block including the pile cap. In using Eq. 5-16, a factor of safety of 2.0 should be used to estimate the allowable group uplift capacity.

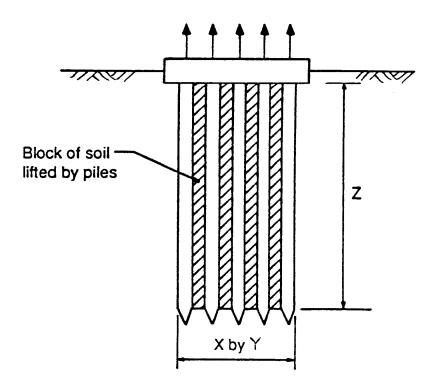


Figure 5-5. Model to Calculate Micropile Group Uplift Capacity in Cohesive Soils.

# Micropile Groups in Cohesionless Soils

The uplift capacity of a micropile group in cohesionless soil may be conservatively taken as the effective weight of a block of soil extending upward from the base of the micropiles at a slope of 1H:4V as shown on Figure 5-6. In this evaluation, the weight of the micropiles within the block is (conservatively) considered equal to the weight of the soil. Using Figure 5-6, the group uplift capacity is given by:

$$Q_{ug} = \left[ \frac{1}{3} \times \left( A_{base} + A_{top} + \sqrt{A_{base} \times A_{top}} \right) \times D \right] \times \gamma$$
 (Eq. 5-17)

where  $A_{base} = B_g \times L_g$  and  $A_{top} = (B_g + D/2) \times (L_g + D/2)$  and  $\gamma$  is the effective unit weight of the soil. In Eq. 5-17, the term in brackets is simply the volume of the enclosed soil. A FS = 1.0 is acceptable for this analysis since the shear strength that would be mobilized within the soil is conservatively neglected; this implies that the allowable micropile group capacity would be equal to the calculated group uplift capacity based on Eq. 5-17.

The allowable group uplift capacity (based on either Eq. 5-16 or 5-17) should be compared to the allowable uplift capacity of a single micropile multiplied by the number of micropiles in the group and the design should be based on the lesser group capacity.

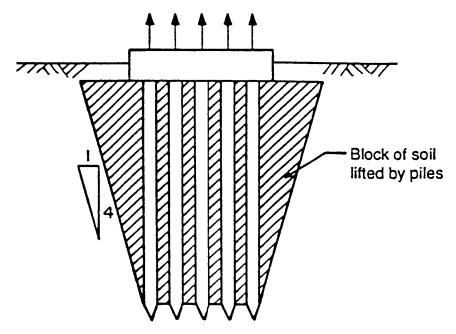


Figure 5-6. Model to Calculate Micropile Group Uplift Capacity in Cohesionless Soils.

### 5.10 STEP 9. ESTIMATE MICROPILE GROUP SETTLEMENT

## 5.10.1 General

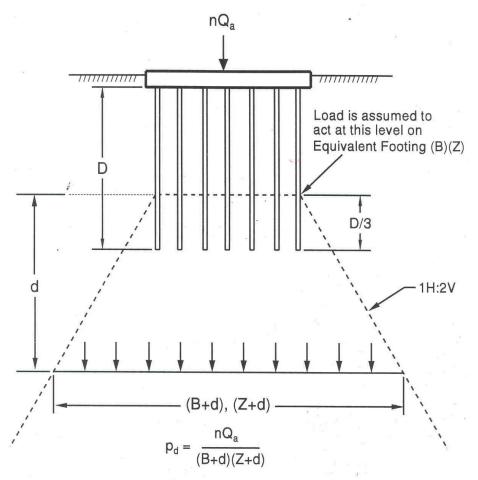
In general, methods used for estimating settlements of driven pile groups are applicable for micropile groups. The major components of settlement that need to be assessed include: (1) settlements of the ground in which the micropiles are constructed; and (2) elastic compression/tension of an individual micropile. These settlements are added together to evaluate the total settlement of the micropile group subject to the design load and are then compared to the allowable settlement.

The specific value for allowable settlement will depend on the structure being supported, but for typical highway bridge projects, the maximum vertical movement will depend primarily on anticipated differential settlements between bridge piers for single span or continuous span bridges.

# 5.10.2 Micropile Group Settlement

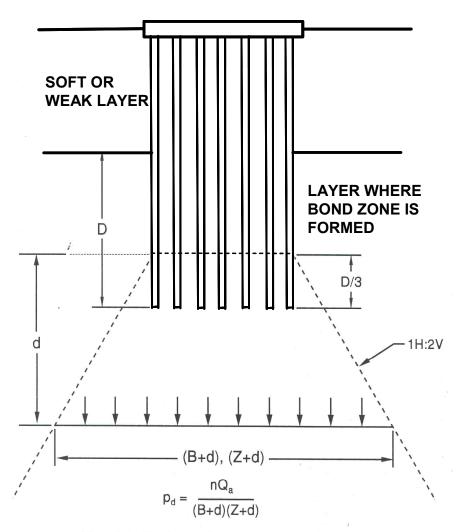
Micropiles in a group can undergo vertical displacement as a result of consolidation of soil layers below the bottom of the micropile group. Where a single pile will transfer its load to the soil in the immediate vicinity of the pile, a pile group can distribute its load to the soil layer below the group. Consideration should be made for this group displacement when the soil below the group is cohesive in nature and subject to consolidation. The method presented herein for evaluating micropile group settlements is similar to that for driven piles (see FHWA-NHI-05-042, 2005).

For purposes of calculating settlements of micropile groups in soil (for which loads are primarily transferred through side resistance), loads are assumed to act on an equivalent footing located at two-thirds of the depth of embedment of the micropiles into the layer that provides support (i.e., two-thirds of the depth of the micropile bond zone). This concept is illustrated in Figure 5-7 for a uniform soil profile and Figure 5-8 for a micropile bond zone formed in firm or strong layer that is overlain by an upper soft or weak layer (which is common for many micropile applications). Where a clayey layer may exist just below the tips of the micropiles, the equivalent footing is assumed to exist at the depth corresponding to 8/9 of the length of the bond zone. The reader is referred to FHWA-NHI-05-042 (FHWA, 2005) for additional information on the equivalent footing concept. For a pile group consisting of only vertical piles, the equivalent footing has a plan area that corresponds to the perimeter dimensions of the pile group.



Note: Pile Group has Plan Dimension of B and Z

Figure 5-7. Equivalent Footing Concept for Uniform Soil (after FHWA-NHI-05-042, 2005).



Note: Pile Group has Plan Dimension of B and Z

Figure 5-8. Equivalent Footing Concept for Firm Soil Underlying Soft Soil Layer.

The pile group load over this plan area is then the bearing pressure transferred to the soil through the equivalent footing. The load is assumed to spread within the frustum of a pyramid of side slopes at 1H:2V and to cause uniform additional vertical pressure at lower levels. The pressure at any level is equal to the load carried by the group divided by the plan area of the base of the frustum at that level. Settlements are calculated based on the pressure increase in the underlying layers. This method is conservative because compression settlements from the layer defined from just below the top of the equivalent footing to the bottom of the micropiles do not take into account the increased stiffness of the profile at this location resulting from the micropiles.

Where clayey soils may consolidate as a result of micropile group loading, nominally undisturbed tube samples should be collected from potential consolidating layers and consolidation tests should be performed to assess compressibility parameters and stress history information for the consolidating layer. The reader is referred to GEC No. 5 for specific information on consolidation testing and parameter evaluation. For micropile group settlements in cohesionless layers, SPT data is used to estimate compression parameters.

Step By Step Procedure for Micropile Group Settlement In Cohesive Soils

<u>Step 1</u>: Determine the new load imposed on soil by the pile group.

- a. Determine the location of the equivalent footing using Figure 5-7 or 5-8.
- b. Determine the dimensions of the equivalent footing. For pile groups consisting only of vertical piles, the equivalent footing has the same dimensions as the length and width of the pile group from Figure 5-7. For pile groups that include batter piles, the plan area of the footing should be calculated from the dimensions of the pile group at depth 2/3 D, including the plan area increase due to the pile batter.
- c. Determine the pressure distribution to soil layers below the equivalent footing up to the depth at which the pressure increase from the equivalent footing is less than 10% of existing effective overburden pressure at that depth. The depth at which the pressure increase is less than 10% will provide the total thickness of cohesive soil layer or layers to be used in performing settlement computations. Note that the group design load should be used in determining the pressure distribution for settlement computations, and not the ultimate group load.
- d. Divide the cohesive soil layers in the affected pressure increase zone into several thinner layers of 1.5 to 3 meter (5 to 10 ft) thickness. The thickness of each layer is the thickness H for the settlement computation for that layer.
- e. Determine the existing effective overburden pressure,  $p_0$ , at midpoint of each layer.

f. Determine the imposed pressure increase,  $\Delta p$ , at midpoint of each affected soil layer based on the appropriate pressure distribution.

Step 2: Determine consolidation test parameters.

Step 3: Compute settlements.

Using an appropriate settlement equation, compute the settlement of each affected soil layer. Sum the settlements of all layers to obtain the total estimated soil settlement from the pile group.

Step By Step Procedure for Micropile Group Settlement In Cohesionless Soils

Pile groups supported in and underlain by cohesionless soils will produce only immediate settlements implying that the settlements will occur immediately as the pile group is loaded. A procedure to calculate pile group settlements in cohesionless soils is provided below.

<u>Step 1</u>: Determine the new load imposed on soil by the pile group.

- a. Determine the location of the equivalent footing using Figure 5-7 or 5-8.
- b. Determine the dimensions of the equivalent footing.
- c. Determine the pressure distribution to soil layers below the equivalent footing up to the depth at which the pressure increase from the equivalent footing is less than 10% of existing effective overburden pressure at that depth.
- d. Divide the soil layers in the affected pressure increase zone into several thinner layers of 1.5 to 3 meter (5 to 10 ft) thickness. The thickness of each layer is the thickness H for the settlement computation for that layer.
- e. Determine the existing effective overburden pressure,  $p_0$ , at midpoint of each layer.
- f. Determine the imposed pressure increase,  $\Delta p$ , at midpoint of each affected soil layer based on the appropriate pressure distribution.

<u>Step 2</u>: Determine bearing capacity index for each cohesionless layer.

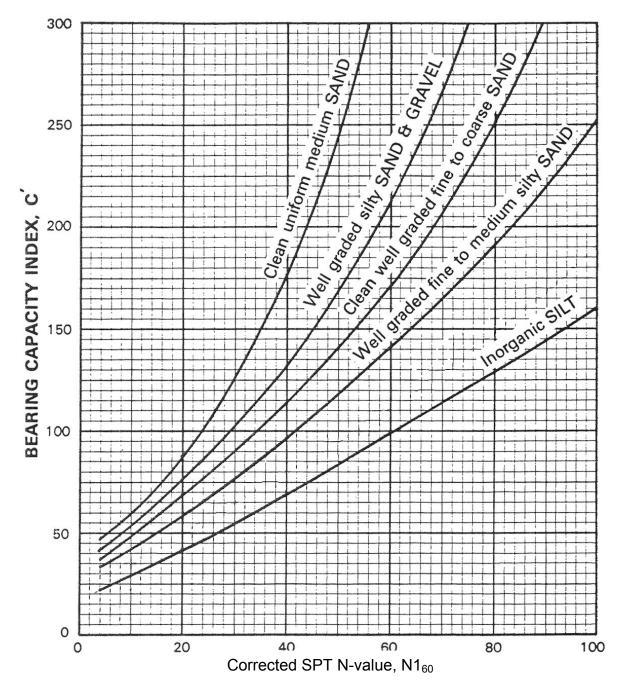
Determine the average corrected (for overburden pressure and hammer efficiency) SPT N1₆₀ value for each cohesionless layer. Use N1₆₀ in Figure 5-9 to obtain the bearing capacity index, C' for each layer.

# Step 3: Compute settlements.

Compute the settlement of each affected soil layer under the applied load using the following formula:

$$\Delta H = H_o \frac{1}{C} \log \left( \frac{p_o + \Delta p}{p_o} \right)$$
 (Eq. 5-18)

Sum the settlements of all layers to obtain the total estimated soil settlement from the pile group. If a layered soil profile is within the compressible zone being considered, the two methods previously described for cohesive and cohesionless soils can be used separately for the appropriate layers and then settlements form each layer added to obtain the total settlement from the pile group.



(Note: The "Inorganic SILT" curve should generally not be applied to soils that exhibit plasticity)

Figure 5-9. Bearing Capacity Index versus Corrected SPT Blowcount (modified after Hough, 1959).

# **5.10.3** Micropile Elastic Movement

The calculation of the elastic compression and/or elastic tension of a single micropile subject to the design compression and/or tension load are presented herein. This elastic compression value is added to the total settlement of the group resulting from consolidation (as discussed in Section 5.10.2) to obtain the total estimated pile group settlement.

Elastic displacement of a micropile is a function of the imposed load, the pile stiffness, and the load transfer characteristics of the pile to the surrounding soil via grout-to-ground bond. The elastic compression displacement,  $\Delta_{elastic}$ , of a micropile can be written in its most general form as:

$$\Delta_{elastic} = \frac{PL}{AE}$$
 (Eq. 5-19)

where P is the design load applied at the ground surface (kN), L is the length of the pile (m), A is the area of the section (m²) and E is the elastic modulus of the section (kPa). Because the stiffness of the micropile may change over its length and because axial load is transferred to the ground, the elastic displacement may be calculated as the sum of elastic displacements of "n" pile segments as follows:

$$\Delta_{elastic} = \sum_{i=1}^{n} \frac{P_i L_i}{A_i E_i}$$
 (Eq. 5-20)

where  $L_i$ ,  $A_i$ , and  $E_i$  are the length, average cross section area, and average modulus, respectively, for each of the pile segments. The term  $P_i$  is the average axial load at the pile segment. The load at the top pile segment would be the total imposed load to that individual pile, and would reduce in magnitude down to the mobilized end bearing load at the pile tip in accordance with the load transfer response from the micropile to the ground. Determination of a stiffness value, i.e., AE, for a micropile is complex due to the:

- contribution of the grout to the pile's stiffness due to the pile acting in compression; and
- varying reinforcement (type and length) used in some micropiles, with casing (and perhaps bar) reinforcement in the upper portion of the pile and bar reinforcement in the lower portion.

For estimates of displacement caused by *compression loads*, the stiffness of the composite section at a given point in the pile can be evaluated using the formula:

$$EA_{pile} = |A_{grout} \times E_{grout}| + |A_{steel} \times E_{steel}|$$
 (Eq. 5-21)

For estimates of displacement caused by *tension loads*, the stiffness of the composite section can be evaluated using the formula:

$$EA_{pile} = \left| A_{steel} \times E_{steel} \right| \tag{Eq. 5-22}$$

The value for  $E_{grout}$  can be quite variable, but for design calculations may be estimated as  $E_{grout}$  (MPa) =  $4732 \times (f'_c \text{ (MPa)})^{1/2} (E_{grout} \text{ (ksi)} = 57 \times (f'_c \text{ (psi)})^{1/2})$ .

A conservative approach to calculate elastic displacement is to assume that no load is transferred to the ground over the length of the micropile from the top of the micropile to the top of the bond zone; this implies that the elastic compression of this length of the micropile can be calculated according to Eq. 5-19 with P equal to the design load and L equal to the length of the micropile above the bond zone. If there are changes in the micropile cross section over that length (e.g., section with just reinforcing bar and section with reinforcing bar and casing), then Equation 5-20 is used with pile segment lengths defined based on changes in cross section.

In the bond zone, the cross section of the micropile will usually be constant. Therefore, since it is assumed that the design load is carried uniformly over the length of the bond zone in side resistance; the elastic displacement along this length of the micropile can be calculated using Eq. 5-19 with P equal to the design load and L equal to one-half the length of the bond zone.

For micropiles bonded in rock or for end-bearing micropiles on rock, the full length of the micropile above the top of rock should be assumed for the elastic length. It is noted that the assumption of the lengths over which elastic movements occur can be confirmed via load testing in which loads are incrementally cycled (similar to a ground anchor performance test) to allow for measurement of the elastic movement.

An example calculation of elastic compression and tension displacement for a micropile is provided in Sample Problem No. 1.

## 5.11 STEP 10. DESIGN MICROPILE CONNECTION AT PILE CAP

Unless a single micropile is used to support a load, a pile cap (footing) is necessary to spread the structure loads and any overturning moments to all the micropiles in the group. Reinforced concrete pile caps are designed in accordance with the AASHTO Standard Specifications for Highway Bridges and individual DOTs may have minimum requirements for pile caps (e.g., minimum concrete cover, minimum embedment of pile top into cap). The structural design of reinforced concrete pile caps is not addressed in this manual.

The connection between the top of the micropiles and the reinforced concrete pile cap can vary depending on the required capacity of the connection, the type of micropile reinforcement, and the details of the pile cap. Seven examples of the pile-to-footing connections are shown in Figures 5-10 through 5-16. Figures 5-10 through 5-13 show typical connections for piles that can have both tension and compression loads depending on load case. Figures 5-14 through 5-16 show simple connections for piles that are only in compression.

Figure 5-10 shows a composite reinforced micropile connected to a new (or extended) footing. The footing tension and compression load is transferred to the pile through the top bearing plate. The stiffener plates provide bending strength to the plate, plus provide additional weld length for transferring the load from the bearing plate to the pile casing. The stiffener plates can be eliminated if the support of the top plate and additional weld length are not required. Additional considerations for this connection detail include the following:

- The portion of the tension load carried by the reinforcing bar can be transferred to the top plate through the nut, reducing the plate-to-casing weld requirement.
- The bond between the pile casing and the footing concrete can be utilized, reducing the load capacity required for the top plate and top plate to casing weld.
- A portion of the compression load can be transferred from the top plate to the casing through bearing, reducing the weld capacity requirement. This requires a higher level of quality for the fabrication of the bearing surface between the casing and the plate.

Sample Problem No. 1 includes the design of a pile connection similar to that shown in Figure 5-10. The additional considerations listed above are not included in the sample problem calculations.

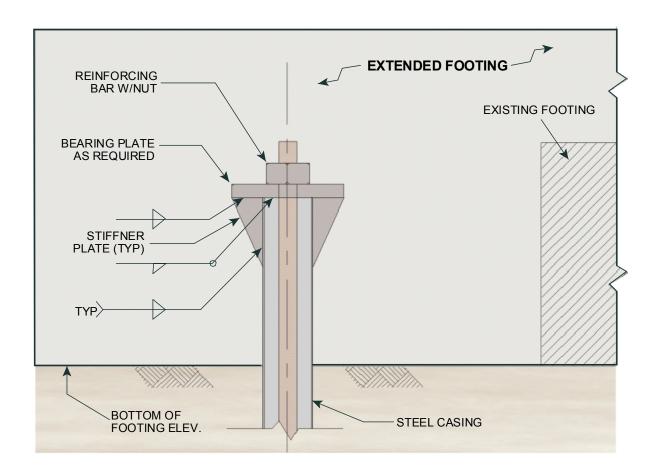


Figure 5-10. Pile to Footing Connection Detail (compression and tension loads).

Figure 5-11 shows a composite reinforced micropile connected to an existing footing. The pile is installed through an oversized hole cored through the existing footing or slab. After the pile is installed, the annulus between the core hole and the micropile is cleaned (usually via pressure washing) and filled with non-shrink cement grout. Steel rings are welded to the top section of the casing prior to pile installation. These rings transfer the pile load from the casing to the non-shrink grout. Adequate spacing must be used between the rings to avoid combining bearing stresses in the concrete and grout. The total capacity of the connection is controlled by the sum of the bearing strength of the rings, the capacity of the load transfer across the interface between the non-shrink grout and the existing concrete, and the shear capacity of the existing concrete.

Grooves may be chipped into sides of the core hole (typical dimension = 20 mm deep and 32 mm wide (3/4 in. deep and  $1 \frac{1}{4} \text{ in.}$  wide)) to increase the load carrying capacity of the grout to existing concrete. Also, vertical reinforcing bars may be

drilled and epoxied into the existing concrete around the exterior of the connection to increase the punching shear capacity.

For thick existing footings, the shear rings and grooves in Figure 5-11 may be eliminated. Load tests on the connections are appropriate to verify the casing to grout bond and grout to existing concrete bond for the proposed materials and methods. If this connection is proposed for a project, the Contractor should be required to perform a load test, provide load test data from previous projects, or provide in-house testing to quantify that the proposed connection will be able to support the design load.

Figure 5-12 shows a composite reinforced micropile connected to a new footing. The footing compression load is transferred to the pile through bearing on the pile top and reinforcing bar plate and the tension load is transferred through bearing on the reinforcing bar plate. A portion of the load transferred from the footing to the pile may be attributed to the bond between the pile casing and the footing concrete.

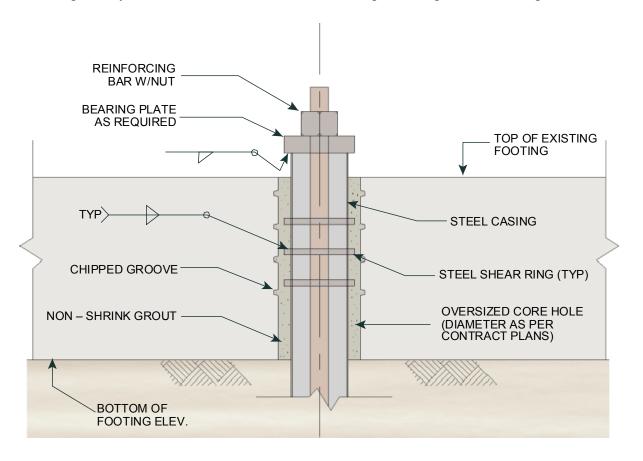


Figure 5-11. Pile to Footing Connection (compression and tension loads).

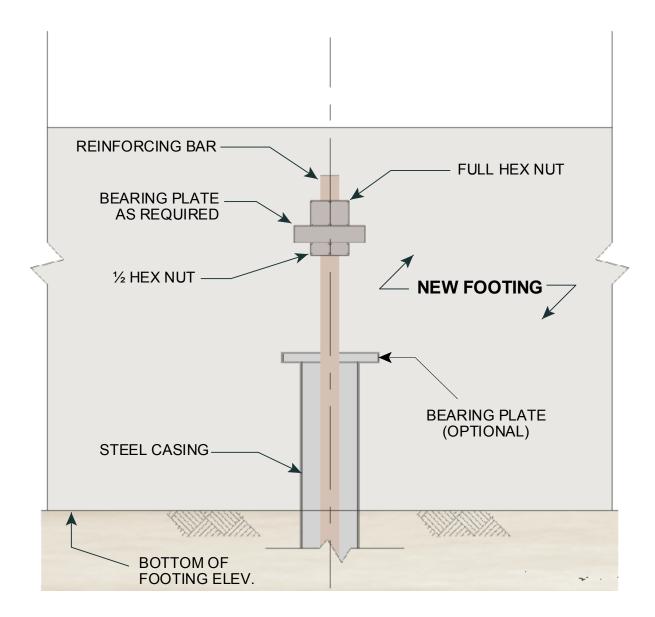


Figure 5-12. Pile to Footing Connection (compression and tension loads).

Figure 5-13 shows a bar-reinforced micropile cast into a new footing. The compression and tension load is transferred to the pile through bearing on the bar plate, and through bond between the footing concrete and the reinforcing bar. Competency of the construction joint between the pile grout and footing concrete is an important quality consideration for this pile type.

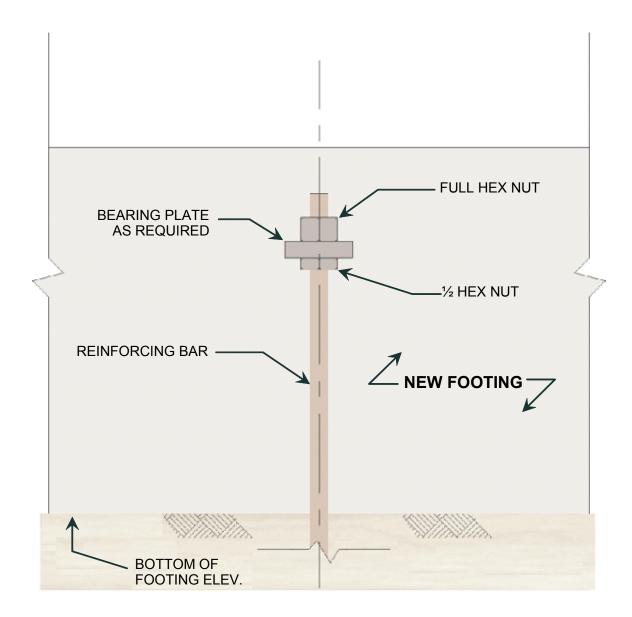


Figure 5-13. Pile to Footing Connection (compression and tension loads).

Figure 5-14 shows a typical compression connection for a moderately loaded micropile where concrete bearing stress on the pile top is within AASHTO limits (see AASHTO Section 8.15.2.1.3). Figure 5-15 shows a typical compression connection for a heavily loaded micropile where a bearing plate welded to the casing is required for concrete bearing stress on the pile top to be within AASHTO limits.

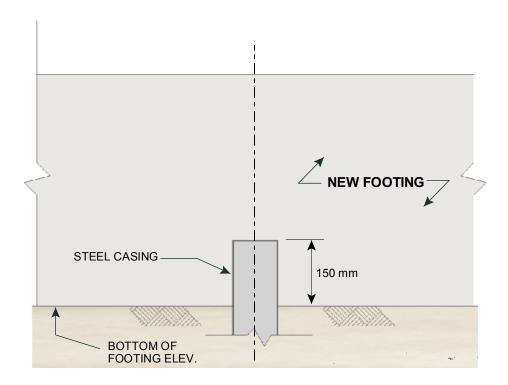


Figure 5-14. Pile to New Footing Connection Detail used for Moderate Loads (compression loads).

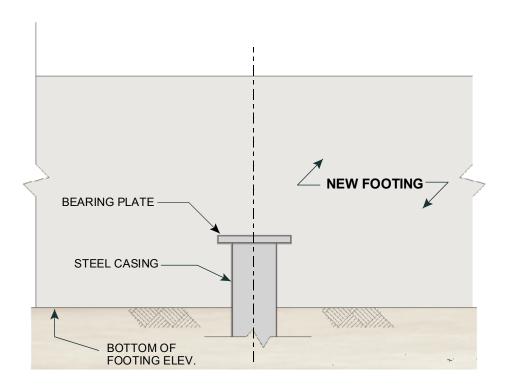


Figure 5-15. Pile to New Footing Connection Detail used for High Loads (compression loads).

Figure 5-16 shows a compression connection for a pile through an existing footing. The bond of the non-shrink grout to the footing is a function of the proposed methods (cored hole, down-the-hole hammered hole, etc.) and materials (non-shrink grout, existing concrete, etc.). Connection load tests are appropriate to verify the design.

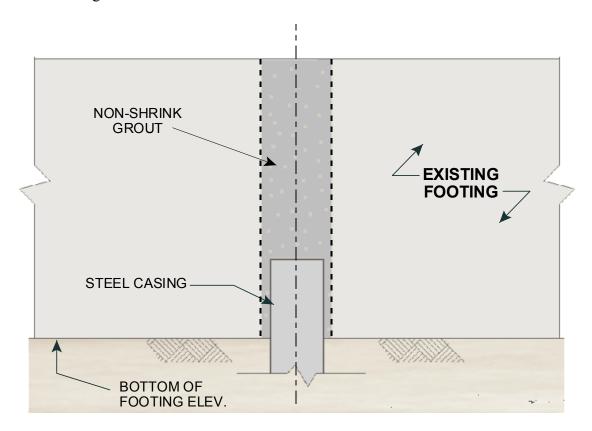


Figure 5-16. Pile to Existing Footing Connection Detail (compression loads).

## 5.12 STEP 11. DEVELOP LOAD TESTING PROGRAM

Section 7.6 of this Manual provides specific information on the evaluations to be performed as part of the development of a load testing program. Of primary importance is that the scope of the load testing program be consistent with the selected factor of safety for the grout/ground bond strength used for geotechnical capacity evaluations. In Section 5.9.2, the minimum requirements for verification and proof testing were described which are consistent with a factor of safety of 2.0.

For load testing, maximum test loads should not exceed 80 percent of the ultimate structural capacity of the micropile. The ultimate structural capacity is given by:

$$P_{ult-compression} = \left[0.85 f_{c-grout}^{\prime} \times A_{grout} + f_{y-ca \sin g} \times A_{ca \sin g} + f_{y-bar} \times A_{bar}\right] \text{ (Eq. 5-23)}$$

$$P_{ult-tension} = \left[ f_{y-ca \sin g} \times A_{ca \sin g} + f_{y-bar} \times A_{bar} \right]$$
 (Eq. 5-24)

For some designs, the verification test pile(s) may require larger pile casing and reinforcing bar than the production micropiles. The resulting stiffer micropile can adequately confirm the grout-ground bond strength for production micropiles, but will likely not provide representative structural displacement behavior. The deflections measured for proof-tested micropiles will need to be relied upon to provide best estimate of structural deflections.

#### 5.13 STEP 12. PREPARE DRAWINGS AND SPECIFICATIONS

When the design has been finalized, drawings and specifications are prepared and the procedures that will be used to verify micropile capacity (e.g. load testing) should be defined. At the time of the bid, all of the quality control procedures to be used for the project should also be defined and included in the specifications. Example typical drawings and specifications is provided in Sample Problem No. 1.

## 5.14 CORROSION PROTECTION

# 5.14.1 Background

Protecting the metallic components of a micropile against the detrimental effects of corrosion is necessary to assure adequate long-term durability of the micropile. The degree and extent of corrosion protection is a function of loading condition, the expected service life of the micropile, the aggressiveness of the ground, the perceived importance of the structure, and consequences of failure. In all cases, it is the responsibility of the Project Designer to select the corrosion protection for each micropile.

The variables which indicate a high corrosion potential include:

- low resistivity of ground;
- high concentration of chlorides or sulfides in ground or groundwater;
- too low or too high hydrogen potential (pH) of ground or groundwater;
- high saturation conditions; and
- stray currents.

The factors above collectively define ground corrosion potential (or aggressivity of the ground). In addition to corrosion of metallic components, potential degradation of the cement grout as a result of sulfate, chloride, and/or acid attack should also be considered. Information on cement degradation as it applies to pile design is provided in FHWA-NHI-05-042.

# 5.14.2 Evaluation of Soil Corrosion Potential

Tests listed in Table 5-5 are used to classify the corrosion potential of the ground.

Table 5-5. Criteria for Assessing Ground Corrosion Potential (Elias et al., 2001).

Test	Units	Strong Corrosion Potential/Aggressive	AASHTO Test Method
рН	-	< 5, >10	T 289
Resistivity	ohm-cm	<3,000	T 288
Sulfates	ppm ⁽¹⁾	>200	T 290
Chlorides	ppm	>100	T 291

Note: (1) ppm = parts per million.

In general, the ground is classified with a strong corrosion potential or aggressive **if any one of the conditions listed in the third column of Table 5-5** exceeds the limits listed during the service life of the micropile. In addition, buried structures immediately adjacent to the project exhibiting corrosion or direct chemical attack might be an indication of strong corrosion potential. If tests are not performed, then the ground should be assumed to be aggressive. Classification of ground aggressivity should consider the possibility of changes during the service life of the structure which may cause the ground to become aggressive (e.g., near mining operations, chemical plants, or chemical storage areas).

## **5.14.3** Corrosion Protection Systems

## 5.14.3.1 Methods for Corrosion Protection of Reinforcing Steel

Corrosion protection can be provided by physical and chemical protection, or a combination thereof. Physical protection involves placing a continuous barrier between the reinforcing bar, pipe casing, other metallic parts, and the corrosion sources. Chemical protection consists of the use of a sacrificial material or a dielectric material, which will preclude the flow of electric current. Some of the corrosion protection systems currently in use utilize a

combination of these mechanisms. The most common systems used to provide corrosion protection for micropiles are described below.

## **Grout Protection**

This method of corrosion protection is used as a protective measure for the steel reinforcing bar and involves fully covering the reinforcing bar with neat cement grout. Centralizers are applied along the length of the bar (Figure 5-17(a)) to ensure adequate cover of grout between the bar and the side of the borehole. After the bar is centered in the drillhole, neat grout is injected and fills up the annular space around the steel bar. The grout provides an alkaline environment that reduces corrosion potential.

# Epoxy Coating

Corrosion protection with epoxy consists of coating the reinforcing rod with a fusion-bonded epoxy that is applied by the manufacturer prior to shipment to the construction site. The minimum required thickness of epoxy coatings is typically 12 mils (0.3 mm). Thicker coatings may reduce steel to grout bond. The epoxy coating provides physical and chemical protection, as epoxy is a dielectric material. In transporting and handling bars, the epoxy coating may be damaged before bar installation. Therefore, it is not uncommon to spray epoxy coating in the field on chipped or nicked surfaces. Applicable standards for epoxy coating and allowable extent of damage (i.e., number of discontinuities in epoxy coating per unit length of bar) are found in ASTM A775/AASHTO M282. Patching materials should be approved by the epoxy coating manufacturer and should be inert in cement grout.

## Galvanized Coating

A common method of providing corrosion protection is galvanization, which consists of applying a zinc coating on the steel surface. The process is performed by hot-dipping bars and other metallic pieces with zinc. The protection provided by galvanized coating is both physical and chemical, as this process forms a protective layer of zinc oxide. Galvanization shall meet the requirements of ASTM A153. Galvanization should not be used on high strength bars.

# Encapsulation

For maximum corrosion protection, a polyvinyl chloride (PVC) or high-density polyethylene (HDPE) (minimum 1-mm (0.04-in.) thick for PVC and 1.5-mm (0.06-in.) thick for HDPE) sheathing may be installed around the reinforcing bar similar to what is done for ground anchors in permanent applications. The sheathing is corrugated to transfer load to the surrounding grout. Grout-filled corrugated sheaths comprise double corrosion protection.

This system may be used with DSI threadbar and GEWI Bar (Figure 5-17(b)) and others. The encapsulation shall meet the requirements for encapsulation of soil and rock ground anchors as provided in PTI (2004).

# 5.14.3.2 Methods for Corrosion Protection of Steel Casing

Grout that may fill the annulus outside the steel casing is not considered to be sufficient to provide a quantifiable level of corrosion protection. Corrosion resistant coatings on permanent drill casing is impractical due to the abrasive action of the soil on the outer surface of the casing which would likely result in damage to the coating. Corrosion protection for steel casing subject to compressive loads in aggressive environments is typically considered by including a sacrificial steel thickness in the design. Casing should not be used to carry tension loads in aggressive ground environments.

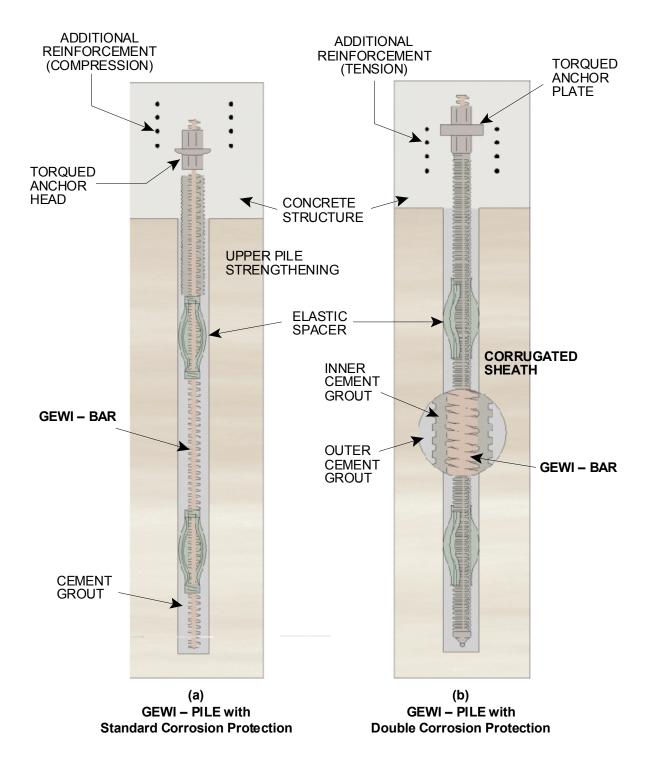


Figure 5-17. GEWI Piles with (a) Grout Protection only; and (b) Double Corrosion Protection (Courtesy of DSI).

# 5.14.3.3 Corrosion Protection Requirements for Micropiles

Corrosion protection recommendations for micropiles are provided in Table 5-6.

Table 5-6. Corrosion Protection Recommendations for Micropiles (after DFI, 2004).

Corrosion Protection							
Loading	Tension ¹		Compression				
Ground	Aggressive ²	Non aggressive	Aggressive ²	Non-aggressive			
Casing	a. Do not rely on casing for load capacity	<ul> <li>a. None required if tension load on casing is less than 20% of casing thread strength</li> <li>b. Do not rely on casing for load capacity</li> </ul>	a. Min.1.6 mm (0.063 in.) corrosion loss on outside  The Specifier may use different corrosion loss per site-specific corrosion studies.	a. None  The Specifier may use different corrosion loss per site-specific corrosion studies.			
Core steel (reinforcing bar) ¹	<ul> <li>a. epoxy coating³</li> <li>OR</li> <li>b. galvanization³</li> <li>OR</li> <li>c. encapsulation in plastic sheath³</li> <li>AND</li> <li>Grout cover⁴</li> </ul>	a. bare steel ⁵ OR b. epoxy coating ³ OR c. galvanization ³ OR d. encapsulation in plastic sheath ³ AND Grout cover ⁴	a. Grout cover ⁴ AND The Specifier may desire to add other options listed for tension.	a. Grout cover ⁴			

# NOTES:

- 1. Permanent tension or temporary tension (e.g., wind, seismic, impact) on critical structures. For temporary tension on normal structures, corrosion protection for compression may be used. The recommendations for corrosion protection for micropiles subject to tension loadings should also be used for that length of the micropile subject to tension as a result of lateral loads and/or overturning moments at the ground surface.
- 2. Corrosion protection must extend 5 m (15 ft) below corrosive material
- 3. Core steel corrosion protection must extend a minimum of 1.5 m (5 ft) into casing
- 4. Minimum 1 inch in soil and 0.5 inch in rock. If protective coatings (epoxy, galvanization, or encapsulation) are provided in compression, minimum cover may be 0.25 inches in soil or rock.
- 5. Not recommended for permanent or cyclic tension loads.

Corrosion protection requirements (via sacrificial steel section losses) prescribed in Table 5-6 for casings subject to compressive loads in an aggressive ground environment include a minimum section loss of 1.6 mm (0.063 in.). This value is prescribed in AASHTO Section 4.5.7.4 for cross section reductions for concrete-filled pipe piles. Guidance on sacrificial thickness for structural steel elements in CCTG (1992) indicate that, for a design life of 75 years, a steel section loss range of 2 mm (0.0787 in.) to 5 mm (0.196 mm) is appropriate for non-protected steel in moderately to strongly corrosive environments, respectively, where no specific site corrosivity studies for the steel elements have been performed. Higher section losses are provided for a design life greater than 75 years.

These information sources provide a relatively wide range of corrosion losses. It is strongly recommended that site-specific corrosivity studies be performed where micropiles will be used in aggressive ground (as defined in Table 5-5).

#### 5.15 PLUNGE LENGTH

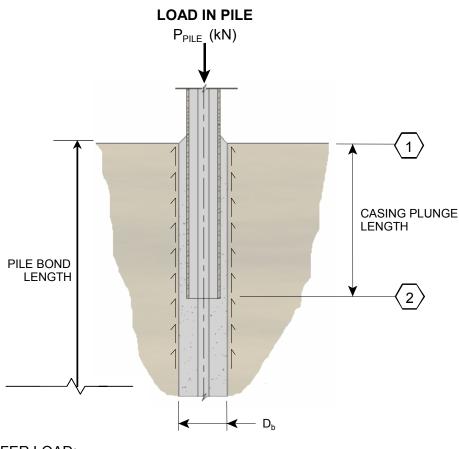
The micropile detail shown in Figure 5-1 depicts a casing plunge length. With this detail (primarily used for micropiles with bond zones formed in soil), it is assumed that a portion of the micropile design load is transferred to the surrounding ground (over the plunge length) by the cased portion of the pile, thus reducing the load that must be supported by the uncased portion of the micropile (see Figure 5-18). This can allow a lesser amount of steel reinforcing through the uncased length to meet the structural strength requirements. The reduction in load applied to the uncased length is termed the transfer load, P_{transfer}.

The allowable axial load transferred through the plunge length,  $P_{transfer-allowable}$  may be calculated as:

$$P_{transfer-allowable} = \frac{\alpha_{bond}}{FS} \times \pi \times D_b \times (Plunge Length)$$
 (Eq. 5-25)

The value for this load is based on the unit grout-to-ground bond,  $\alpha_{bond}$  (from Table 5-3) acting uniformly over the casing plunge length. It must be recognized that reliably achieving this load transfer depends on the casing installation method, the specific soil type and grouting method to obtain sufficient grout coverage between the casing and the surrounding ground.

For these reasons, micropile designs which incorporate a plunge length and a corresponding reduction in axial load reaching the uncased portion should be confirmed by the site-specific load testing information wherein axial load transfer over the plunge length is measured or can be computed based on verification load testing. Alternatively, P_{transfer} may be conservatively neglected.



TRANSFER LOAD:

 $P_{\text{TRANSFER}} = \quad \alpha_{\text{bond}} \times \ 3.14 \times D_{\text{b}} \times \text{Casing Plunge Length}$  LOAD CARRIED BY PILE @ DEPTH 1 =  $P_{\text{PILE}}$  LOAD CARRIED BY PILE @ DEPTH 2 =  $P_{\text{PILE}} - P_{\text{TRANSFER}}$ 

Figure 5-18. Detail of Load Transfer Through the Casing Plunge Length.

## 5.16 END BEARING MICROPILES

Due to the relatively small cross sectional area of micropiles, load carrying capacity resulting from end bearing is generally considered to be negligible for micropiles in soil or weak rock.

Micropiles founded on high quality sound rock, however, may develop their capacity primarily through end bearing and secondarily by side resistance. In this case, care must be taken to ensure that the micropile is not terminated on a boulder or on rock with voids or very soft material below. Where end bearing micropiles are being considered, the subsurface investigation should be sufficiently detailed to allow for a determination of the quality of the rock (see Table 5-2).

The design for end bearing micropiles may be done similar to end bearing drilled shafts, or may be based on previous load test experience of similar micropiles. Typically, a nominal length rock socket may be used (on the order of 0.6 m (2 ft)) to assure that the micropile is, in fact, founded on high quality rock. The capacity of end bearing micropiles on competent rock will likely be controlled by the structural capacity of the micropile since very high end bearing capacities can be achieved for micropiles on rock.

## 5.17 DOWNDRAG

Micropiles may be subjected to additional axial compression loading due to downdrag forces when the soils in contact with the cased portion of the micropile (i.e., above the bond zone) move downward relative to the micropile and tend to "drag" the micropile downward. The resulting downward force will add to the load applied to the micropile by the structure at the ground surface. The user of this manual is referred to the NHI/FHWA reference manuals for design of driven piles and for drilled shafts (FHWA-NHI-05-042 and FHWA-IF-99-025, respectively) for background information on downdrag and methods to compute downdrag forces.

The potential for downdrag exists when the surface soils can settle and where the foundation element passes through those settling soils into a stratum of relatively rigid geomaterial. Possible development of downdrag loads on micropiles should be considered where: (1) the site is underlain by compressible silts, clays, or peats; (2) fill has recently been placed on the earlier; and (3) the groundwater is substantially lowered.

If analyses or computations indicate that the surface soils are moving downward more than the micropile, a conservative solution can be obtained if it is assumed that the downdrag force will develop along the micropile from the ground surface to the top of the bond zone. To compute the downdrag force from the upper weak material, grout-to-ground bond stress values based on Table 5-3 should be used with consideration for the grouting technique used over the length of the micropile formed in the relatively weak materials. The maximum load along the micropile would occur at the top of the bond zone and would be the sum of the downdrag force and the load applied at the top of the micropile. The structural capacity of the micropile would be checked based on this total load.

The use of micropiles for a foundation system on sites where downdrag forces are of concern offers several benefits. The small surface area of a micropile will result in relatively small downdrag forces transmitted from the settling soil to the micropile. Further isolation of the micropile from the moving soils can be accomplished by installation of an additional oversized outer casing through the settling soils. Battered micropiles should not be used in soil conditions where large soil settlements are expected because of the additional bending forces imposed on the piles.

## 5.18 DESIGN OF MICROPILES FOR LATERAL LOADING

#### **5.18.1** General

It is specifically noted that the analysis of a single vertical micropile for lateral loading and/or overturning moments is equivalent to that for a driven pile or drilled shaft. The user of this manual is referred to the NHI/FHWA reference manuals for design of driven piles and for drilled shafts (FHWA-NHI-05-042 and FHWA-IF-99-025, respectively) for specific modeling details related to lateral loading analysis. Herein, the overall design procedure for a laterally loaded micropile is provided (within the context of a p-y analysis) and specific issues that must be addressed for the design of a micropile subject to lateral load are discussed.

## 5.18.2 Analysis Steps for Single Laterally Loaded Micropile

<u>Step 1:</u> Determine basic pile input parameters for the micropile including: (1) pile length; (2) modulus of elasticity for grout, reinforcing bar, and steel casing; (3) distance from pile head to ground surface; and (4) slope of ground surface.

<u>Step 2:</u> Divide the micropile into segments with uniform cross sectional properties. For each segment, provide the pile diameter, moment of inertia, and area of pile.

A micropile subject to lateral loads and/or overturning moments will include a cased length in the upper portion of the micropile. A center steel reinforcing bar may be used along the entire length of the micropile, however the steel bar provides negligible resistance to lateral loads. Lateral loads and overturning moments applied at the ground surface will usually be carried by the portion of the micropile from the ground surface down to a depth on the order of 20 micropile diameters; below that depth bending moments will usually be negligible. The length of the micropile to be analyzed should be such that calculated bending moments, shear forces, and lateral pile movement are negligible at the bottom of the micropile. This length can be used to select the minimum micropile cased length.

<u>Step 3:</u> Delineate the soil/rock profile into layers over the maximum anticipated penetration depth of the trial micropile.

<u>Step 4:</u> Determine the required soil input parameters for each layer. For cohesive soil layers, the effective unit weight of the soil and the undrained shear strength is required for analysis while for cohesionless soils, the effective unit weight and drained friction angle is required.

The user inputs two additional parameters: (1)  $\varepsilon_{50}$  which is the axial strain corresponding to a shear stress equal to  $\frac{1}{2}$  of the shear strength of the material (this parameter is used for clays only); and (2) slope of the soil resistance versus lateral deflection curve, k. These values are typically selected based on soil type using Tables 5-7 through 5-10.

It is noted that user-defined p-y curves can be used for analysis where these curves are based on micropile lateral load test results (which include pile lateral movement measurements at the ground line and at various depths along the length of the micropile) from previous projects in similar ground or preproduction test piles. Actual foundation lateral displacements will likely be less than those measured in a load test since most load test setups do not incorporate the beneficial effects of pile cap stiffness and embedment below the ground surface which will likely be part of the actual foundation structure.

Most engineers, however, simply use the p-y curves contained within programs such as LPILE. These p-y curves have not been developed specifically for relatively small diameter micropiles but can provide reasonably accurate results. Moreover, good subsurface and shear strength characterization of the ground in the upper 5 m (15 ft) of the subsurface profile is critical to developing p-y curves for analysis (Richards and Rothbauer, 2004). If overly conservative assumptions regarding soil shear strength near the ground surface are used, it is likely that ground line lateral movements will be significantly overpredicted. Site specific strength data should be obtained.

Table 5-7. Values of  $\varepsilon_{50}$  for intact clays (after Reese et al., 2005).

Consistency of clay	ε ₅₀
Soft	0.020
Medium	0.010
Stiff	0.005

Table 5-8. Values of  $\epsilon_{50}$  for stiff clays (after Reese et al. 2005).

Undrained shear strength		
(kPa)	(psi)	$oldsymbol{arepsilon}_{50}$
50 – 100	7.3 - 14.5	0.007
100 -200	14.5 - 29.0	0.005
300 -400	43.5 – 58.1	0.004

Table 5-9. Soil-modulus parameter (k) for sands (after Reese et al., 2005).

Loose		Medium		Dense		
Relative Density	(kPa/m)	$(lb/in^3)$	(kPa/m)	(lb/in ³ )	(kPa/m)	(lb/in ³ )
Submerged Sand	5,430	20	16,300	60	33,900	125
Sand Above WT	6,790	25	24,430	90	61,000	225

Table 5-10. Soil-modulus parameter (k) for clays (after Reese et al., 2005).

Clay	Undrained Shear Strength		Static		Cyclic	
Consistency	(kPa)	(psi)	(kPa/m)	$(lb/in^3)$	(kPa/m)	$(lb/in^3)$
Soft	12 – 24	1.74 – 3.47	8,140	30	-	-
Medium	24 – 48	3.47 – 6.94	27,150	100	-	-
Stiff	48 – 96	6.94 – 13.9	136,000	500	54,300	200
Very Stiff	96 – 192	13.9 – 27.8	271,000	1,000	108,500	400
Hard	192 - 383	27.8 – 55.6	543,000	2,000	217,000	800

<u>Step 5:</u> Determine the critical loading combinations and boundary conditions to be analyzed.

For each loading combination, determine the axial load, lateral load, and overturning moment at the ground line to be analyzed. An important input to the analysis is the assumed boundary condition at the ground line. In general, the assumption of full fixity at the pile head will result in large calculated negative bending moments at the top of the pile and small lateral deflections at the ground line. Conversely, the assumption of a pinned pile head connection will result in the largest calculated bending moment below the ground surface and relatively large calculated movements at the ground surface. The use of vertical micropiles to carry lateral loads is a relatively new application and little data exists to define the appropriate level of fixity for a given micropile-footing connection to be assumed for design analyses.

Typical practice is to evaluate the maximum bending moment from an analysis assuming pinned head conditions (i.e., 0% fixity) and the maximum bending moment from an analysis assuming fixed head conditions (i.e., 100% fixity). The structural capacity of the micropile is then checked for the larger of the two calculated bending moments.

Calculated ground line deflections are also affected by the assumed level of fixity for the micropile-footing connection. For assessing ground line deflections, a representative level of fixity should be assumed. In other words, the approach used to evaluate structural capacity is based on the "worst-case" bending moment from two analyses. This approach should not be used to assess deformations, but instead the level of fixity assumed to evaluate ground line deflections should be consistent with the actual micropile-footing connection. If a certain level of fixity is assumed in design, this level of fixity must be at least achieved by the actual (i.e., as-built) micropile-footing connection. To this end, Table 5-11 provides preliminary guidance for selecting a level of fixity for a given micropile-footing connection. The level of fixity (i.e., 0, 50, or 100 percent) can then be used in a lateral pile analysis to compute the lateral ground line deflection.

For a given micropile-footing connection, greater fixity than that reported in Table 5-11 may be able to be achieved. The user of this manual should assess fixity on a project-specific basis.

Table 5-11. Guidance on Level of Fixity for Micropile-Footing Connections.

0 % Fixity (Pinned Head Condition)	50 % Fixity ⁽¹⁾	100 % Fixity (Fixed Head Condition) ⁽¹⁾
Casing embedment of 300 mm	Casing embedment of	Casing embedment of
(12 in.) or less or	450 mm (18 in.) or	600 mm (24 in.) or
		more
Reinforcing bar embedment with	Shear connection	
or without bearing plate or	between casing and	
	existing footing with	
Any detail where top of	minimum casing	
micropile embedment is at or	embedment of 450 mm	
below the level of the bottom	(18 in.)	
reinforcement of the footing		

(1) Guidance provided assumes that footing itself is restrained. For example, if only one row of piles in direction of loading then 0% fixity should be assumed

Example LPILE analysis results are provided in Figure 5-19 and 5-20. The 50% fixity condition can be modeled in LPILE as follows:

- Perform LPILE analysis for case of 100% fixity (i.e., assume slope of zero for top of micropile) and compute negative bending moment at ground line, M_{neg (100%)};
- Perform second LPILE analysis with an assumed moment boundary condition equal to 50 percent of  $M_{neg (100\%)}$ ; this analysis is used to obtain the ground line deflection.

Example LPILE analysis results and structural evaluation of the cased length using the combined stress (i.e., combined axial and bending) check (Eqs. 5-4 and 5-6) are provided in Sample Problem No. 2.

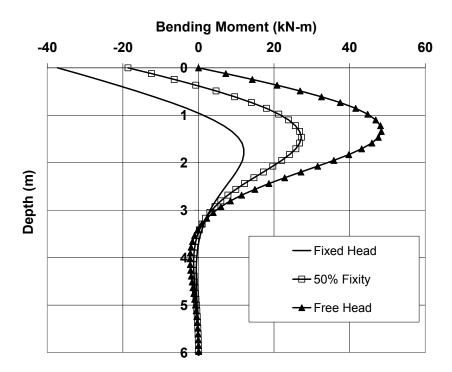


Figure 5-19. LPILE Analysis Result for Bending Moment.

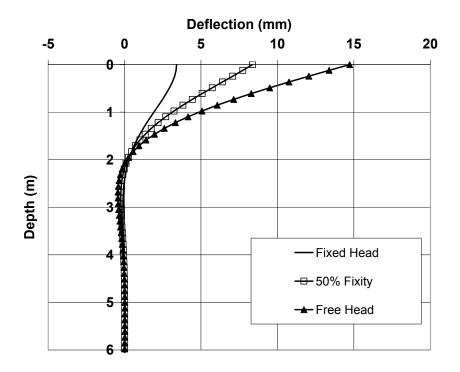


Figure 5-20. LPILE Analysis Result for Lateral Micropile Deflection.

<u>Step 6:</u> Determine structural capacity of the micropile for the critical case axial and lateral load.

The structural capacity of the micropile should be verified for combined stresses due to axial load and bending moment using Eq. 5-3 or Eq. 5-6. As previously mentioned, it may be conservatively assumed that the maximum bending moment is carried completely by the steel casing with no load being carried by the grout inside the casing. For this evaluation, it is assumed that the structural capacity of the micropile is not impacted by potential weaknesses at the threaded casing connection. The capacity of the connection and its effect on lateral load capacity is discussed in Section 5.5.3 and Section 5.18.3.

If the condition prescribed in Eq. 5-3 or Eq. 5-6 is not met, additional lateral loading capacity can be achieved by:

- installing an oversized casing in the top portion of the micropile where bending moments are high;
- constructing a larger micropile diameter at the top (which will tend to increase lateral soil resistance);
- embedding the pile cap deeper below the ground surface to develop more passive resistance which will result in reduced groundline deflections and bending moments (for a given lateral load); or
- battering some of the micropiles.

These options would need to be evaluated on a project-specific basis. For example, embedding the pile cap deeper may not be a viable option if the foundation layout has already been finalized for the project. That is, specific options may be outside the control of the micropile contractor.

<u>Step 7:</u> Determine pile acceptability based on deflection under the design load and modify the pile section properties, as needed, to meet lateral capacity and maximum groundline deflection criteria.

## 5.18.3 Evaluation of Micropile Lateral Load Capacity at Threaded Casing Joints

A conservative approach is provided herein to evaluate the bending moment capacity at a threaded casing joint. The method assumes that the wall thickness, t_w, of the casing at the location of a threaded joint is equal to 50 percent of the intact casing wall thickness; therefore

the section modulus at the joint location is reduced. The outside diameter of the casing at the joint is then equal to OD - 2 ( $t_w/2$ ) =  $OD - t_w$ . The reduced section modulus of the threaded joint,  $S_{ioint}$  is calculated as:

$$S_{jo \text{ int}} = \frac{I_{jo \text{ int}}}{(OD - t_w)/2} = \frac{\frac{\pi}{64} \times \left( (OD - t_w)^4 - ID^4 \right)}{(OD - t_w)/2}$$
 (Eq. 5-26)

Eq. 5-3 is used to evaluate the maximum bending moment at a joint location,  $M_{max\ (joint)}$ , as follows:

$$M_{\max(jo\,\text{int})} = S_{jo\,\text{int}} \times \left(1 - \frac{f_a}{F_a}\right) \times \left(1 - \frac{f_a}{F_e}\right) F_b$$
 (Eq. 5-27)

The use of this method is demonstrated and discussed in Sample Problem No. 2.

## 5.19 LATERAL RESISTANCE OF MICROPILE GROUPS

#### **5.19.1** General

Similar to other types of piles, micropile behavior in a group configuration is influenced by spacing between individual elements. The deflection of a pile group under a lateral load may be 2 to 3 times larger than the deflection of a single pile loaded to the same intensity. Holloway et al. (1981) and Brown et al. (1988) reported that piles in trailing rows of pile groups have significantly less resistance to a lateral load than piles in the lead row, and therefore exhibit greater deflections. This is due to the pile-soil-pile interaction that takes place in a pile group. The pile-soil-pile interaction results in the lateral capacity of a pile group being less than the sum of the lateral capacities of the individual piles comprising the group. Hence, laterally loaded pile groups have a group efficiency of less than 1. Based on experiments conducted as part of the FOREVER National Project (FOREVER, 2003) on horizontally loaded micropile groups, the following conclusions were drawn:

- For in-line micropiles, group effects are negligible for micropile spacing between 6 to 7 diameters; and
- For micropiles arranged in a row perpendicular to the direction of loading, group effects are negligible for micropile spacing just greater than 3 diameters.

The lateral capacity of an individual pile in a pile group is a function of its position in the group and the center to center pile spacing. Piles in trailing rows of pile groups have less resistance to a lateral load than pile sin the lead row, and therefore exhibit greater deflections. This is due to the pile-soil-pile interaction that takes place in a pile group. Brown et al. (1998) proposed a p-multiplier,  $P_m$ , be used to modify the p-y curve of an individual pile based upon the piles row position to account for this pile-soil-pile interaction. An illustration of the p-multiplier concept is presented in Figure 5-21. For piles in a given row, the same  $P_m$  value is applied to all p-y curves along the length of the pile. In a lateral load test of a 3 by 3 pile group in very dense sand with a center to center pile spacing of 3b, Brown found the leading row of piles had a  $P_m$  of 0.8 times that of an individual pile. The  $P_m$  values for the middle and back row of the group were 0.4 and 0.3, respectively.

A summary of additional laterally loaded driven pile group studies is provided in FHWA-NHI-05-042 (2005). Also, preliminary results from the FOREVER project indicate that P_m multipliers for micropiles may be slightly higher than those recommended herein, however, only limited data from centrifuge testing is available at this time.

Brown and Bollman (1993) proposed a p-multiplier procedure for the design of laterally loaded pile groups. This approach, outlined in the step by step procedure that follows, may be used for the design of laterally loaded micropile groups.

# 5.19.2 Step By Step Design Procedure For Laterally Loaded Pile Groups

<u>Step 1</u>: Develop p-y curves for single pile (see guidance for single pile previously provided)

# Step 2: Perform LPILE analyses

- a. Perform LPILE analyses using the  $P_{\rm m}$  values for each row position to develop load-deflection and load-moment data.
- b. Based on current data, it is suggested that  $P_m$  values of 0.8 be used for the lead row, 0.4 for the second row, and 0.3 for the third and subsequent rows. These recommendations are considered reasonable for center to center pile spacing of three pile diameters and pile deflections at the ground surface ranging from 10 to 15 percent of the micropile diameter. For larger center to center spacings or smaller deflections (as would be anticipated for typical micropile groups), these  $P_m$  values should be conservative.

c. Determine shear load (at the ground line) versus deflection behavior for piles in each row. Plot load versus pile head deflection results similar to as shown in Figure 5-22(a). This plot can be developed for each row by selecting a set of shear loads and using LPILE to evaluate the deflection for each shear load

# Step 3: Estimate group deflection under lateral load

- a. Average the load for a given deflection from all piles in the group to determine the average group response to a lateral load as shown in Figure 5-22(a).
- b. Divide the lateral load to be resisted by the pile group by the number of piles in the group to determine the average lateral load to be resisted by each pile. Enter load-deflection graph similar to Figure 5-22(a) with the average load per pile to estimate group deflection using the group average load deflection curve

# Step 4: Evaluate pile structural acceptability

- a. Plot the maximum bending moment determined from LPILE analyses versus deflection for each row of piles as illustrated in Figure 5-22(b).
- b. Use the estimated group deflection under the lateral load per pile to determine the maximum bending moment for an individual pile in each row. Evaluate structural capacity according to Eq. 5-3 or Eq. 5-6 where the  $M_{\text{max}}$  used in these equations is the maximum bending moment corresponding to the estimated group deflection.

<u>Step 5</u>: Perform refined pile group evaluation that considers superstructuresubstructure interaction.

A detailed example demonstrating this procedure for a driven pile group can be found in Appendix F.8 of FHWA-NHI-05-042 (2005). The steps are the same as would be used for a micropile group.

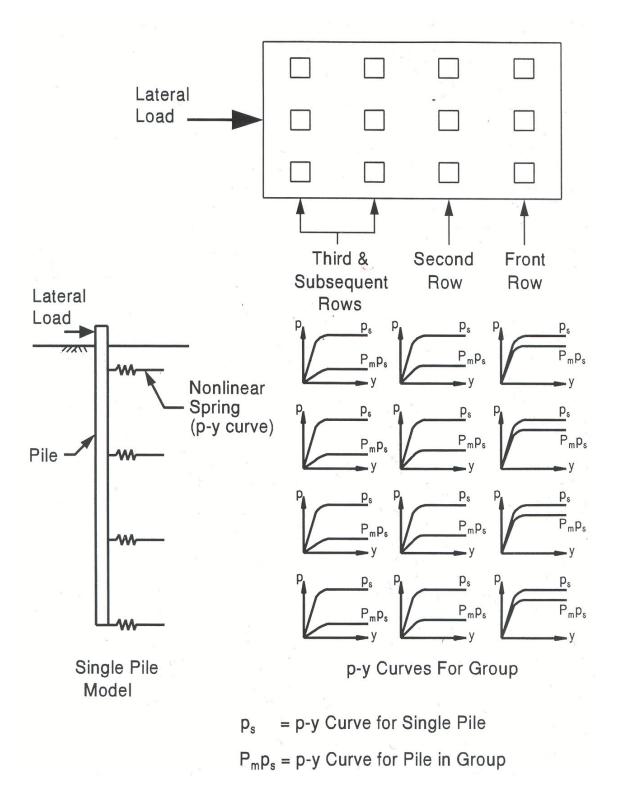


Figure 5-21. Illustration of P-Multiplier Concept for Lateral Group Analysis (after FHWA-NHI-05-042, 2005).

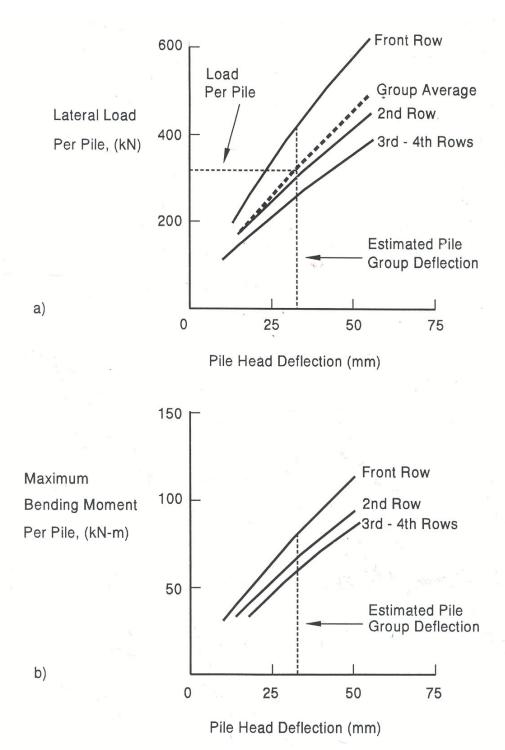


Figure 5-22. Load-Deflection and Bending Moment-Deflection for Pile Group Analysis (after FHWA-NHI-05-042, 2005).

## **5.19.3** Soil-Structure Interaction Analyses for Micropile Groups

The methods described above uses analyses of single micropiles as a means to evaluate lateral load response of micropile groups. Micropiles are often used in combination with existing deep foundation elements. Because of this, estimates on the amount of load that will be shared by each individual foundation element need to be made. In some cases, this may be a statically indeterminate problem (i.e., loads need to be carried by, for example, more than 2 piles in a given cross section) requiring that the stiffness of the foundation elements (both existing and new micropiles) and the pile cap be considered in the analysis.

The computer program FB-Pier (2001) was developed with FHWA support as the primary design tool for analysis of pile groups under axial and lateral loads. This program is a nonlinear, finite element analysis, soil-structure interaction program. FB-Pier uses a p-multiplier approach in the evaluation of laterally loaded pile groups under axial, lateral, and combined axial and lateral loads. Additional information on FB-Pier program capabilities can be found at <a href="http://bsi-web.ce.ufl.edu">http://bsi-web.ce.ufl.edu</a>. The computer program GROUP (2003) can also be used to model pile groups (see <a href="https://www.ensoftinc.com">www.ensoftinc.com</a>).

## 5.19.4 Battered Micropiles

The lateral load-carrying capacity of individual vertical micropiles is limited compared to more conventional drilled shafts and driven piles. As for other deep foundation systems, micropiles can be battered as a means to provide additional resistance to lateral loading. Note that since micropile drilling equipment is designed to drill both vertically and subvertically, there is not a significant increase in cost (on a per unit length basis) or quality of finished pile for battered micropiles as compared to vertical micropiles.

The calculation of lateral capacity of a single battered micropile is demonstrated in Sample Problem No. 1. The total lateral capacity of the battered micropiles is the sum of the lateral capacities of each battered micropile. This lateral capacity is compared to the lateral load applied to the foundation from the superstructure. If this sum is less than the lateral load applied to the foundation, the remaining load is carried by the micropiles in bending (i.e., this remaining load is used in a lateral load (i.e., LPILE analysis) for the structure).

Micropile groups with vertical and battered piles should be analyzed using the soil-structure interaction programs described in Section 5.19.3. Pile groups that contain battered piles are relatively stiff and will undergo less lateral movement for a given load than for a system with the same number of vertical piles. However, this increased system stiffness also results in greater bending moments in the pile cap which is a concern, especially for highly seismic

regions. Moreover, battered micropiles should not be used where the potential for ground settlement around the battered micropile is a possibility. These settlements will induce additional bending moments in the micropiles and some loss of support. Additional discussion on batter piles for seismic regions is discussed in Section 5.21.

#### 5.20 BUCKLING CONSIDERATIONS FOR MICROPILES

#### **5.21.1** General

Because micropiles are frequently installed to or into relatively sound rock or dense/hard soil, their capacity is frequently dictated by the structural strength of the element, rather than by the side resistance developed between the micropile grout and surrounding ground. The potential for buckling is reduced by the lateral restraint provided by the surrounding ground, however where soft or weak soils (e.g., very soft sedimentary deposits), voids (e.g., karstic formations), or liquefiable soils overly the bearing strata, buckling may potentially control the load-carrying capacity of a micropile and should be considered in design. For this reason, it is critical that the subsurface investigation identify these critical zones and, also, the depth of these zones should be recorded during the micropile installation process.

Herein, design analyses are presented to address micropile buckling. A more detailed coverage of micropile buckling is provided in Cadden and Gomez (2002).

## 5.21.2 Micropile Surrounded by Very Weak Or Liquefiable Soil

It is not possible to specifically define "very weak soil" or liquefiable soils by means of a readily available parameter such as SPT N value for purposes of evaluating buckling potential. Rather, a simple analysis is presented which uses a soil modulus parameter to evaluate whether buckling of the micropile is possible. The analysis involves comparing the critical buckling load for an axially loaded micropile,  $P_{cr}$ , to the maximum axial stress (i.e., capacity) of the micropile. For simplicity, only the contribution of the steel casing to resist buckling is considered, i.e., the potential benefits of grout within the casing and outside the casing are not considered as part of this analysis. Eq. 5-28 is used to estimate the critical buckling load:

$$P_{cr} = \frac{\pi^2 E I}{l^2} + \frac{E_s l^2}{\pi^2}$$
 (Eq. 5-28)

where:

E = modulus of elasticity of the steel casing (e.g., 200,000 MPa (29,000 ksi));

I = moment of inertia of the micropile (previously defined for a steel casing in Eq. 5- 4);

l = "unsupported" length of the micropile assumed to be the thickness of the relatively weak or potentially liquefiable soil; and

 $E_s$  = lateral reaction modulus of the soil surrounding the micropile over the "unsupported" length.

Using Eq. 5-28, the limiting lateral reaction soil modulus for buckling,  $E_s^{LIMIT}$  can be evaluated as:

$$E_s^{LIMIT} = \frac{1}{\left[\left(\frac{4I}{A^2}\right)\left(\frac{E}{F_y^2}\right)\right]}$$
 (Eq. 5-29)

The first of the two terms inside the brackets in Eq. 5-29 represents the geometric properties of the pile, while the second term represents its material properties. The combination of these two terms is referred to as the *pile factor* and is given in units of [stress⁻¹].

Using Eq. 5-29, if the  $E_s^{LIMIT}$  value is less than the measured or assumed soil modulus,  $E_s$ , then the geotechnical and structural strength of the micropile will control the micropile capacity and buckling does not need to be considered further. If the  $E_s^{LIMIT}$  value is greater than  $E_s$ , buckling should be evaluated further. Tables 5-12 and 5-13 provide ranges of  $E_s$  values for various soil types.

Figure 5-23 provides a summary chart of limiting lateral reaction modulus values for various micropile materials.

Table 5-12. Elastic Constants of Various Soils Based on Soil Type (modified after AASHTO, 2002).

Soil Type	Range of Equivalent Elastic Modulus,
	kPa (ksf)
Clay	
Soft sensitive	2,400 - 14,400 (50 - 300)
Medium stiff	14,400 - 48,000 (300 – 1,000)
Very stiff	48,000 - 96,000 (1,000 - 2,000)
Loess	14,400 - 57,500 (300 – 1,200)
Silt	1,900 - 19,000 (40 – 400)
Fine sand	
Loose	7,600 - 11,500 (160 – 240)
Medium dense	11,500 - 19,000 (240 – 400)
Dense	19,000 - 29,000 (400 – 600)
Sand	
Loose	9,600 - 29,000 (200 – 600)
Medium dense	29,000 - 96,000 (600 – 1,000)
Dense	96,000 - 76,000 (1,000 – 1,600)
Gravel	
Loose	29,000 - 76,000 (600 – 1,600)
Medium dense	76,000 - 96,000 (1,600 – 2,000)
Dense	96,000 - 192,000 (2,000 - 4,000)

Table 5-13. Elastic Constants of Various Soils Based on SPT N Value (modified after AASHTO, 2002).

Soil Type	Equivalent Elastic Modulus,
	kPa (ksf)
Silts, sandy silts, slightly	400 (N ₁ ) ₆₀ (8 (N ₁ ) ₆₀ )
cohesive mixtures	400 (11)60 (8 (11)60)
Clean fine to medium sands	700 (N ₁ ) ₆₀ (14 (N ₁ ) ₆₀ )
and slightly silty sands	700 (1\1)60 (14 (1\1)60)
Coarse sands and sands with	1,000 (NI) (20 (NI))
little gravel	$1,000 (N_1)_{60} (20 (N_1)_{60})$
Sandy gravels	1,200 (N ₁ ) ₆₀ (24 (N ₁ ) ₆₀ )

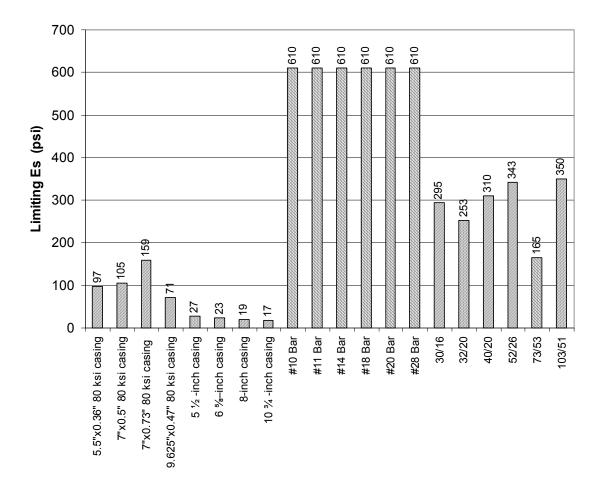


Figure 5-23. Limiting Lateral Modulus Values for Various Micropile Materials (after Cadden and Gomez, 2002).

If the analysis presented above indicates the potential for buckling (i.e.,  $E_s^{LIMIT} > E_s$ ), the allowable compression load for the cased section subject to buckling should be calculated. Eq. 5-1 can be modified to account for buckling as:

$$P_{c-allowable} = \left[0.4 f'_{c-grout} \times A_{grout} + 0.47 F_{y-steel} \left(A_{bar} + A_{ca \sin g}\right)\right] \times \frac{F_a}{0.47 F_{y-steel}}$$
(Eq. 5-30)

In Eq. 5-30, the allowable stress, F_a is calculated based on the following:

$$if \ 0 < \frac{Kl}{r_t} \le C_c, F_a = \frac{F_{y-steel}}{FS} \times \left[ 1 - \frac{\left(\frac{Kl}{r_t}\right)^2}{2C_c^2} \right]$$
 (Eq. 5-31)

if 
$$\frac{Kl}{r_t} > C_c$$
,  $F_a = \frac{\pi^2 E_{steel}}{FS[Kl/r_t]^2}$  (Eq. 5-32)

where 
$$C_c = \sqrt{\frac{2\pi^2 E_{steel}}{F_{y-steel}}}$$

K = effective length factor (assumed equal to 1.0 and previously defined in Section 5.6);

1 = unsupported length of the micropile;

 $r_t$  = radius of gyration of the steel section only =  $(I/A)^{1/2}$ ;

FS = factor of safety = 2.12 (see Table 10.32.1.A in AASHTO (2002)) and

 $F_{y-steel}$  = the casing yield stress.

For this analysis, the unsupported length of the micropile, l, is assumed to be the thickness of the weak soil surrounding the micropile and the effective length factor is conservatively assumed to be 1.0. Also, this analysis can be used to consider scour in which the depth of scour is assumed to be the unsupported length of the micropile.

Where combined axial and bending stresses are present and where buckling should be checked (based on the evaluations presented in this section), Eq. 5-3 should be used.

## **5.20.3** Micropiles Installed through Voids

Figure 5-24 illustrates the case of a micropile installed through a void such as for a micropile installed in karst terrain. The micropile is subject to a centered load P applied at the top, and penetrates consistent ground throughout its entire length, except at the void location.

The structural capacity of such a micropile should be checked using Eq. 5-30. Depending on the procedure followed for micropile installation, the portion of the pile through the void may be analyzed as a doubly pinned, pinned-fixed, or fixed-fixed column and k selected accordingly. The model in Figure 5-24 assumes that the pile has been grouted only along the bond length, and that an annular gap around the casing exists throughout its unbonded length. Under these conditions, the micropile can be conservatively assumed to be pinned on both ends such that k = 1.0.

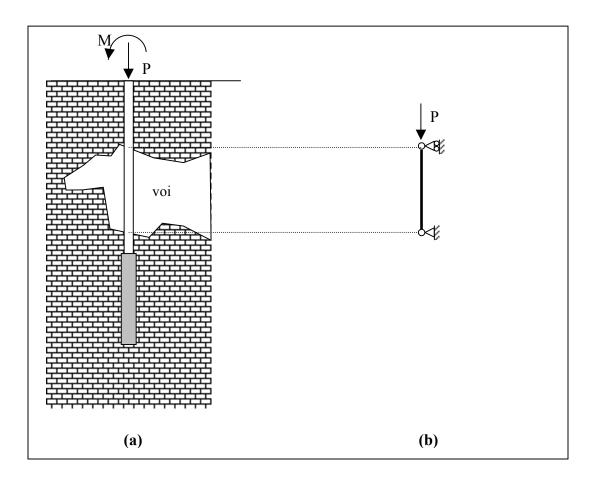


Figure 5-24. Micropile Installed Through Voids in Karstic Terrain; (a) Actual Configuration, (b) Model Used for Estimation of Structural Capacity (after Cadden and Gomez, 2002).

In cases where the pile extends through hard rock above the void, consideration should be given to the effect this may have on the ability of lateral loads or moments to transfer to the portion of the pile within the void. If the pile is fixed in a rock layer above a void, then there will not be any lateral load that is transferred to portion of micropile over the length of the void; only vertical load is transferred over that length. The calculated allowable load assuming lateral load is transferred over the length of the void is therefore conservative for this case.

Micropiles may be susceptible to buckling-induced failure at the casing joints. To consider the effect of joints, Eq. 5-29 is used to evaluate the critical or limiting lateral soil reaction using a reduced value for the moment of inertia. This value for I is calculated as for I_{joint} in Eq. 5-26. It is noted that this method is conservative since it assumes that the micropile stiffness is equivalent to that of the joint over the entire length of the unsupported micropile. More detailed structural analyses could be carried out that only use the reduced casing stiffness over the length of the joint, however, these are relatively complex and beyond the scope of this report. As a practical consideration, however, micropiles installed through karst must be designed for buckling, considering the presence of the casing joints, or should include installation of continuous internal reinforcement along portions of micropile traversing voids or very soft or loose soil.

#### 5.21 SEISMIC CONSIDERATIONS

#### 5.21.1 General

Micropiles have been used for seismic retrofit projects in which existing deep foundations have been shown to have insufficient capacity to resist seismic forces consistent with the design earthquake. As discussed in Chapter 3, seismic retrofit projects typically involve adding micropiles to an existing foundation to provide additional capacity required to withstand seismic effects (i.e., overturning, uplift, lateral forces). Current guidance for seismic design of bridge foundations is provided in Division I-A of AASHTO (2002) and the recommendations provided here apply generally to micropiles subject to seismic effects. Additional information on seismic design of micropiles is found in JPWRI (2002)

As shown in Figure 5-25, the seismic response of a pile foundation involves the distribution of a set of superstructure loads into the surrounding soil mass through the pile members. The general case involves consideration of three components of translational forces (an axial and two lateral shear forces) and three components of rotational moments (a torsional moment about the pile axis and two rotational moments about two orthogonal horizontal axes) along the pile member.

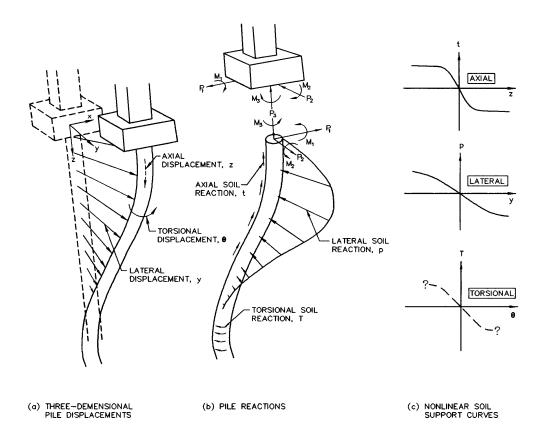


Figure 5-25. Three-dimensional Soil Pile Interaction (after Bryant and Matlock, 1977).

The evaluation of the dynamic response of a pile foundation can be performed using either a pseudo-static analysis or a dynamic response analysis. A realistic approach to dynamic analysis of pile foundations should account for the nonlinear behavior of near-surface soils and the layered nature of typical soil profiles. In view of these constraints, current design practice usually models the soil support characteristics along the pile by discrete nonlinear springs. The pile is modeled as a beam-column supported by one set of lateral springs (using p-y curves as previously discussed) and another set of axial springs. The curves for the axial load transfer characteristics of the pile are referred to as *t-z curves*. Torsional resistance against rotation of individual piles is usually ignored or assumed to be negligible for highway bridges, as most deep highway foundations are supported by pile groups and torsional loads on pile groups become resolved as lateral loads on the individual piles.

For evaluating the vertical response of piles subject to dynamic loading, t-z curves are generally calculated over the entire length of the pile. Procedures for evaluating t-z curves are provided by Lam and Martin (1986, 1997) and Kraft et al. (1981a, b).

# 5.21.2 Use of Battered Micropiles in Highly Seismic Regions

Vertical micropiles in groups do little to resist horizontal seismic deformations due to their relatively low stiffness (FOREVER, 2003). Under seismic loading, however, battered micropiles will have a reduced positive bending moment (as compared to vertical micropiles), but significantly higher negative bending moments at the pile head. In current U.S. practice, the concern over excessive bending moments being mobilized during the design seismic event has resulted in some owner agencies disallowing the use of battered piles for seismic retrofit projects.

Trinh et al. (2004) performed finite element analyses to investigate the effects of combined axial compression and lateral displacements on battered micropiles. The micropile foundation consisted of a square column supported on a 4572 mm by 4572 mm (180 in. by 180 in.) 915-mm (36-in.) high pile cap. Twelve, 178-mm (7-in.) diameter micropiles arranged in the configuration shown in Figure 5-26 were used to support the pile cap. Micropiles were battered inward at 15 degrees and outward at 25 degrees from the vertical.

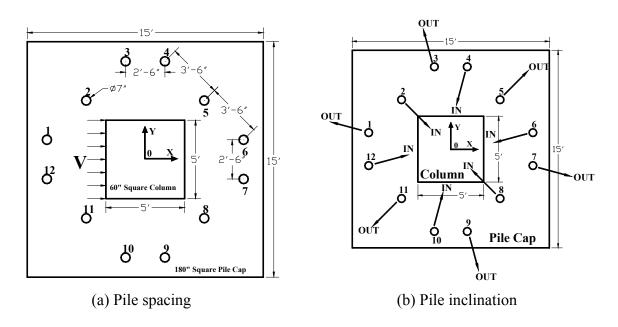


Figure 5-26. Plan View of the Micropile Foundation (after Trinh et al., 2004).

They concluded that with an adequate amount of flexural reinforcement in the pile cap, the failure mode of the micropile foundation will primarily involve yielding of the micropiles or pullout of the micropile itself with little (if any) yielding of the micropile-footing connection. Figure 5-27 shows the effect of increasing steel reinforcement in the cap. This figure indicates that a fully ductile response of the foundation can be achieved with a flexural

reinforcement ratio,  $\rho_s$  (equal to area of flexural steel reinforcement to cross section area) of about 0.5 percent. Ductility implies that the foundation does not undergo significant loss of lateral support at large lateral displacements and/or where the ratio of ultimate deformation to deformation at yield is relatively large. If the micropile-footing connection were to incur higher than expected loading, the connection is expected to perform in a highly ductile manner and the potential failure mechanism would be either pullout of the micropile or yielding of the micropile.

## 5.21.3 Load Sharing with Existing Foundations

Applications in which micropiles are used to seismically retrofit an existing deep foundation requires that load sharing between existing foundation elements and the micropiles be evaluated. Where additional foundation elements are required to support additional compression and uplift forces (e.g., rocking motions), vertical micropiles are used.

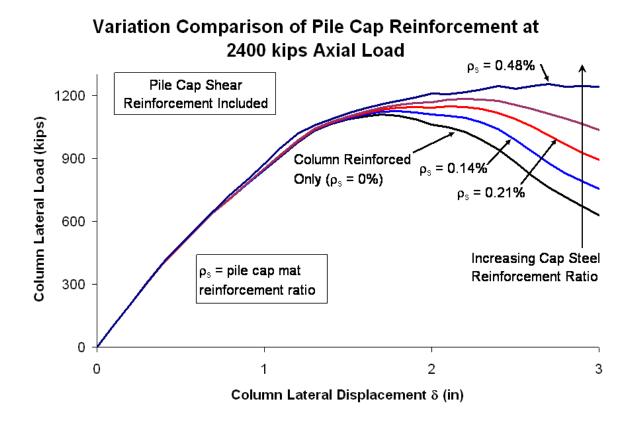


Figure 5-27. Lateral Response of Micropile Foundation for Different Flexural Reinforcement Ratio (after Trinh et al., 2004).

For the retrofit design of an old or deteriorated foundation or for a foundation in which the original structural design details and specifications are uncertain, design seismic loads should be assumed to be carried by the micropiles only. Load sharing between existing and new foundations should only be considered if sufficient information on the existing foundation system (i.e., as-built drawings, load test results, design calculations) is available. Where this is considered, soil-structure interaction analyses will need to be performed.

# **5.21.4** Pile Uplift Capacity

Individual piles in pile groups will be subjected to significant uplift resulting from seismic loading. The overturning moment applied by the seismic lateral force to the pile cap is typically resisted by axial resistance in the piles with the outermost piles in the group being subjected to relatively large cyclic axial loads.

Section 6.4.2(B) of AASHTO (2002) Division I-A suggests that some separation between the bottom of the pile cap and the foundation soil is allowed, provided that the foundation soil is not susceptible to loss of strength (e.g., liquefaction) under the imposed cyclic loading. For pile groups, up to one-half the bearing area of the pile cap is allowed. In Section 6.4.2(C), AASHTO recommends that the ultimate capacity of the piles be used in designing the foundation for uplift forces resulting from seismic forces (i.e., FS = 1.0 on geotechnical uplift capacity). It is noted that all other permanent loads are included in this assessment. Structural requirements including embedment length of the pile in the pile cap and the detailing of the connections need to be considered, as discussed below.

As part of the Trinh et al (2004) study, battered micropiles on the outboard side of the pile cap were shown to develop large tensile forces and relatively severe cracking even though the foundation was subject to large vertical compression forces. They concluded that a prudent design approach would include increasing the amount of vertical shear reinforcement (i.e., placing steel reinforcement at closer spacing) in the cap near the piles that are furthest from the column (i.e., the outboard piles) to mitigate cracking of the cap concrete.

# 5.21.5 Liquefaction

In many earthquakes where liquefaction occurs, the soil may not liquefy until the end of the earthquake. Therefore, piles in liquefied ground may still be able to rely on the vertical and lateral support of the soil in the potentially liquefied zone during the earthquake. However, due to uncertainties as to exactly when liquefaction will occur, it is common practice to assign a reduced vertical and lateral resistance to potentially liquefiable soil surrounding a pile if the pile is expected to function as a load carrying member during and after an earthquake. Results presented by Ishihara and Cubrinovski (1998) suggest that the lateral

resistance of a pile in liquefied ground is approximately 0.1 to 1.0 percent of the lateral resistance in non-liquefied ground. Therefore, if a pile foundation in potentially liquefiable soil is expected to carry lateral loads after the surrounding soil liquefies, batter piles may be required to provide adequate lateral support. This reduction in lateral support is particularly important for relatively flexible micropiles.

Studies reported in the FOREVER (2003) project showed that vertical micropiles were not effective in reducing liquefaction. Batter micropiles, however, were shown to limit seismically-induced soil movements (and pore pressure buildup) resulting in no liquefaction in the zone affected by the piles, whereas the free-field soil did undergo liquefaction. If batter piles are used, the pile cap connections should be designed to sustain moment loads induced by lateral movements and the batter piles should be designed to sustain lateral loads due to soil settlement.

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# CHAPTER 6 DESIGN OF MICROPILES FOR SOIL SLOPE STABILIZATION

## 6.1 INTRODUCTION

In addition to structural foundation support, micropiles are also used for structural slope stabilization. In this application, micropiles are designed to provide the required restraining forces to stabilize a slope using one of two approaches:

Approach 1: Battered micropiles are installed through the unstable slope to a specific depth below the potential slip surface. In this approach, micropiles are affixed at the ground surface to a concrete cap beam (see Figure 6-1). With this method, the individual micropiles provide resisting forces through the mobilization of axial, shear, and bending resistance. The spacing of the micropiles along the slope length is evaluated by considering the number of micropiles necessary (per lineal meter) to provide the minimum required stabilizing force. The minimum required stabilizing force is typically that force required to increase the stability of the slope to a prescribed minimum factor of safety.

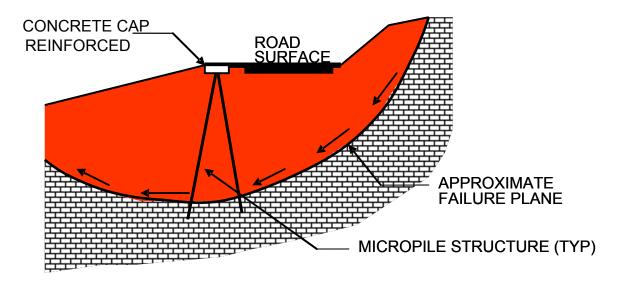


Figure 6-1. Micropile System in Approach 1.

Approach 2: Micropiles are installed similarly as for Approach 1, except many more micropiles are used (see Figure 6-2). In this case, micropiles are placed sufficiently close to each other to create a coherent structure of micropiles and soil. This structure is assumed to behave much like a gravity retaining wall in that the required restraining force necessary to stabilize a slope is achieved by sliding resistance developed along the bottom of the micropile group. For this reason, individual micropiles are subject to relatively small loads. The group enscribes and internally reinforces the soil mass so it acts as a unit.

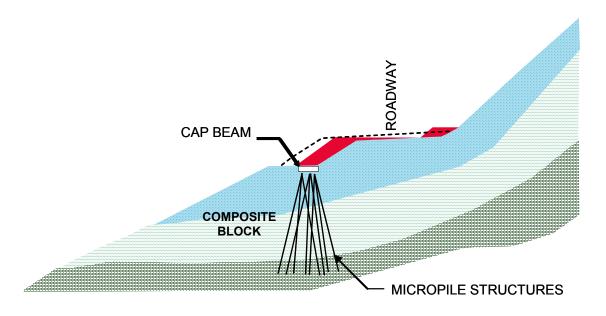


Figure 6-2. Micropile System in Approach 2.

In this chapter, a step-by-step design method for micropiles based on Approach 1 is presented (see Table 6-1). Also, Section 6.9 presents three case histories wherein Approach 1 was used.

A step-by-step design method for micropile groups based on Approach 2, however, cannot be developed at this time since limited data is available to confirm a specific design method and since the Approach 2 micropile system has limited applicability in current US practice. Design concepts for micropile groups using Approach 2 are provided in Appendix A.

Table 6-1. Design Steps for Micropiles for Soil Slope Stabilization.

- 1. Identify project specific constraints and evaluate feasibility
- 2. Identify performance requirements
- 3. Review available information and geotechnical data
- 4. Evaluate factor of safety of existing slope
- 5. Determine additional force required to obtain target factor of safety
  - choose a location for the single vertical micropile within the existing slope
  - model restraining force (micropile) and perform slope stability analysis
  - evaluate the stability of the slope away from micropile
- 6. Select micropile cross section
- 7. Estimate length of micropile
- 8. Evaluate bending moment capacity of single vertical micropile
- 9. Evaluate shear capacity of single vertical micropile
- 10. Evaluate shear capacity of battered micropile group
  - select batter angle for upslope and downslope micropile
  - determine maximum shear capacity of a single battered micropile
  - determine maximum shear capacity of battered micropile group
- 11. Calculate spacing required to provide required force to stabilize the slope
- 12. Check potential for soil flow between micropiles
- 13. Perform structural design of concrete cap beam

# 6.2 STEP 1: IDENTIFY PROJECT SPECIFIC CONSTRAINTS AND EVALUATE MICROPILE FEASIBILITY

Slope stabilization projects in which micoropiles may be feasible are usually located in remote areas or where difficult site access is a concern. Other project constraints common to slope stabilization include:

- (1) space restrictions that may include limited ROW, availability of on-site storage for construction materials, limited access for construction equipment, and restrictions on traffic disruption;
- (2) interference with above-ground utilities and nearby structures;
- (3) performing work on an unstable slope (i.e., need to perform any cut/fill operations in a controlled manner, potential for excess seepage in and around the work area, soil and/or rock fall hazards, etc.);
- (4) environmental concerns that may include local policies concerning construction noise, vibration, transportation of material to the site, and protection of animals and plants;

- (5) landscape aesthetics such as sensitivity to scars created by access road cuts or excavations;
- (6) disposal of rock or soil that is excavated as part of the slope stabilization method; and
- (7) cost of project.

In assessing the use of micropiles as a means to stabilize a slope, micropiles will most often be compared to other structural slope stabilization measures such as ground anchors, soil nail walls, or driven pile or drilled shafts.

The use of micropiles has come into favor for slope stabilization projects because micropile construction is relatively simple and requires a small work area, and micropiles can be readily installed in areas with limited equipment access, such as for landslides located in hilly, steep, or mountainous areas. However, the implementation of these systems still requires a specialty geotechnical contractor. The other advantages offered by micropiles include, reduced excavation compared to earth retaining systems (i.e., the system is constructed from the top-down, no excavation is required to construct a wall or install anchor supports); improved aesthetics in that the system is completely buried so that there is no visual evidence of an active structural stabilization system; and micropiles can be installed in virtually any ground type. This latter advantage is important for landslide stabilization since, in many cases, an upper competent layer is underlain by soft, wet soil material (comprising the location where landslide movements are occurring) resting on rock. The upper layer may comprise colluvium or talus materials which are known to contain a wide range of soil and rock particle sizes through which installation of driven piles or drilled shafts would be difficult and costly.

The cost-effective use of micropiles will be based on the required forces necessary to stabilize a slope. For example, projects which involve a relatively long landslide (i.e., large failure surface length) or where the depth to the potential slip surface is large, may not be well-suited for micropiles because of the very large restraining forces required to stabilize the slope. It is noted, however, that micropiles can be designed to withstand relatively large loads by battering the micropiles to mobilize axial restraint forces. In some cases, even with battered micropiles, the required loads to be resisted are so large that additional restraint, usually from ground anchors, is required.

For first-order comparisons, micropiles for slope stabilization range in cost from \$4,000 to \$11,000 per lineal meter of slope (\$1,200 to \$3,400 per lineal ft of slope). The higher end of the range being for projects involving relatively long micropiles (e.g., in excess of 15 m (50 ft) to reach the top of the slide surface) and where access and other project-specific constraints result in relatively low micropile installation production rates (e.g., less than 90 m (300 ft) per day) and the need for large amounts of rock drilling.

Previous designs and contractor experience indicates that micropiles for slope stabilization will likely only be cost-effective if unbalanced slope forces can be resisted through the placement of a micropile structure at approximately the mid-height of the slope. Design calculations for locating the position of micropiles on a slope is described in this chapter. If a slope stabilization measure would be required to minimize, for example, future downward movements of a roadway near the top of the unstable slope, then a single micropile structure would likely not be sufficient to stabilize the slope since it is possible that the slope would be unstable in front of the micropile structure. In some cases, however, multiple micropile structures could be used but may not be cost effective.

The design method described herein for micropiles is based on the assumption that the portion of the micropiles below the potential slip surface "tie" the slope mass above the potential slip surface to the more competent ground below the potential slip surface. In this sense, the micropiles serve as dowels. Also, the design assumes that concentrated deformations occur at the location of the potential slip surface. With this assumption, maximum bending moments and shears in the micropiles occur near the location of the potential slip surface. Design engineers considering the use of micropiles for a slope stabilization project must review available instrumentation data on slope movements. The design method presented herein requires that movements are occurring at a well-defined critical potential slip surface. As an example, Figure 6-3 shows concentrated lateral soil movements at approximately a depth of 8 m (25 ft). These data are from a landslide in Summit County, Ohio. Where slope movements are less localized, or where more than one potential slip surface may exist (i.e., where a single, well-defined slip surface has not been observed (via instrumentation) or expected (via review of subsurface information)), other slope stabilization measures such as anchored walls should be considered.

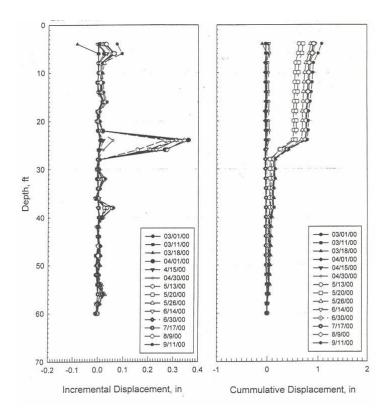


Figure 6-3. Concentrated Movements Recorded from Inclinometer at the Slip Surface (after Liang, 2000).

# 6.3 STEP 2: IDENTIFY PERFORMANCE REQUIREMENTS

The primary performance requirement for a slope stabilization project is for the stabilized slope to meet or exceed a target slope stability factor of safety with respect to static and seismic slope stability. Typical static factors of safety range from 1.3 to 1.5 depending on, for example, whether other structures are supported by the slope and whether only limited geotechnical data is available. For seismic slope stability analyses (based on pseudo-static analysis), a target value of 1.1 is typically used.

Other performance (and/or design) requirements will include:

- prescribed level of corrosion protection for the micropiles;
- permissible variation in groundwater levels during construction;
- maximum loads that can be carried (as part of load testing); and
- allowable stresses for steel and concrete.

It is noted that design of earth slopes (and stabilization of slopes) is not codified in, for example, AASHTO (2002). Design criteria for slopes are typically developed on a project-specific basis.

# 6.4 STEP 3: REVIEW AVAILABLE INFORMATION AND GEOTECHNICAL DATA

The existing slope conditions should be assessed by review of available information and collection of geotechnical data through a focused subsurface exploration and laboratory testing program. For guidance regarding the planning and execution of subsurface exploration programs for slopes, refer to the Manual on Subsurface Investigations (Mayne et al., 2001) and Geotechnical Engineering Circular (GEC) No. 5 "Evaluation of Soil and Rock Properties" (Sabatini et al., 2002).

The information gathering, subsurface exploration and laboratory testing program should be developed with the goal of obtaining the following information:

<u>Topography of the area.</u> Topographic information for the area of interest is used to develop analysis cross sections for slope stability analysis. If relatively recent topographic maps are not available for the site or if it is known that site topography has been modified since the last ground survey was performed, a ground surface survey of the area should be performed since accurate information on slope geometry is critical for analysis.

Lateral extent of the landslide or potential landslide area. This information can be obtained through observations from a site inspection and through review of aerial photographs (if available). The lateral extent of the area to be stabilized needs to be known to enable potential slip surfaces with the lowest factor of safety to be identified. Usually, multiple parallel cross sections are analyzed using 2-dimensional limit equilibrium methods to determine the slip surface with the minimum slope stability factor of safety. This cross section is used to perform design analyses of the slope.

<u>Subsurface profile and groundwater conditions.</u> The subsurface profile at the location of the critical cross section is developed based on information from historical borings and from borings advanced as part of the slope stabilization project. This exercise is carried out similarly as for other geotechnical features where the development of a subsurface profile is required. Specifically, for slopes stabilized with micropiles, borings should be advanced into the competent materials below the potential slip surface which will serve as the resistance zone for the micropile.

Groundwater conditions within the slope may be determined from the logs of soil borings, piezometer data, and observation wells. This information is used to model pore pressure conditions within the slope. It is specifically noted that the cause of slope movements is oftentimes related to large precipitation events which cause groundwater levels and pore pressures to increase in a slope mass. Where the conditions of the slope at the time of instability are required for analyses (e.g., where back analysis to obtain strength properties is required), it is necessary to develop pore pressure conditions at the time of the slope instability.

The assessment of design groundwater levels (or design pore pressures) should consider the effect that the micropile structure will have on long-term groundwater levels within the slope. Typically, however, the spacing between micropiles is sufficiently large such that the possibility of pore pressure buildup (resulting from a potential hydraulic cutoff effect from the micropile structure) is relatively insignificant. Where project conditions require close micropile spacing and/or where the potential for significant groundwater recharge to the slope area is possible, the Owner should require that seepage analyses be performed that consider the effects of micropile spacing, micropile installation methods (e.g., effect of possible grout travel), precipitation events, and hydraulic conductivity of the slope material. Subsurface drainage systems may be required and/or the proposed micropile system may be designed to resist long-term seepage pressures.

The importance of an accurate assessment of pore pressure conditions within a slope cannot be overemphasized.

<u>Soil and rock parameters for analysis.</u> Material parameters for soil and rock are required for slope stability analyses and for the evaluation of the structural capacity of micropiles (using p-y analyses discussed subsequently). Material parameters required include soil and rock unit weights and shear strength parameters.

Depending on the soil type and access to sampling locations in the slope area, soil and rock sampling may be difficult and obtaining nominally undisturbed soil samples for strength testing may be impossible. In these situations, it is prudent to collect as much index type data as possible (i.e., Atterberg limits, grain size analysis, and moisture content) to establish differences between soil and rock stratum. Based on these data, strength properties would be determined from engineering correlations. Common engineering correlations for soil and rock properties that may be used for micropile slope stabilization assessment are provided in GEC No. 5 (Sabatini et al., 2002).

The use of these and other correlations for geotechnical parameters should be considered primarily for use in preliminary design evaluations and not as a substitute for a comprehensive site investigation, sample collection, and laboratory testing program.

<u>Critical slip surface</u>. Information on the location of the critical slip surface may be obtained from several sources during initial data review. In some cases, especially if the slope has been subject to previous movements, inclinometer data may be available which can be used to locate the critical slip surface. Also, boring logs and other stratigraphic information can be used to locate a potential slip surface. Oftentimes the critical slip surface will be located at the interface just above a competent soil or rock surface where water may be perched. This area becomes saturated and soft and slope movements may be concentrated at this location.

For micropile design, in addition to the requisite slope stability analyses, the location of the critical slip surface is required for laterally loaded pile analyses. As previously introduced, the location of the critical potential slip surface (as determined from slope stability analysis and/or field observations) is used as the location where maximum lateral micropile movement is assumed to occur

<u>Site Seismicity.</u> As for any other slope, destabilizing forces resulting from seismically-induced ground accelerations need to be considered. This evaluation for slopes is typically performed using a pseudo-static slope stability analysis (see Kavazanjian et al. 1997).

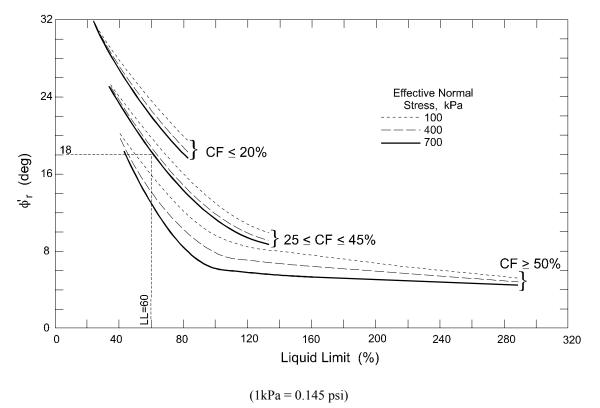
### 6.5 STEP 4: EVALUATE FACTOR OF SAFETY OF EXISTING SLOPE

Using the information from Step 3, slope stability analysis methods are used to evaluate the slope stability factor of safety for the slope that is to be stabilized. Presumably, this slope is at a slope stability factor of safety of approximately 1.0 (if the slope has undergone significant movements) or may be at a slightly higher factor of safety. From this evaluation, the minimum factor of safety ( $FS_{min}$ ) is evaluated. As a result of the analysis, the location of the critical potential slip surface is evaluated.

Analyses are typically performed for the static and seismic case and the results are compared to the target minimum factor of safety (previously discussed). In performing these analyses, estimates of shear strength, subsurface stratigraphy, and pore pressures within the slope mass are developed. A special case includes one in which the slope is known to have failed or have undergone significant downslope movement. By definition, this slope is at a FS = 1.0 at the time of the failure. Micropiles for slope stabilization have been used most commonly with applications involving slope failures (i.e., landslides). The technique used to adjust

shear strength parameters for this case is termed "back-analyses". Back-analysis techniques involve the following steps:

i. Estimate analysis parameters. If the slope has moved sufficiently, the residual drained friction angle may be used (e.g., c' = 0,  $\phi' = \phi'_r$ ) to model the soil material where these movements have occurred. Figure 6-4 may be used to evaluate  $\phi'_r$ . The use of Atterberg limits data and clay content can be used to assess residual (or large-displacement) drained friction angle for clayey landslide material (see Figure 6-4). For example, based on Figure 6-4, for a landslide material with clay content between 25 and 45 percent and with liquid limit of 60, the residual friction angle is 18 degrees.



Note:  $\phi'_r$  = Residual friction angle and CF = Percent clay-particles < 0.002 mm (0.00008 in)

Figure 6-4. Residual Friction Angle for Clayey Soils (after Stark and Eid, 1994).

The shear strength parameters estimated are considered as trial strengths ( $\phi_{trial}$  and  $c_{trial}$ ) in the back-analysis. Representative shear strength parameters for other soil and rock materials (i.e., those above and below soils near the critical potential slip surface) are evaluated based on available information and are usually not adjusted as part of the back analysis.

- ii. <u>Perform slope stability analysis</u>. Limit equilibrium slope stability analysis is performed to obtain the factor of safety that corresponds to trial strengths. Slope stability analyses are performed for several analysis cross sections. The best available information for pore pressure values, shear strength, stratigraphy, and topography at the time of the failure is used in the analyses. Also, the location of the failure surface needs to be known with some level of certainty so that analysis results can be compared to actual conditions.
- iii. Adjustment of parameters until FS = 1.00. If the previous slope stability analyses do not yield FS=1.00, shear strength parameters should be modified and analyses performed. This process is continued until shear strength parameters result in a corresponding FS = 1.00 result. It is important to note that shear strength represents only one of the unknowns in the analysis. Pore pressures and location of the critical failure surface (at the time of failure) need to be understood and hence their potential uncertainty should also be considered when varying parameters. A back analysis that produces FS = 1.00, but includes a calculated critical failure surface that is not consistent with that observed in the field should not be relied upon. All relevant parameters need to be consistent with observed results.

For the case where the existing slope may have a factor of safety greater than 1.0, but where the factor of safety is less than a target value, shear strengths and groundwater elevations should be evaluated as described in Design Step 3. In these cases, the location of the critical slip surface needs to be estimated based on available data. Slope stability analyses to evaluate  $FS_{min}$  should be performed considering circular and planar slip surfaces. Subsurface stratigraphy information should be used to evaluate the reasonableness of the calculated potential slip surface.

# 6.6 DESIGN CONCEPTS FOR MICROPILES USED FOR SLOPE STABILIZATION

#### 6.6.1 Overview

At this stage in the design process, an existing slope has been shown to be either unstable or marginally stable with a calculated slope stability factor of safety less than a target value. The remaining steps of the design process comprise designing a micropile system to improve or otherwise stabilize the slope.

The steps specific to the geotechnical and structural design of micropiles used for slopes is outside the typical design practice for most geotechnical engineers. For this reason, this

section provides background information on load transfer mechanisms and analysis methods used for Design Steps 5 through 13. The complete design of a micropile stabilized slope is demonstrated in Section 6.7.

### 6.6.2 Evaluating the Additional Force Required to Obtain Target Factor of Safety

Micropiles used for slopes are designed to prevent downward movement of the slope mass above the potential slip surface. The micropiles must be capable of providing the force required to stabilize the slope. This force is the force required to increase the factor of safety of the slope from an existing value to a target value.

Slope stability analysis programs are used to determine this additional force ( $H_{req}$ ). The slope stability analyses are performed in three stages: (1) a location is chosen for the micropiles; (2) the micropiles are modeled explicitly in the slope stability analysis to determine the required restraining force; and (3) the stability of the slope away from the micropile is evaluated by performing additional slope stability analysis.

### 6.6.2.1 <u>Micropile Location Within Slope Cross Section</u>

The magnitude of  $H_{req}$  will vary depending on the location of the micropile within the slope. This affect is demonstrated using the example slope geometry provided in Figure 6-5.

Several analyses were performed in which the location of a single micropile was adjusted within the cross section. At each location, the shear force provided by the micropile was increased until a target factor of safety ( $FS_{min}$ ) of 1.3 was achieved for the slope. The results of the analyses are shown in Figure 6-6 and these results indicate that, for this example, if the micropile is placed at or near the toe of the slope or at or near the crest of the slope, the use of a micropile structure at these locations would be ineffective. In other words, regardless of the magnitude of force that the micropiles could develop, the target factor of safety (i.e.,  $FS_{min} = 1.3$ ) could never be achieved (see Figures 6-7 and 6-8 for the most critical slip surface).

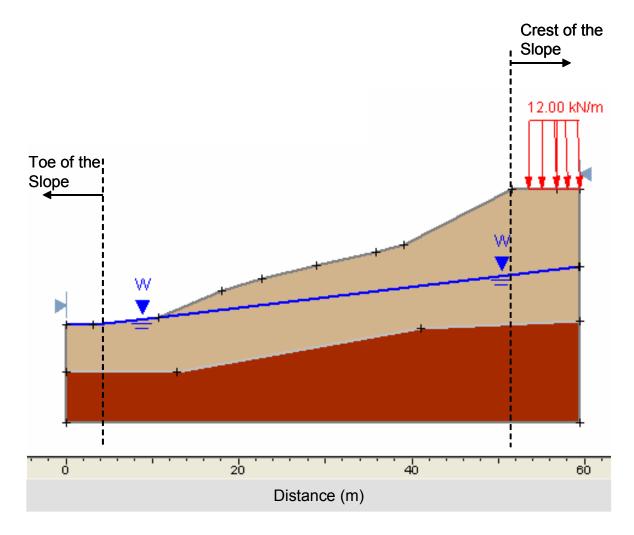
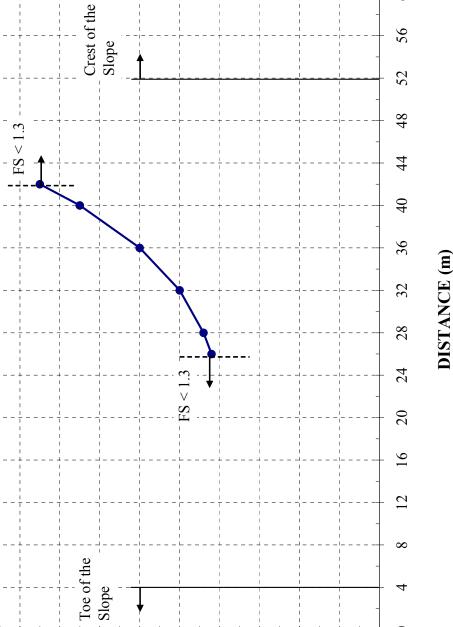


Figure 6-5. Example Slope Geometry.



EORCE REQUIRED FOR FS = 1.3 (kV/m)

Note: 1 m = 3.28 ft and 1 kN/m = 68.53 lb/ft

Figure 6-6. Relationship between Force Required For FS = 1.3 and Location of the Micropile.

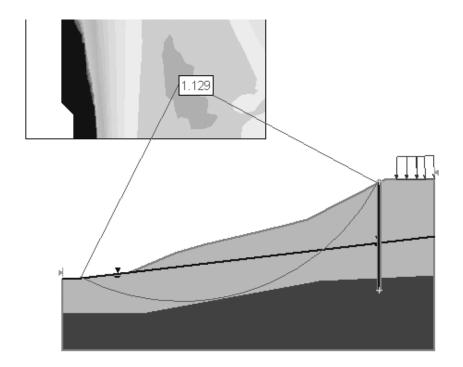


Figure 6-7. Effect of Micropile Placed Too Far Upslope ( $FS_{min} < 1.3$ ).

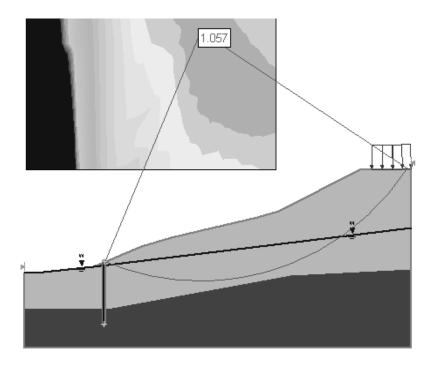


Figure 6-8. Effect of Micropile Placed Too Far Downslope (FS_{min}  $\leq$  1.3).

The results of the above example indicate that the maximum benefits from micropiles correspond to a micropile structure placed in the vicinity of the middle of the slope.

#### 6.6.2.2 Methods to Model Resisting Force from a Micropile

While it is recognized that micropile structures for slope stabilization will typically include a battered upslope "leg" and a battered downslope "leg" connected at the ground surface via a concrete beam (Figure 6-9), the micropile structure is modeled considering a single vertical micropile from the ground surface (at the design cap beam location) to a sufficient depth into a competent layer (see Figure 6-10). In subsequent design steps, the shear capacity, inclination, and the number of micropiles required to resist  $H_{req}$  is evaluated.

Slope stability input files generated in Design Step 4 are typically modified in one of two ways to model the effects of a single vertical micropile, as described below.

- Approach 1: The shear resistance provided by the single vertical micropile, H_{req}, can be modeled as a relatively large cohesive shear strength assigned to the soil layer where the micropile crosses the potential slip surface. By selecting a width of say 0.5 m, the slope stability analysis program will develop a single slice with a width of 0.5 m having the relatively large cohesive shear strength. The relationship between H_{req} and cohesive strength is shown in Figure 6-11 for this approach. It should be noted H_{req} is oriented at the same angle as the bottom of the slice. Repeat the slope stability analyses and change the cohesive strength until a factor of safety equal to the target value is obtained.
- Approach 2: Some slope stability software packages enable the user to directly input a micropile restraining force at any given location. With this approach, it is not necessary to indirectly obtain the restraining force via the introduction of a thin soil layer with a relatively large cohesive strength. Repeat the slope stability analyses and change the value for the restraining force until a factor of safety equal to the target value is obtained.

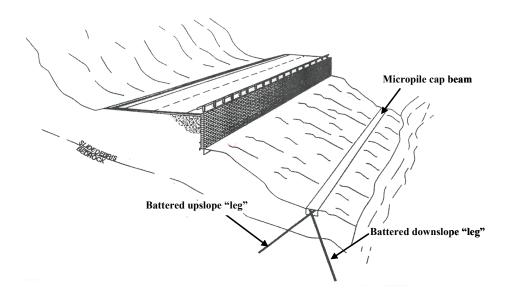


Figure 6-9. Micropiles with Battered Uplsope Leg and Battered Downslope Leg (modified after Hasenkamp, 1999).

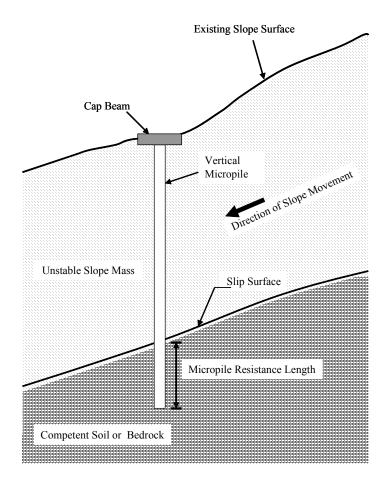
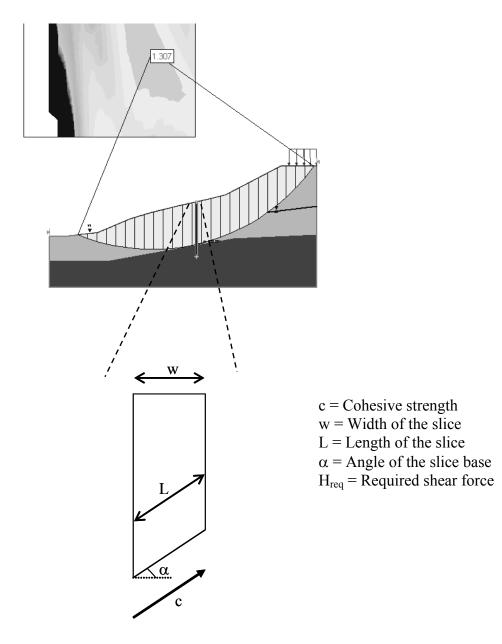


Figure 6-10. Single Vertical Micropile Model for Design Analyses.



$$H_{\text{req}} = c \times L$$

$$H_{req} = c \times w \times \frac{1}{\cos \alpha}$$

Figure 6-11. Relationship Between  $H_{req}$  and Cohesive Strength for Micropile Analysis Model.

### 6.6.2.3 Evaluating Slope Stability Away From Micropile

Results of the previous slope stability analysis provide the location and the required restraining force for the slope to achieve the target factor of safety. However, it is possible that slip surfaces away from the micropile may have factor of safety values less than the target value and therefore, additional slope stability analyses should be performed. For these analyses, the presence of the micropile is ignored by setting the search limits for potential slip surfaces located entirely upslope of the micropile and for potential slip surface located entirely downslope of the micropile (see Figure 6-12).

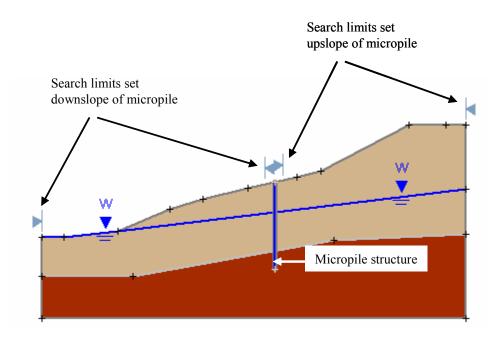


Figure 6-12. Slope Stability Analysis Search Limits Away From Micropile Location.

Specific practical issues are associated with the evaluation of downslope stability (as for Figure 6-13). If, for example, a roadway is located at the toe of the slope, then it is possible that future roadway widening would require excavation at the toe of the slope. Excavation near the toe of the slope may also be associated with certain long-term slope maintenance activities. For many earth retaining structures used to stabilize slopes, the resistance provided by soil in front of the wall (i.e., passive soil resistance) is conservatively neglected because of the possibility that this material would be removed at a later date. This design assumption can be adequately addressed with many earth retaining systems. For micropiles, it is explicitly noted that the assumption of zero passive soil resistance in front of the micropile is not considered using the design method presented herein. If slope material in front of the micropile were to move away from the structure as a result of instability or if soil

were removed as part of a maintenance activity, it is likely that the micropile structure would experience excessive deflection or structural failure of the downslope micropiles due to the loss of lateral support.

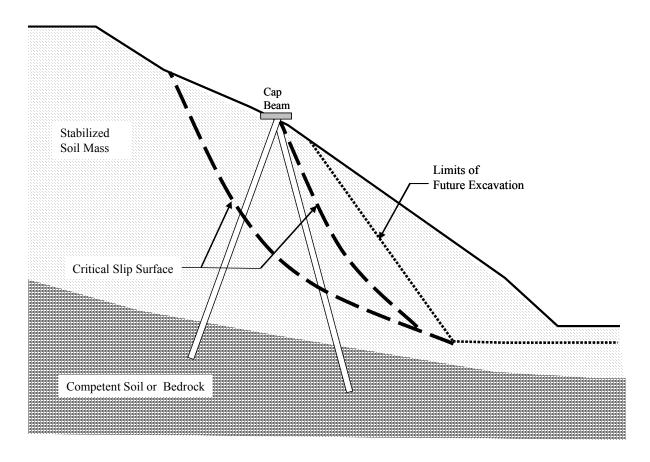


Figure 6-13. Potential Instability Resulting from Future Excavation.

There are two approaches to address these issues:

• As part of the design submittal, the Owner can require calculations to be performed which establish the maximum amount of excavation that could be performed in front of the micropiles. This critical geometry would show the greatest length of excavation into the slope such that a minimum factor of safety is maintained and so that the soil in front of the micropile structure remains stable thus providing the required lateral support to the front row of micropiles. Furthermore, it is recommended herein that this design check be performed and the information be

provided to the Owner, regardless of whether such a check is specifically requested in the Contract Documents.

• Where micropile structures are used, the Owner may fence off the area and post signs alerting that excavation should not be performed in the area.

### 6.6.3 Load Transfer in Micropiles

Micropiles resist unstable slope forces through a combination of axial resistance developed at the grout-to-ground interface both above and below the potential slip surface and structural (i.e., shear and bending) resistance. As mentioned earlier, the maximum lateral micropile movement is assumed to occur near the elevation of the critical potential slip surface. This is a reasonable assumption for micropiles since micropiles are relatively flexible. An example showing the resultant axial force and bending moment diagrams for an upslope leg and downslope leg of micropiles used for a slope stabilization project in Littleville, Alabama (Brown and Chancellor, 1997) is presented in Figure 6-14.

The capacity of individual micropiles used for slope stabilization can be increased significantly by designing the micropiles to be inclined or "battered" relative to the critical potential slip surface. If the micropile is battered, slope movements will result in the tendency for the micropile to be "pulled" away from the slip surface resulting in axial tension forces or to be "pushed" towards the slip surface resulting in axial compression forces. These forces are mobilized as side resistance at the grout-to-ground interface. For micropile structures without ground anchors used to stabilize landslides, the upslope leg will typically be in tension and the downslope leg will typically be in compression.

The maximum axial force in a micropile will occur near the location of the critical potential slip surface. In this sense, the development of axial resistance is similar to that for soil nails. For the micropiles to develop the required axial resistance for design, the micropile must be embedded sufficiently into the ground below the critical slip surface to prevent micropile

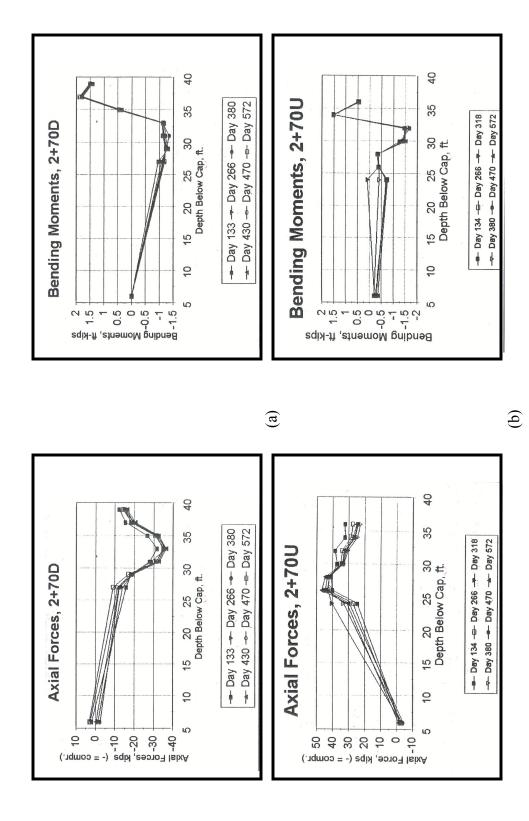


Figure 6-14. Example Resultant Axial Force and Bending Moment Diagrams for (a) Downslope and (b) Upslope Micropile (after Brown and Chancellor, 1997).

Note: 1 kip = 4.448 kN and 1 ft = 0.3048 m

failure through pullout (if the micropile is loaded in tension) or failure as a result of insufficient bearing capacity (if the micropile is loaded in compression). In other words, the side resistance capacity of the micropile below the potential slip surface must be sufficient to resist axial forces developed above the potential slip surface (see Figure 6-15).

The axial force required to be resisted by the micropile below the potential slip surface is assumed to be equal to the ultimate side resistance of the micropile that could develop above the failure surface with a factor of safety. The ultimate side resistance of the micropile above the failure surface,  $P_{ult}$ , can be calculated as:

$$P_{\text{ult}} = \alpha_{\text{bond-above}} \times L_{\text{above}} \times \pi \times d$$
 (Eq. 6-1)

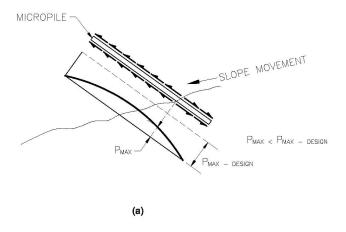
where  $\alpha_{bond-above}$  is the grout-to-ground ultimate bond strength above the critical slip surface,  $L_{above}$  is the length of the micropile from the slip surface to the bottom of the cap beam, and d is the diameter of the micropile. The value for  $\alpha_{bond-above}$  is estimated using Table 5-3.

In addition to axial resistance, micropiles develop flexural resistance. The design objective therefore, is to select a micropile system with sufficient structural capacity to resist the unbalanced slope force (i.e.,  $H_{req}$ ) without structural failure of the micropile in combined axial loading and bending.

Therefore, the required length of the micropile below the slip surface, L_{below}, is calculated as:

$$L_{\text{below}} = \frac{P_{\text{ult}}}{\alpha_{\text{bond-below}} \times \pi \times d} \times FS$$
 (Eq. 6-2)

where  $P_{ult}$  is calculated using Eq. 6-1,  $\alpha_{bond-below}$  is the grout-to-ground ultimate bond strength below the critical slip surface and is estimated using Table 5-3. A FS = 2.0 should be used in Eq. 6-2.



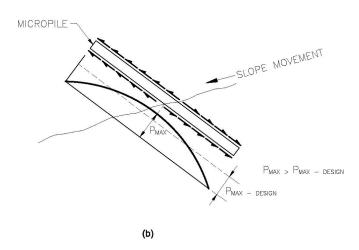


Figure 6-15. (a) Micropile Resistance Length Not Sufficient to Prevent Pullout and (b) Micropile Resistance Length Sufficient to Prevent Pullout.

Currently, load testing of micropiles for slope stabilization projects is not commonplace; therefore required micropile side resistance has relied exclusively on contractor experience in similar ground. This document, however, recommends that load testing be performed. Load testing requirements for slope stabilization projects is provided in Chapter 7.

# 6.6.4 Bending Moment and Shear Capacity of Single Vertical Micropile

# 6.6.4.1 Evaluation of Bending Moment Capacity of Single Vertical Micropile

The shear resistance of a micropile corresponds to the maximum shear force that can be applied to the micropile that results in a maximum bending moment within the micropile (at any location) to be just equal to the ultimate bending moment of the micropile.

To evaluate the shear resistance of a single micropile, the ultimate bending moment ( $M_{ult}$ ) of the single micropile is checked. The ultimate bending moment of a single vertical micropile can be conveniently evaluated using the computer program LPILE (2005) or other soil-structure interaction programs used for the analysis of laterally loaded piles and shafts. Because micropiles are battered, they develop axial resistance through side friction between the grout and the ground. Since the bending moment capacity of a micropile (or any other structural section) varies depending on the applied axial load, the bending moment capacity of a single micropile is checked for two limiting axial load conditions: (1) axial load equal to zero, P = 0; and (2) axial load equal to the ultimate side resistance of the micropile,  $P = P_{ult}$  (where  $P_{ult}$  is calculated using Eq. 6-1).

In these analyses, the shear capacity corresponding to the ultimate bending moment in the micropile is used. The rationale for this is described in Section 6.8.

As previously discussed, axial loads in micropiles may be in tension or compression. In general, the uphill micropile will be in tension and the downhill micropile will be in compression. However, where ground anchors are incorporated into the micropile structure, the direction of the axial load for individual micropiles may change depending on ground anchor stressing and lock-off loads. For this reason,  $M_{ult}$  should be evaluated for the  $P = P_{ult}$  case considering that this axial load is applied in compression and in tension. The design would then be based on the case that provides the lower  $M_{ult}$ ; and therefore the lower value for available micropile shear resistance.

### 6.6.4.2 Evaluation of Shear Capacity of Single Vertical Micropile

The maximum shear force that the micropile can carry corresponds to that shear force applied at the elevation of the slip surface that results in a calculated maximum bending moment in the micropile that is equal to  $M_{ult}$ . This maximum bending moment is affected by the stiffness (i.e., p-y response) of the ground above and below the potential slip surface and the flexural rigidity of the micropile. This evaluation can be performed using laterally loaded pile analyses for single elements such as that provided in LPILE.

The shear force capacity of a single vertical micropile is determined by analyzing separately the portion of the micropile above the potential slip surface (termed the "up" analysis) and the portion of the micropile below the potential slip surface (termed the "down" analysis). This requires, for the up analysis, adjustment of the location of previously determined p-y curves relative to the top of the pile in the analysis. Figure 6-16 shows p-y curves for the entire length of the micropile and Figure 6-17 shows how they are adjusted for the up and down analyses.

The iterative process to determine the maximum shear capacity requires performing up and down analyses as a set. Both analyses are performed for minimum axial resistance conditions (i.e., P = 0) first and then for maximum axial resistance conditions (i.e.,  $P = P_{ult}$ ). The boundary shear forces and bending moments applied at the slip surface location, although applied as boundary conditions in the analyses, are actually internal forces and bending moments within the micropile. Because of this, specific criteria need to be satisfied when comparing the up and down analyses results to evaluate the correctness of the analyses. These are described below:

- The same value for axial load is used for both the up and down analyses.
- The input shear force magnitude and direction applied at the slip surface location is the same for the up and down analyses.
- The input bending moment applied as a boundary condition should be equal in magnitude and opposite in sign for the up and down analyses.
- The calculated slope of the micropile head at the slip surface should be the same for the up and down analyses.
- The head of the micropile is modeled as free.

Figure 6-18 shows calculated bending moment diagrams for a micropile using the up and down analyses. These analyses show the iterative process wherein the analysis is complete for the case where  $M_{max} = M_{ult}$  and the pile head slope from the up and down analysis is equivalent. For Analysis 1, a bending moment at the slip surface location of 40 kN-m is assumed. With this, it is seen that the calculated slopes of the micropile from the up and down analysis are not the same. This implies a discontinuity in slope at the slip surface location, which is not possible. For the next iteration, a bending moment of 87 kN-m is assumed. Inspection of the table in Figure 6-18 indicates that for this slip surface location bending moment, the pile head slope from the up and down analysis are equivalent; it is also seen that the maximum calculated bending moment of 161 kN-m occurs below the slip surface and is approximately equal to the ultimate bending moment based on the structural capacity of the micropile section assumed. Thus, the analysis is complete. **This procedure** is demonstrated in the **Design Example provided in Section 6.7.6.** 

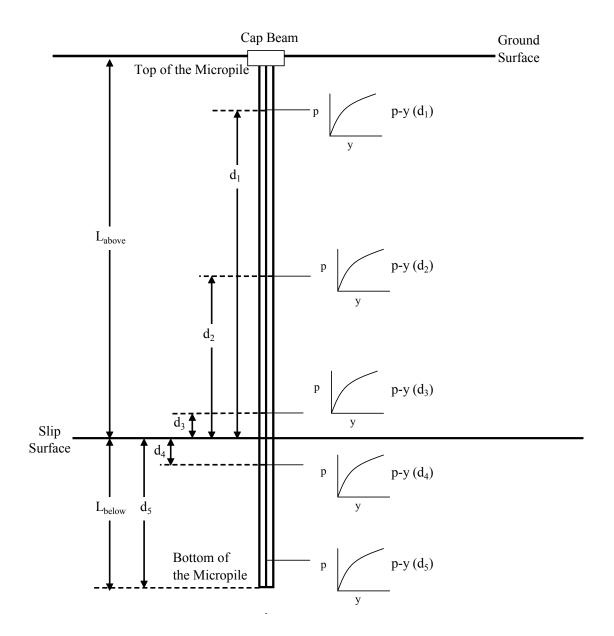
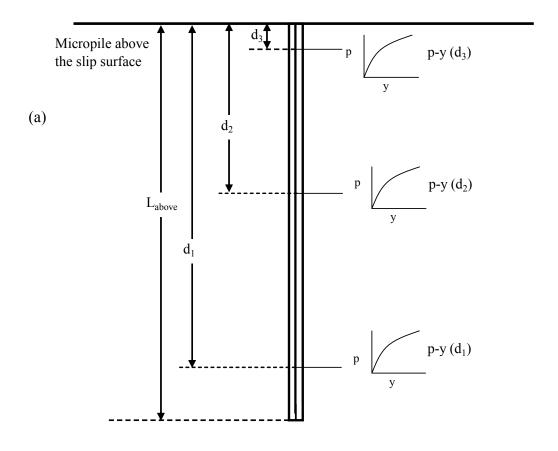


Figure 6-16. An Example Distribution of p-y Curves with Depth Obtained from Laterally Loaded Pile Analysis.



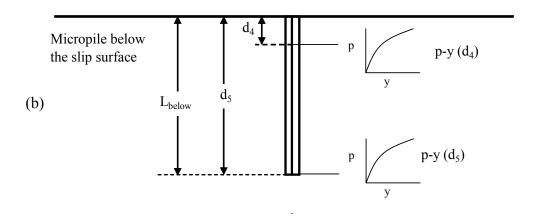
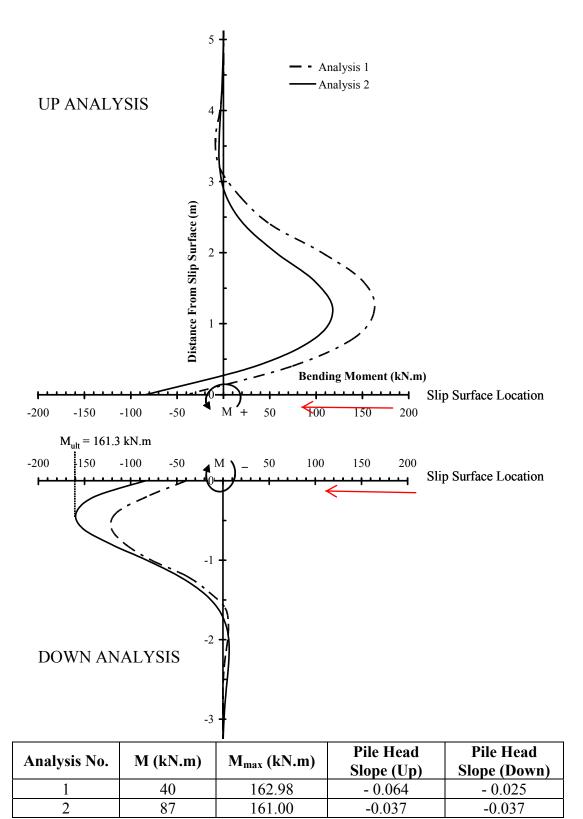


Figure 6-17. Utilizing p-y Curves Obtained From Laterally Loaded Pile Analysis in: (a) Up Analysis and (b) Down Analysis.



Note: M: Applied bending moment. 1 kN.m = 0.737 k.ft

Figure 6-18. Example of Calculated Bending Moment Diagrams for Up and Down Analyses.

#### 6.6.5 Shear Capacity of Battered Micropile Group

The maximum lateral force ( $H_{ult}$ ) that an inclined (or battered) single micropile can resist at the location of the critical slip surface is evaluated in this step. For the analysis, the effects of a non-horizontal slip surface are also addressed. The value for  $H_{ult}$  which will be compared to the required force to provide the target factor of safety, i.e.,  $H_{req}$ , is the sum of the individual  $H_{ult}$  values from each battered micropile in the cross section.

The assumed forces acting on a micropile are shown in Figure 6-19 for the case of a vertical micropile (where axial resistance is assumed to be zero, i.e., P=0) and for an inclined micropile (where axial resistance is assumed to be equal to the ultimate axial resistance provided by the ground above the slip surface, i.e.,  $P=P_{ult}$ ). The inclination angle ( $\psi$ ) may be defined as the angle between the slip surface and the vertical axis of the pile.

Summing the shear (Q) and axial (P) forces shown in Figure 6-19b in the x and y direction results in the following:

$$Q = H \cos \psi - V \sin \psi \qquad (Eq. 6-3)$$

$$P = V \cos \psi + H \sin \psi$$
 (Eq. 6-4)

These equations can be solved simultaneously to provide the lateral pile load (along the slip surface):

$$H = Q \cos \psi + P \sin \psi \qquad (Eq. 6-5)$$

This lateral pile load, H, is coincident with the orientation of  $H_{req}$  (see Figure 6-11). Since the purpose of this analysis is to evaluate the ultimate capacity of the micropile, corresponding ultimate values for P and Q in Eq. 6-5 are selected. The minimum axial resistance of a single micropile is zero and the maximum axial resistance is assumed to equal  $P_{ult}$ . Because Eq. 6-5 is a function of the inclination of the micropile relative to the slip surface, it is necessary to select a range of inclination angles for which the analyses corresponding to P=0 is valid and for which the analyses corresponding to P=0 is valid and for which the analyses corresponding to P=0 is valid and P=0 is valid and P=0 is valid and P=0 in Eq. 6-5 are defined as:

For 
$$\psi = 0^{\circ} \rightarrow P = 0$$
 and  $Q = Q_{P=0}$ ; therefore  $H_{ult} = Q_{P=0}$  (Eq. 6-6)

For 
$$\psi \ge 30^{\circ} \rightarrow P = P_{ult}$$
 and  $Q = Q_{P=Pult}$ ; therefore  $H_{ult} = Q_{P=Pult} \cos \psi + P_{ult} \sin \psi$  (Eq. 6-7)

Although axial resistance of micropiles should be mobilized even at very small inclination angles, it is conservative to assume that axial resistance is not mobilized until a nominal amount of inclination is achieved. Moreover, relying on axial resistance at small inclination angles implies a level of certainty in the angle of the slip surface (i.e., slope of the failure surface) which can probably not be achieved practically through subsurface investigation techniques; the accurate assessment of the failure surface angle may be difficult to achieve.

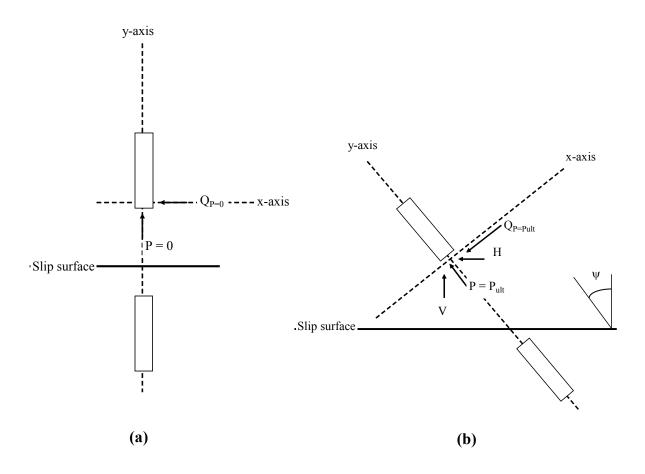


Figure 6-19. Forces Acting On (a) Vertical and (b) Inclined Micropile Along The Slip Surface.

Therefore, for the design procedure presented herein, the following recommendations are provided for inclination angles between 0 and 30 degrees:

For 
$$0 < \psi \le 10^{\circ} \rightarrow H_{ult} = Q_{P=0}$$
 (Eq. 6-8)

For 
$$10 < \psi < 30^{\circ} \rightarrow H_{ult}$$
 is interpolated (see Figure 6-20) (Eq. 6-9)

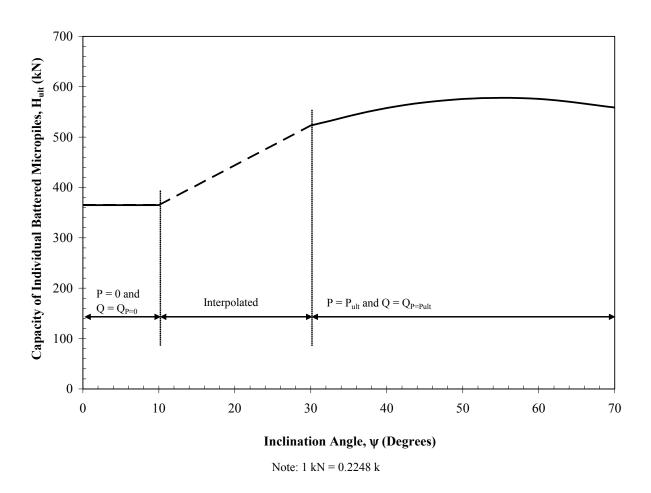


Figure 6-20. Relationship Between Adjusted Capacity of Individual Micropiles and Inclination Angle.

The relationship between adjusted capacity of the individual micropiles and inclination angle based on the above definitions is provided in Figure 6-20 for a specific single micropile design. Once the inclination angles for design are selected, Eqs. 6-7, 6-8, and 6-9 can be used directly to evaluate the shear capacity of each micropile in a cross section, i.e., the development of a figure such as Figure 6-20 is not necessary. This analysis is shown as part of a detailed design example in Section 6.7.7.

The inclination angle  $\psi$  is defined as the angle between the axis perpendicular to the slip surface and the micropile axis or as the angle between the axis perpendicular to the micropile axis and the slip surface (Figure 6-21). Solutions for positive and negative inclination angles are identical for Eqs. 6-3 and 6-4 (Poulos and Davis, 1980). Therefore,  $\psi$  should be written as positive in Eq. 6-5 regardless of its sign.

Using Eq. 6-5, the capacity of the upslope micropile and the downslope micropile can be evaluated using the criteria presented concerning appropriate values for Q and P and depending on the micropile inclination angle, $\psi$ . The inclination angle should be assessed at the location where each of the two micropiles crosses the slip surface. The combined capacity of the upslope and downslope micropile is determined as:

$$H_{\text{ult-pair}} = H_{\text{ult}} (\Psi_{\text{us}}) + H_{\text{ult}} (\Psi_{\text{ds}})$$
 (Eq. 6-10)

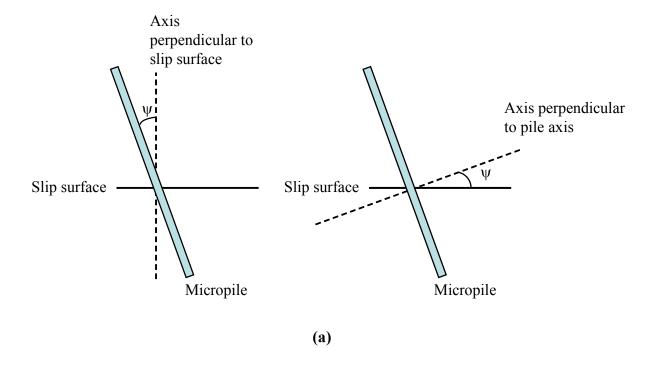
where  $\psi_{us}$  is the inclination angle for the upslope micropile and  $\psi_{ds}$  is the inclination angle for the downslope micropile.

#### 6.6.6 Spacing Required to Provide Required Force to Stabilize the Slope

Figure 6-22 shows a detail of a typical micropile layout at the cap beam location. The magnitude of resisting force provided by the micropiles on a per unit length of cap beam basis must be at least equal to  $H_{req}$  (calculated from slope stability analysis in Design Step 5). Also, the distance between individual micropiles along the cap beam ( $S_{offset}$ ) must be large enough to permit ease of construction of the micropile elements.

The shear capacity of the battered upslope micropile  $(H_{ult(\Psi us)})$  and battered downslope micropile  $(H_{ult(\Psi ds)})$  are evaluated using Eq. 6-5 and the combined capacity of the upslope and downslope micropile  $(H_{ult-pair})$  is calculated using Eq. 6-10. From this,  $S_{max}$  (see Figure 6-22) may be evaluated as:

$$S_{\text{max}} = \frac{H_{\text{ult-pair}}}{H_{\text{req}}}$$
 (Eq. 6-11)



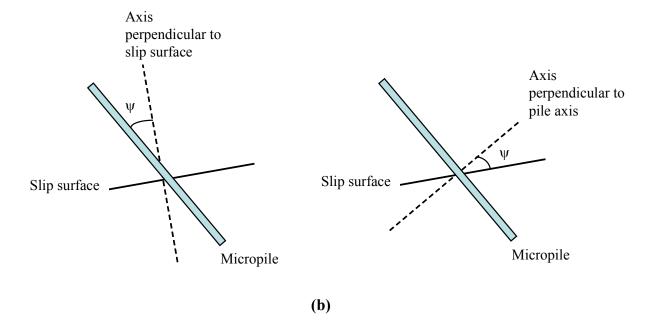
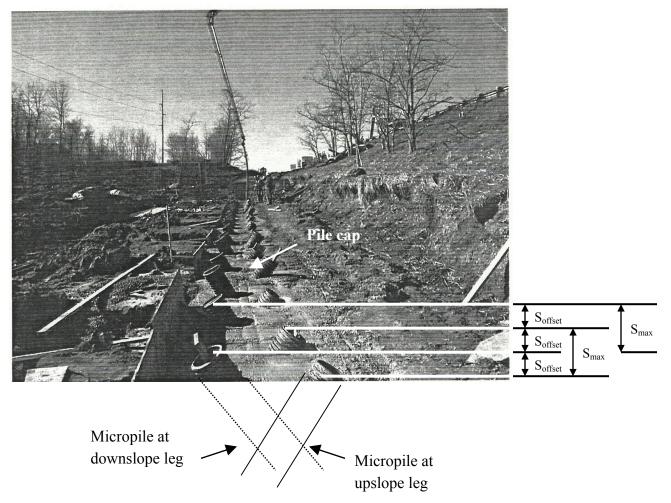


Figure 6-21. Definition of Inclination Angle When (a) Slip Surface is Horizontal and (b) Slip Surface is not Horizontal.



Notes:  $S_{offset}$  is the spacing between two micropiles  $S_{max}$  is the spacing between two upslope or downslope micropiles

Figure 6-22. Spacing Between Micropiles.

# 6.6.7 Potential for Soil Flow Between Micropiles

If micropiles are spaced too far apart and/or if the soil above the slip surface is very weak, there is a potential for soil material to move in-between adjacent micropiles (Figure 6-23). This failure mechanism has been termed plastic flow. Ito and Matsui (1975) developed a theory to evaluate plastic flow between piles. The lateral force per unit thickness of soil acting on the micropile, q is calculated as (Hassiotis et al., 1997):

$$q = A \times c \times \left(\frac{1}{N_{\phi} \tan \phi} \times \{B - (2 \times E) - 1\} + F\right) - c \times \left(D_{1} \times F - 2 \times D_{2} \times N_{\phi}^{-(1/2)}\right) + \frac{\gamma \overline{z}}{N_{\phi}} \times \{(A \times B) - D_{2}\}$$
 (Eq. 6-12)

where:

c = cohesion of the soil

 $\gamma$  = unit weight of soil

 $D_1 = S_{max}$  (Eq. 6-11)

 $\phi$  = friction angle of soil  $\bar{z}$  = depth from ground surface

 $D_2$  = opening between micropiles (Figure 6-23)

$$N_{\phi} = \tan^2 \left[ \left( \pi / 4 \right) + \left( \phi / 2 \right) \right]$$

$$\mathbf{A} = \mathbf{D}_1 \times \left(\frac{\mathbf{D}_1}{\mathbf{D}_2}\right)^{\left[\mathbf{N}_{\phi}^{(1/2)} \tan\phi + \mathbf{N}_{\phi} - 1\right]}$$

$$B = \exp \left[ \frac{D_1 - D_2}{D_2} \times N_{\phi} \tan \phi \tan \left( \frac{\pi}{8} + \frac{\phi}{4} \right) \right]$$

$$E = N_{\phi}^{(1/2)} tan \phi$$
; and

$$F = \frac{(2 \times \tan \phi) + (2 N_{\phi}^{(1/2)}) + N_{\phi}^{-(1/2)}}{E + N_{\phi} - 1}$$

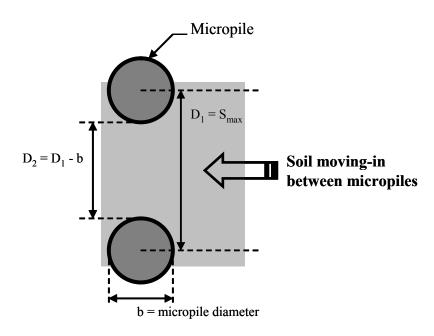


Figure 6-23. Plastically Deforming Soil between Two Adjacent Micropiles.

The ultimate horizontal force acting on the micropile due to soil movement between adjacent micropiles, H_{ult-soil/pile} is the value for q integrated over the length of the micropile from the slip surface to the cap beam. An example spreadsheet showing this procedure is presented is presented in Section 6.7.9.

To evaluate the spacing between micropiles, the calculated  $H_{ult-soil/pile}$  is compared to the average resistance provided by the upslope and downslope pair  $(H_{ult-pair}/2)$  as shown below:

- If the plastic flow conditions are satisfied, then  $S_{max}$  previously calculated using Eq. 6-11 does not need to be reduced.
- If  $H_{ult\text{-}soil/pile} < H_{ult\text{-}pair}/2$ , then plastic flow conditions govern and  $S_{max}$  should be reduced. The plastic flow analysis should be repeated based on the new pile spacing corresponding to the reduced  $S_{max}$ . The final design spacing should be selected as the spacing that satisfies  $H_{ult\text{-}soil/pile} \ge H_{ult\text{-}pair}/2$ .

#### 6.7 DESIGN EXAMPLE FOR SLOPE STABILIZATION WITH MICROPILES

This section provides a complete design example for micropiles used for slope stabilization. The problem comprises stabilizing an embankment that exhibits creep movements particularly during rainy periods. The cross section of the embankment and subsurface information is shown in Figure 6-24.

The roadway surcharge for design is 12 kPa. Right-of-way limitations preclude the use of a berm to stabilize the embankment. For this example, it is assumed that micropiles have been determined to be the best solution to meet the project constraints.

Subsurface conditions are illustrated on Figure 6-24. The slope consists of silty clay overlying calcareous siltstone. Based on laboratory test results, the unit weight of the silty clay is estimated to be 21.2 kN/m³ (134.9 pcf) and calcareous siltstone is estimated to be 23.0 kN/m³ (146.4 pcf). Based on the Atterberg limits results, the silty clay has a liquid limit of 60 and hydrometer results indicate that the silty clay has up to 30 percent clay size material. Shear strength test results for the bedrock indicate a friction angle of 23 degrees with a cohesion intercept of 480 kPa (69.65 psi).

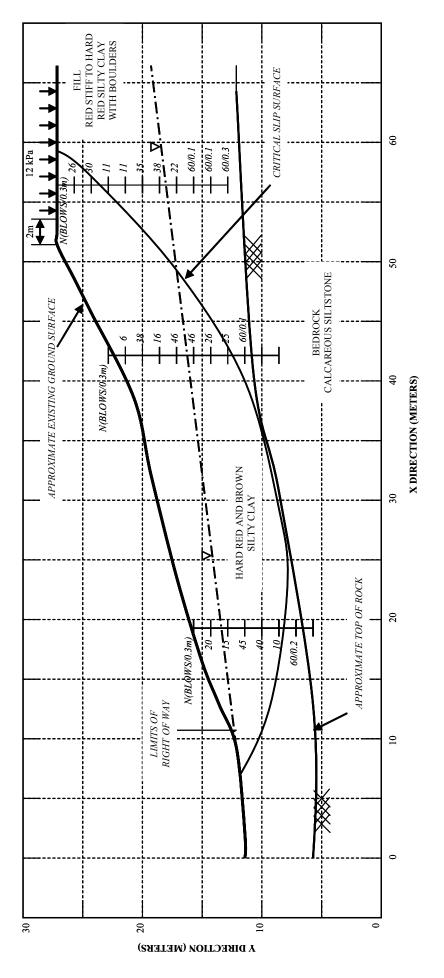


Figure 6-24. Slope Geometry and Subsurface Information for the Design Example.

The critical slip surface location was identified via observations from surficial features (i.e., scarp location at embankment crest and heaving near toe) and from preliminary slope stability analyses.

## 6.7.1 STEP 4: Evaluate Factor of Safety of Existing Slope

Perform slope stability analysis to compute the minimum factor of safety of the slope ( $FS_{min}$ ). Computer programs such as XSTABL, SLIDE, or others can be used to perform the analyses. When performing slope stability analyses, methods such as Simplified Janbu, Simplified Bishop, or Spencer are used.

Because this slope had previously undergone movements, it was assumed that the existing factor of safety of the slope is 1.0. A back-analysis is performed to estimate the shear strength parameters of the silty clay that correspond to FS = 1.0. Back-analysis is performed following the steps presented below:

i. <u>Estimate shear strength parameters</u>. Because the slope has moved sufficiently, the residual drained friction angle can be used (e.g.,  $\phi' = \phi'_r$ ) to model the soil material where these movements have occurred. For the back-analysis, the shear strength parameters estimated at this stage are considered as trial strengths ( $\phi_{trial}$  and  $c_{trial}$ ).

Using Figure 6-4, with LL=60 and a clay fraction of 30 percent, results in  $\phi'_r$  equal to 18° (i.e.,  $\phi_{trial} = 18^\circ$ ). The cohesion of the same soil layer was assumed to be 25 kPa (3.63 psi) (i.e.,  $c_{trial} = 25$  kPa) based on previous experience with these materials.

Slope stability analyses were performed using the computer program SLIDE and Spencer's limit equilibrium method. The FS of the slope based on trial strengths (i.e.,  $\phi_{trial} = 18^{\circ}$  and  $c_{trial} = 25$  kPa) is 1.67 (Figure 6-25).

The trial shear strength parameters were modified using Eqs. 6-13 and 6-14:

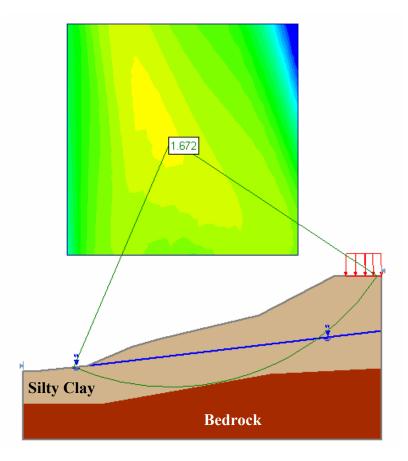


Figure 6-25. FS_{min} Determined from Trial Shear Strength Parameters.

$$\phi(\text{modified}) = \tan^{-1} \frac{\tan{\{\phi(\text{trial})\}}}{FS_{\text{trial}}}$$
 (Eq. 6-13)

$$c(\text{modified}) = \frac{c(\text{trial})}{\text{FS}_{\text{trial}}}$$
 (Eq. 6-14)

Based on the above,  $\phi$ ' (modified) is found to be 11° and c' (modified) is 15 kPa (2.18 psi).

The back-analysis method presented above should be used with caution. As mentioned before, the calculated critical failure surface needs to be compared against the observed critical failure surface in the field. Also, the use of a nonzero effective stress cohesion intercept should be used with caution as deformations tend to reduce this cohesion.

A slope stability analysis was performed using the modified shear strength parameters of the slope material and the computed FS = 1.0, (Figure 6-26) and the critical slip surface generated by the program is found to be reasonably consistent with the actual slip surface in the field.

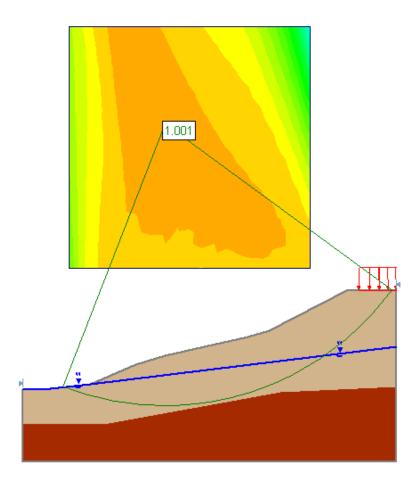


Figure 6-26. FS_{min} of the Slope Based on Modified Shear Strength Parameters.

## 6.7.2 STEP 5: Evaluate Additional Force Required To Obtain Target Factor of Safety

A target factor of safety (FS_{target}) of 1.3 is selected for this slope and the micropile was modeled using Approach 2 (see Section 6.6.2.2) using the computer program SLIDE (2004). Several slope stability analyses were performed in which the micropile was located at approximately a midslope location. For these analyses, the shear strength assigned to the micropile was varied until the target factor of safety for the slope was achieved (see Figure 6-

27). The additional force required from the micropile ( $H_{req}$ ) is 650 kN/m (44.54 k/ft) of slope length.

Additional slope stability analyses were performed to confirm that slip surfaces upslope and downslope from the micropile location have an acceptable factor of safety. The results of these analyses are presented in Figure 6-28. From the analyses, the minimum factor of safety for upslope slip surfaces ( $FS_{up}$ ) is 1.30 and the minimum factor of safety for downslope slip surface ( $FS_{down}$ ) is 1.35. These values are greater than  $FS_{target}$ , and therefore the location for the micropile is deemed appropriate.

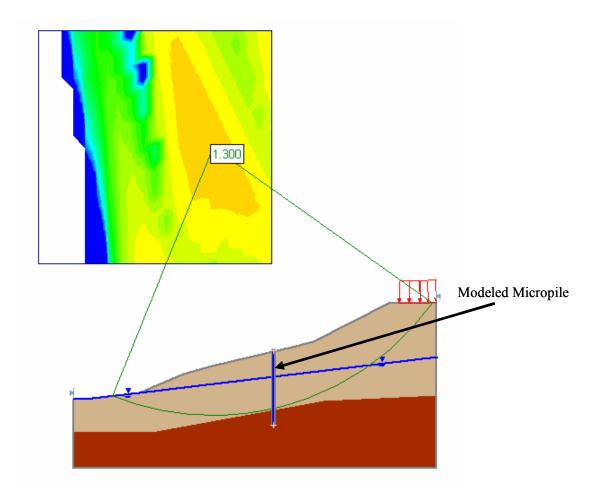


Figure 6-27. Slope Stability Analysis to Determine Additional Force to Obtain Target Factor of Safety.

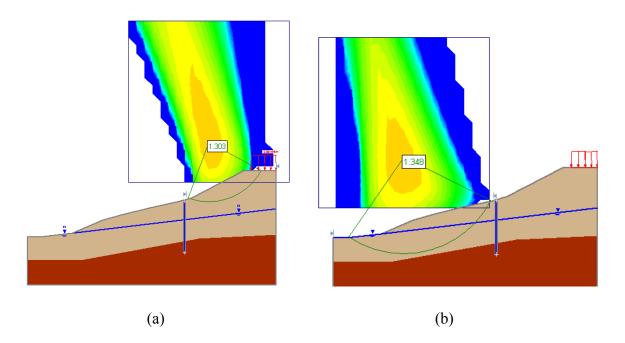
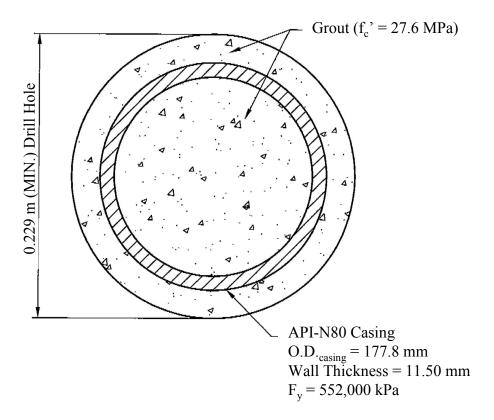


Figure 6-28. Stability of the (a) Upslope Away from the Micropile and (b) Downslope Away from the Micropile.

If the factor of safety of the slope entirely downslope or entirely upslope of the micropile was less than FS_{target} then the location of the micropile would need to be changed or an additional micropile would be required.

## 6.7.3 STEP 6: Select Micropile Cross Section

In this example, the micropile cross section is selected as shown in Figure 6-29. A Type A micropile is used. The ground is considered nonagressive and no reduction in steel casing thickness is required.



Note: 1 mm = 0.04 in, 1 m = 3.281 ft, 1 MPa = 1,000 kPa = 145.1 psi

Figure 6-29. Micropile Cross-Section for the Design Example.

## 6.7.4 STEP 7: Estimate Length Of Micropile

Estimate total length (L_{total}) of the micropile as:

$$L_{\text{total}} = L_{\text{above}} + L_{\text{below}}$$
 (Eq. 6-15)

 $L_{above}$  is the length of micropile between the ground surface and the critical slip surface.  $L_{below}$  is the length of the micropile below the critical slip surface.

In the design example,  $L_{above}$  is approximately 10 m (3.28 ft). This depth can be approximated from Figure 6-24 based on the selected micropile location shown in Figure 6-27. To calculate  $L_{below}$ ,  $P_{ult}$  is calculated using Eq. 6-1:

$$P_{ult} = \alpha_{bond-above} \times L_{above} \times \pi \times d = 66 \text{ kPa} \times 10 \text{ m} \times \pi \times 0.229 \text{ m} = 475 \text{ kN (107 k)}$$

The value for  $\alpha_{\text{bond-above}}$  is within the range for Type A micropiles in relatively stiff silts and clays (see Table 5-3).

L_{below} is calculated as:

$$L_{\text{below}} = \frac{P_{\text{ult}}}{\alpha_{\text{bond-below}} \times \pi \times d} \times FS = \frac{475 \text{ kN}}{515 \text{ kPa} \times \pi \times 0.229 \text{ m}} \times 2.0 = 2.6 \text{ m} (8.5 \text{ ft})$$

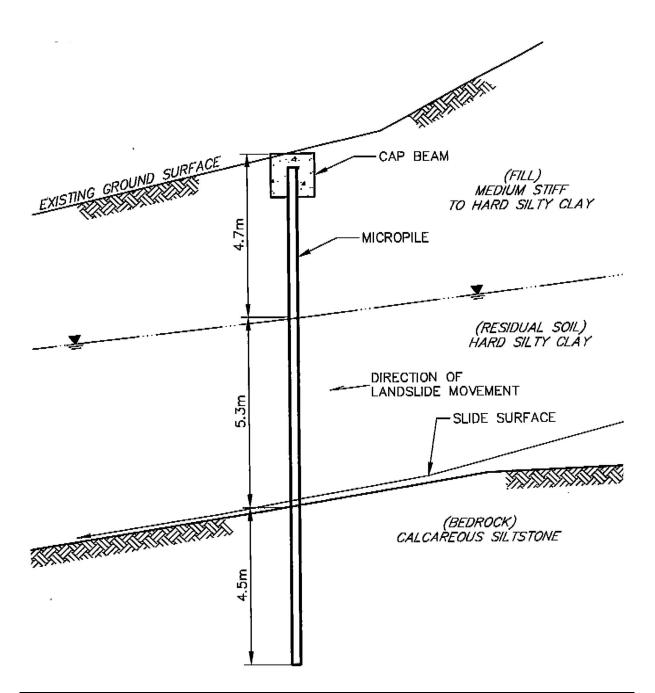
where  $\alpha_{\text{bond-below}}$  is estimated from Table 5-3 for hard shale. The bedrock at the site consists of siltstone, which is by definition closer to shale than sandstone or limestone. The FS for ultimate side resistance was selected to be 2.0.

The estimated length to resist uplift or compression forces is calculated to be 2.6 m. Preliminary LPILE analyses showed that this length of micropile below the slip surface was not sufficient to provide fixity of the micropile. To promote fixity of the micropile below the critical slip surface (with respect to lateral loading considerations), the length of the micropile below the critical slip surface was increased from 2.6 m (8.5 ft) to 4.5 m (15 ft) based on further analysis.

## 6.7.5 STEP 8: Evaluate Bending Capacity Of Single Vertical Micropile

The ultimate bending moment,  $M_{ult}$ , for a single vertical micropile with the cross section shown in Figure 6-29 is evaluated in this step using LPILE. The single vertical micropile model is shown in Figure 6-30. In addition to the cross section geometry, the following material properties must be specified for the analysis: (1) grout compressive strength; (2) yield strength of the steel casing; and (3) modulus of elasticity of the steel.

The soil parameters for the LPILE analysis are shown in Figure 6-30. For this lateral loading condition, the profile at the location of the micropile was modeled using p-y curves for stiff clays. The undrained strength,  $S_u$ , was conservatively estimated for the fill and residual soil layer based on measured SPT N values. Modeling the bedrock as a stiff clay is also conservative. More accurate parameter values could have been evaluated by more sophisticated testing methods.



Soil Type	φ (deg)	$S_u (kN/m^2)$	$\gamma$ ' (kN/m ³ )	<b>€</b> 50
Fill	0	120	21.2	0.0050
Residual Soil	0	168	11.4	0.0040
Bedrock	0	480	13.2	0.0025

 $1 \text{ kPa} = 0.1451 \text{ psi} \text{ and } 1 \text{ kN/m}^3 = 6.366 \text{ psf}$ ).

Figure 6-30. Single Vertical Micropile Modeled in LPILE.

In the analysis,  $M_{ult}$  is calculated for P = 0 and for  $P = P_{ult} = 475$  kN (107 k). The value for  $M_{ult}$  was calculated using the option within LPILE to account for nonlinear flexural rigidity of the micropile. That is, the bending stiffness of the micropile reduces with increasing strain. The value for  $M_{ult}$  is assumed to correspond to the bending moment in the micropile for which the compressive strain in the grout inside the casing is 0.003. The results of the  $M_{ult}$  evaluation are shown in Table 6-2.

**Table 6-2.** Mult Values for Design Example.

]	)	$\mathbf{M}_{ ext{ult}}$		
(kN)	(k)	(kN.m)	(k.ft)	
0	0	161.3	119.0	
475	107	147.7	108.9	

## 6.7.6 STEP 9: Evaluate Shear Capacity of Single Vertical Micropile

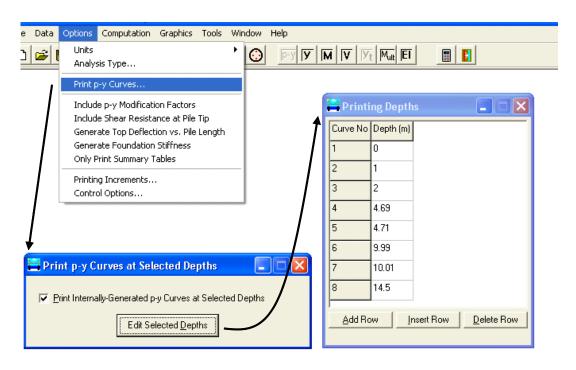
The maximum shear capacity of a single vertical micropile (Q) is determined iteratively by performing laterally loaded pile analyses. For the design example, p-y curves may be generated within LPILE in the same analyses as were performed for the calculation of M_{ult}. The p-y curves are generated for various depths along the micropile and specifically for depths just below and above the depth of the transition between individual soil or rock layers (Figure 6-30). The depths chosen for this example are shown in Figure 6-31.

After obtaining the p-y curves, the maximum shear capacity of a single vertical micropile can be calculated using: (1)  $M_{ult}$  from P = 0 case; and (2)  $M_{ult}$  from  $P = P_{ult}$  case using up and down analyses.

The iterative design process for up and down analyses is summarized in Figure 6-32. Perform a set of up and down analyses for P = 0 axial load case first and then perform the same analyses for  $P = P_{ult}$  following the process described below:

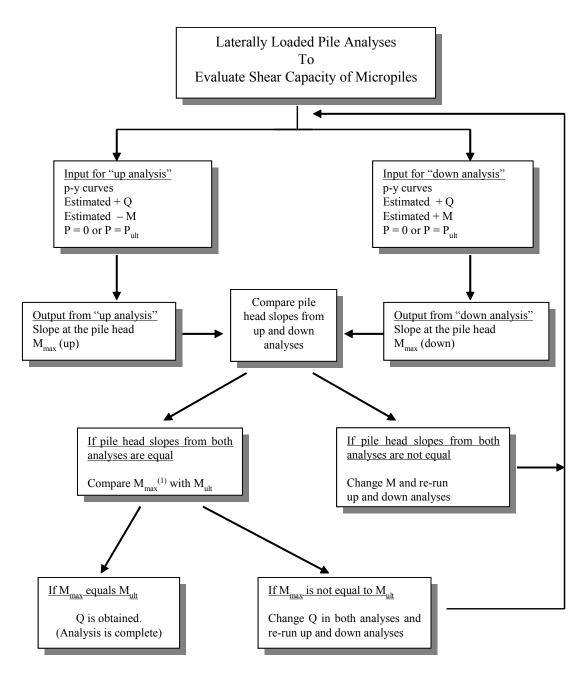
- 1. Set up the up and down analyses by inputting micropile cross section, micropile material properties, soil or rock parameters for each layer and p-y curves (adjust the location of p-y curves relative to slip surface as shown on Figure 6-17).
- 2. Input a trial estimate of the shear force Q (magnitude and signs are same for up analysis and down analysis) and input a trial estimate of the internal bending moment (M) (magnitude is same but M is negative for the up analysis and positive for the down analysis). It should be noted that the selection of trial

- estimates for Q and M are arbitrary. If the initial estimate of Q is <u>less than</u> the value of Q which ultimately corresponds to  $M_{ult}$ , the solution will converge. If the initial estimate of Q is <u>greater than</u> the value of Q which ultimately corresponds to  $M_{ult}$ , the solution will not converge. This will be evidenced by pile head slopes from the up and down analysis which diverge from each other with each iteration.
- 3. Perform laterally loaded pile analyses for up and down analyses and compare the slopes computed at the micropile head from both analyses. If the slopes at the micropile head are not equal then change the magnitude of the initially estimated M (i.e., in Step 1) and re-run both analyses again. When slopes at the pile head are equal from both analyses, note the calculated maximum bending moment (M_{max}) from each analysis.
- 4. Compare  $M_{max}$  (greater of  $M_{max}$  values from up and down analyses) with previously calculated bending moment capacity ( $M_{ult}$ ) for the corresponding axial load.
- 5. If  $M_{max}$  is approximately equal to  $M_{ult}$  then Q is determined and analysis for this axial load case is completed. If  $M_{max}$  is not equal to  $M_{ult}$ , change the magnitude of the initially estimated Q (i.e., in Step 5) and re-run both analyses again.
- 6. Repeat steps 1 through 4 for the  $P = P_{ult}$  case. In step 3 use  $M_{ult}$  calculated for the  $P = P_{ult}$  case.



Note: 1 m = 3.281 ft.

Figure 6-31. Depths Chosen for p-y Curves for Entire Length of the Micropile.



Note:  $^{(1)}$   $M_{max}$  = the greater of  $M_{max}$  (up) and  $M_{max}$  (down)

Figure 6-32. Process to Evaluate Shear Resistance (Q) of Single Vertical Micropile Using Up and Down Laterally Loaded Pile Analyses.

The laterally loaded pile analysis output for P = 0 and  $P = P_{ult}$  are presented in Appendix B. The up analysis is performed for the pile length of 10 m (32.8 ft) and the down analysis for the pile length of 4.5 m (15 ft). The soil/rock layers in up and down analyses are modeled by adjusting the previously determined p-y curves. For each soil layer depth, p-y curves are inputted in the model. An example is shown in Figure 6-33 for the up analysis. The p-y values in the "external p-y curve" dialog box in Figure 6-33 are the previously determined p-y values at a depth of 10 m. Using the adjustment shown in Figure 6-17a, they are assigned to a depth of 0 m for the up analysis.

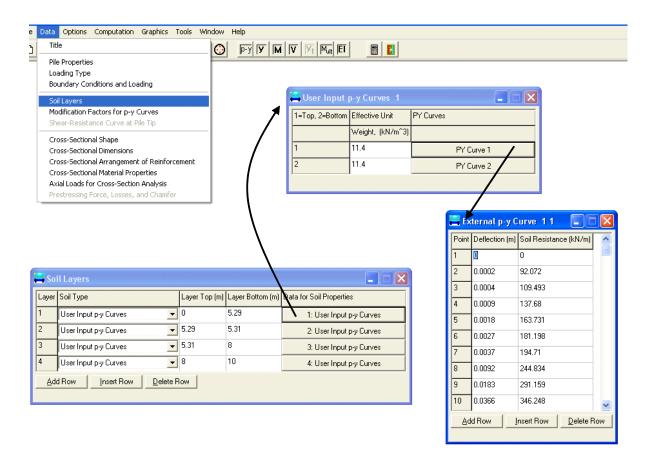


Figure 6-33. Modeling Soil Layers with Previously Determined p-y Curves.

For the P = 0 case, the shear capacity of the micropile ( $Q_{P=0}$ ) is calculated as 365 kN (82 k) and the maximum bending moment ( $M_{max}$ ) is calculated as 161.3 kN.m (119.0 k.ft). The  $M_{ult}$  for this axial load case was previously calculated as 161.3 kN.m (119.0 k.ft) (see Table 6-2).

For the  $P = P_{ult}$  case, the shear capacity of the micropile ( $Q_{P}=P_{ult}$ ) is calculated as 330 kN (74.2 k) and the maximum bending moment is calculated as 147.7 kN.m (108.9 k.ft). The  $M_{ult}$  for this axial load case was previously calculated as 147.7 kN.m (108.9 k.ft) (see Table 6-2).

For both axial load conditions,  $M_{max}$  is approximately equal to  $M_{ult}$  and the up/down analyses are considered to be complete. Therefore, both  $Q_{P=0}$  and  $Q_{P=Pult}$  can be used in the subsequent design steps to evaluate the shear capacity of battered micropiles.

## 6.7.7 STEP 10: Evaluate Shear Capacity of Battered Micropile Group

For this step, the maximum lateral force that the battered micropile group or pair (i.e., upslope micropile leg and downslope micropile leg as shown in Figure 6-9) (H_{ult-pair}) can resist at the location of the critical slip surface is evaluated (see Section 6.6.5).

In this design example, the batter angle for the upslope micropile leg is selected as  $3^{\circ}$  and the batter angle for the downslope micropile leg is selected as  $21^{\circ}$ . The  $H_{ult}$  for each leg is calculated as shown below:

For 
$$\psi_{us} = 3^{\circ}$$
,  $H_{ult (\psi us)} = Q_{P=0} = 365 \text{ kN } (82 \text{ k})$ 

For  $\psi_{ds} = 21^{\circ}$ ,  $H_{ult\;(\psi ds)}$  has to be interpolated.  $H_{ult\;(\psi ds)}$  calculated for various batter angles are shown in Table 6-3 and interpolation for  $\psi_{ds} = 21^{\circ}$  is shown in Figure 6-34.  $H_{ult\;(\psi us)}$  is evaluated as 450 kN (101 k).

Table 6-3. Hult (wds) for Various Batter Angles.

ψ _{ds} (degree)	H _{ult(}	Equations	
ψ _{ds} (degree)	(kN)	(k)	Equations
0	365	82	6-8
10	365	82	0-8
30	523	117.6	6-7
40	558	125.4	0-7

Therefore, according to Eq. 6-10:

$$H_{ult-pair} = H_{ult (\psi us)} + H_{ult (\psi ds)} = 365 + 450 = 815 \text{ kN } (183.2 \text{ k})$$

This is the calculated maximum lateral force that the micropile pair can resist at the location of the critical slip surface.

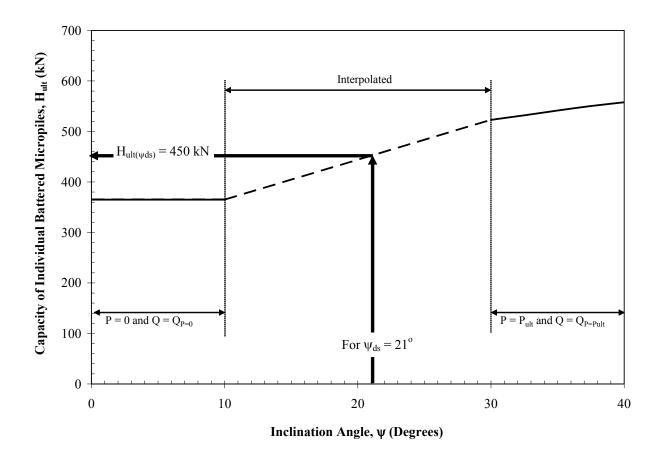
## 6.7.8 STEP 11: Calculate Spacing Required to Provide Force to Stabilize the Slope

The definition of spacing between two upslope micropiles and two downslope micropiles is presented in Figure 6-22 and is calculated using Eq. 6-11 as:

$$S_{\text{max}} = \frac{H_{\text{ult-pair}}}{H_{\text{req}}}$$

In the design example,  $H_{req}$  is calculated as 650 kN/m (44.5 k/ft) and  $H_{ult-pair}$  is calculated as 815 kN (183.2 k), therefore  $S_{max}$  is:

$$S_{max} = \frac{815 \text{ kN}}{650 \text{ kN/m}} = 1.25 \text{ m}$$



Note: 1 kN = 0.2248 k

Figure 6-34. Interpolation of H_{ult} for Battered Downslope Micropile Leg.

## 6.7.9 STEP 12: Check Potential Soil Flow between Micropiles

In this Design Step, the ultimate horizontal pile force ( $H_{ult\text{-soil/pile}}$ ) from a plastic flow analysis is compared to the average resistance provided by the upslope and downslope micropile pair ( $H_{ult\text{-pair}}/2$ ). This comparison is performed to check that  $S_{max}$  is adequate to prevent plastic soil flow above the critical slip surface between micropiles.

For the design example, Eq. 6-12 was developed in a spreadsheet format (Figure 6-35). The formulas used for each cell in the spread sheet are presented in Figure 6-36. The  $H_{ult-soil/pile}$  column in Figure 6-35 is the summation of soil resistance against plastic flow from the ground surface to the depth of slip surface. This is also shown graphically in Figure 6-37. In the design example the depth of the critical slip surface is 10 m. Therefore,  $H_{ult-soil/pile}$  is calculated for 10 m to be 753 kN (169.3 k).

For this design,  $H_{ult\text{-soil/pile}} = 753 \text{ kN } (169.3 \text{ k}) \ge H_{ult\text{-pair}}/2 = 407.5 \text{ kN } (91.6 \text{ k})$ . Therefore, plastic flow conditions are satisfied and the calculated  $S_{max}$  from Design Step 11 does not need to be reduced.

#### 6.7.10 STEP 13: Perform Structural Design of Concrete Cap Beam

The steel-reinforced CIP concrete cap beam spans and anchors the micropile array at the ground surface. The concrete cap beam is typically 2-m wide and 1-m deep, but, in general, the cap beam should have sufficient height and width to allow for at least two to three micropile diameters embedment into the cap beam to promote fixity of the upslope and downslope micropile. The structural design of the concrete cap beam follows typical methods for reinforced concrete (see Section 8 of AASHTO (2002)). Specific considerations involved in the design of a concrete cap beam include:

- Where ground anchors are used, the cap beam provides a reaction for the ground anchors to be installed and subsequently stressed and locked-off. The cap beam needs to be designed for these forces.
- Where ground anchors are not incorporated, axial loads transferred towards the ground surface should be small (particularly if the slide plane is relatively deep). Although these forces are postulated to be small, the provision of fixity of the micropile group at the cap beam will cause load transfer to the cap beam. Also, where the depth of the slide plane is relatively shallow, it is likely that bending moments in the cap beam may be on the order of bending moments calculated at the slide plane. For this case, soil-structure interaction analyses should be performed to evaluate bending moments for structural design of the cap beam.
- In some cases, relatively significant deflections of the cap beam may need to be considered in the structural design. That is, ground anchor stressing, non-uniform depth to competent material, and/or compression of soil material within the unstable soil mass may result in differential settlements of the length of the cap beam. The resulting bending stresses and torsional stresses from such movements should be considered in the structural design of the cap beam.

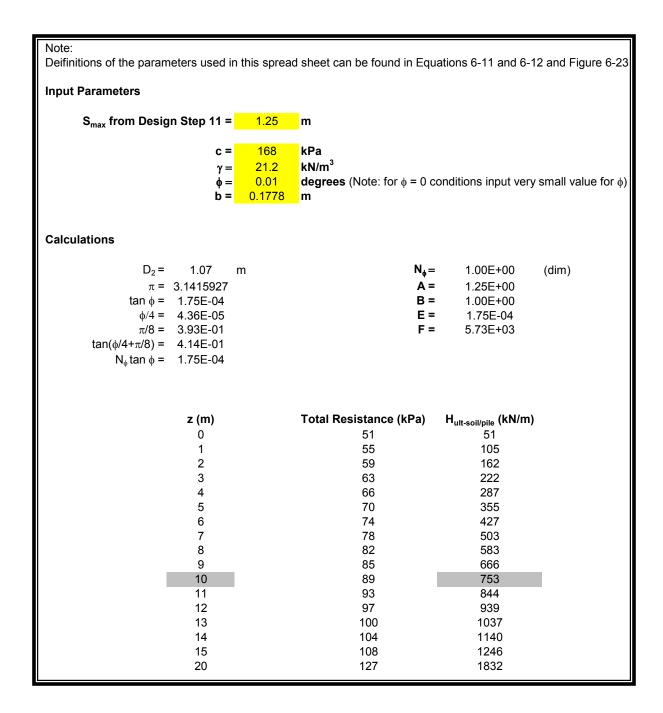


Figure 6-35. Spreadsheet Calculations Based on Eq. 6-12 to Obtain  $H_{ult\text{-soil/pile}}$  for the Example Problem.

7	A	В
1 Input Parameters	ers	
1 1	S _{max} from Design Step 11 = 1.25	1.25
യ	ï	89
0 1	ל	v= 21.2
. ∞	- <del>-</del>	= 0.01
6	<u>م</u> .	<b>b</b> = 0.1778
10		
12 Calculations		
2 4	D ₂ :	$D_2 = \$8\$4-\$8\$9$
15	, E	$\eta = = \Gamma(1)$
16	tan $\phi$ :	tan $\phi = = T  \text{AN}(\text{RADIANS}(\$B\$\$))$
17	φ/4 :	$\phi/4 = \text{RADIANS}(8\$8/4)$
200	: 8/E	7.18 = 1845.15.18
20	tan(∲/4+π/8) N _∲ tan φ :	$(\phi/4+\pi G) = 1$ AN $(\psi/4+\pi G) $
22	Ž	N _b = =TAN((\$B\$15/4)+(RADIANS(\$B\$8/2)))^2
23	` ₹ ¤	A = =(\$B\$4)*(\$B\$4/\$B\$14)^((\$B\$22^0.5*\$B\$16+\$B\$22-1)) B = EY/((\$P\$4.\$P\$11/\$P\$41.**\$P\$77*\$P\$70**
7 7 7 7 8 7	, iii iii	E = (\$8\$22^0.5)*88\$16 F = ((2*\$8\$16)+(2*(\$8\$22^0.5))+(\$8\$22^0-0.5))/(\$8\$25+\$8\$22-1)
28 29 30 5 31 10	Ê.	Otal Kesistance (KPa)  =((\$B\$23*\$B\$6*((1/(\$B\$22*\$B\$16))*(\$B\$24-(2*\$B\$25)-1)+\$B\$26))}\$B\$6*(\$B\$4*\$B\$26-2*\$B\$14*\$B\$22^0.0.5)+(((\$B\$7*A29)\$B\$22)*(\$B\$23*\$B\$24-\$B\$14))  =((\$B\$23*\$B\$6*((1/(\$B\$22*\$B\$16))*(\$B\$24-(2*\$B\$25)-1)+\$B\$26))}\$B\$6*(\$B\$4*\$B\$26-2*\$B\$14*\$B\$22^0.0.5)+(((\$B\$7*A30)\$B\$22)*(\$B\$23*\$B\$24-\$B\$14))  =((\$B\$23*\$B\$6*((1/(\$B\$22*\$B\$16))*(\$B\$22-(2*\$B\$25)-1)+\$B\$26))}\$B\$6*(\$B\$4*\$B\$26-2*\$B\$14*\$B\$22^0.0.5)+(((\$B\$7*A31)\$B\$22)*(\$B\$23*\$B\$24-\$B\$14))
32 15 34 20		=((\$B\$23*\$B\$6*((1/(\$B\$22*\$B\$16))*(\$B\$24-(2*\$B\$25}-1)+\$B\$26))}\$B\$6*(\$B\$4*\$B\$26-2*\$B\$14*\$B\$22^-0.5)+(((\$B\$7*A32)\\$B\$22)*(\$B\$23*\$B\$24-\$B\$14)) =((\$B\$23*\$B\$6*((1/(\$B\$22*\$B\$16))*(\$B\$24-(2*\$B\$25)-1)+\$B\$26))}\$B\$6*(\$B\$4*\$B\$26-2*\$B\$14*\$B\$22^-0.5)+(((\$B\$7*A33)\\$B\$22)*(\$B\$23*\$B\$24-\$B\$14))
35 o z (m)	Œ.	Hutsolipie (KN/m) = B29
37 5		=B36+0.5*(A30-A29)*(B30+B29)
39 15 39 15		=B37+0.5°(A31-A30)°(B31+B30) =B38+0.5°(A32-A31)*(B32+B31)
40 20		=B39+0.5*(A33-A32)*(B33+B32)

Figure 6-36. Equations Used in Each Cell in Figure 6-35.

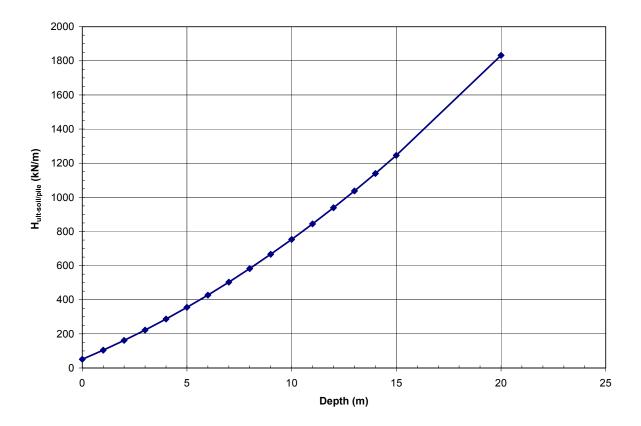


Figure 6-37. Graphical Solution for H_{ult-soil/pile} Based on Figure 6-36.

## **Summary of the Design Example**

- Type A gravity-grouted micropiles comprising API-N80 casing with OD._{casing} = 177.8 mm embedded 4.5 m (15 ft) into bedrock are used.
- The upslope micropile leg is battered at 3 degrees and the downslope micropile leg is battered at 21 degrees. Individual micropiles in each pair should be constructed as close to each other as possible with just large enough space to permit ease of construction.
- The spacing between two upslope micropiles and two downslope micropiles should be no more than 1.25 m.
- All of the micropiles should be connected at the ground surface via a concrete beam.
- For verification load testing, micropiles with a 4.5-m (15-ft) long bond length in rock (below the slip surface) should be tested to 950 kN (213 kips) (i.e., 2.0 × the calculated axial resistance for the micropile above the slip surface). For proof load testing, micropiles should be tested to 760 kN (171 kN) (i.e., 1.6 × the calculated axial resistance for the micropile above the slip surface). Load testing requirements are presented in Chapter 7.

#### 6.8 SHEAR CAPACITY OF MICROPILES FOR ANALYSIS

As previously noted, the shear load that an individual micropile provides is assumed to correspond to the maximum shear force in the micropile when the micropile has reached its ultimate bending capacity. The rationale for this is explained below.

A slope that has failed (i.e., some movement has been observed and may have stopped or continuous or intermittent movements being measured) implies that its slope stability factor of safety is equal to 1.0. Since the design of the micropile-stabilized slope is predicated on good knowledge of the position of the failure surface and the pore pressures in the slope at the time of failure, then the loads and soil resistances are reasonably well-known, and, in fact, are equal in magnitude to each other (i.e., the FS = 1.0 condition requires this).

The analysis now requires that the slope be stabilized to a target factor of safety (e.g., FS = 1.3). Using the shear strengths obtained from the back-analysis of a failed slope, a shear force (provided by the micropile) is added until the target factor of safety for the slope is calculated. It is recommended that this shear force be added to the resisting forces (or moments) in the limit equilibrium calculations (as compared to treating it as a negative driving force or moment).

In an allowable stress design format, the service loads on the micropile are equal to zero since the slope is "stable" at a FS of 1.0. In a retaining wall, for example, the service loads on the wall for the FS = 1.0 condition are not zero and may be associated with full active earth pressure conditions.

To increase the factor of safety of the slope, micropiles are added. In the design, it is assumed that, if the ultimate shear capacity of the micropiles was mobilized at a limit (i.e., failure) state, the factor of safety of the slope would be at 1.3. This approach is exactly consistent with reinforced slope design. In that case, the design strength of the reinforcement corresponds to its strength at a specific design life, T_{al} and then slope stability analyses are performed to verify a target factor of safety for the slope. As for the micropile analysis described herein, no reductions to some allowable stress (or strength) are used. Whereas, the reinforced slope soil reinforcement strength is reduced to account for creep, durability, and construction damage, the strength of the micropile may be reduced to account for potential steel loss due to corrosion.

A design engineer may incorporate additional conservatism in a project if warranted. For example, additional conservatism may be prudent if the failure slip surface and/or residual soil shear strength are not well understood for a particular slide or if the soil within the failure slip surface has the potential for continued long-term creep movements. Additional

conservatism may be incorporated through selection of soil properties, phreatic surface assumptions, value of target slope stability factor of safety, maximum micropile shear force, or a combination of these. Note that a probabilistic analysis can be performed to examine slope stability factor of safety values for ranges of material parameters (see Duncan et al., 1999), and that this can provide a better understanding of the effect of material parameters.

## 6.9 CASE HISTORIES

## 6.9.1 Stabilization of Blue Trail Landslide Using Micropiles, Wyoming

The Blue Trail Landslide project is located on U.S. Highway 26/89 between Alpine Junction and Hoback Junction, Wyoming. This section of roadway is next to the canyon of the Snake River (Figure 6-38). This highway was constructed between 1955 and 1960 and had experienced episodes of movement resulting from movement of the landslide. Throughout the years, various remedial design alternatives were reviewed to mitigate slope movements and to stabilize the slide to a desired factor of safety of 1.3. Alternatives considered included regrading the slope and constructing a toe berm, constructing a bridge over the entire slide area, and installing drilled shafts near the toe of the landslide to provide structural restraint (Hasenkamp, 1999). These alternatives were rejected for implementation because they were not cost effective. Ultimately, micropiles were selected for implementation since they were less expensive that other alternatives and could be constructed in highly variable ground and under restricted access conditions. Other advantages included the ability to maintain traffic during construction and minimal environmental impacts.

The design of the micropiles was performed using the design approach described in this chapter. Originally, two micropile walls (i.e., two sets of upslope and downslope micropiles) and a mechanically stabilized earth (MSE) wall were designed to stabilize the slope (Figure 6-39). The first wall was located 3 m below the roadway (i.e., upper wall) and the second one was located approximately between the road and the toe of the slide (i.e., lower wall). At a later time, a third wall was added along the western edge of the project at about 12 m (39 ft) below the roadway to increase the factor of safety of the slope at that location. The original design included a single ground anchor at each wall location. During the early stages of construction, it became necessary to significantly increase the restraining force provided by the lower wall. This was the result of a significant increase in the seismic coefficient that was required by a reviewing agency. This was accomplished by significantly increasing the capacity of the ground anchors in the lower wall. Micropiles were battered 30 degrees from the vertical and ranged in length from 19 to 34 m (62 to 112 ft). Ground anchors were installed at 30 degrees from the horizontal (see Figure 6-40).

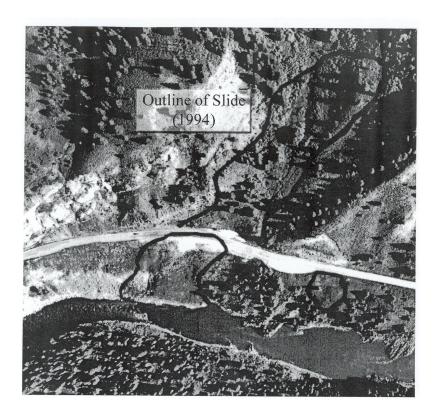


Figure 6-38. Extent of Blue Trail Landslide (after Hasenkamp, 1999).

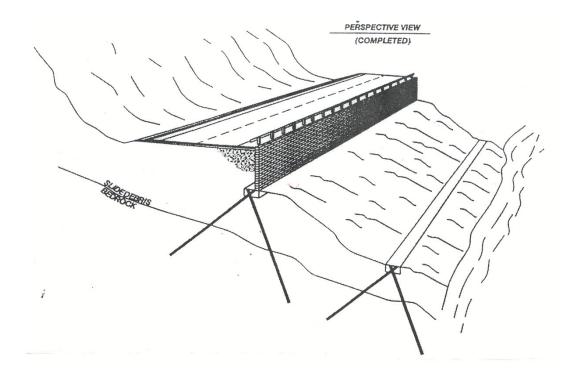


Figure 6-39. Conceptual Design Drawing of the MSE and NRM Walls for Blue Trail Landslide Project (after Hasenkamp, 1999).

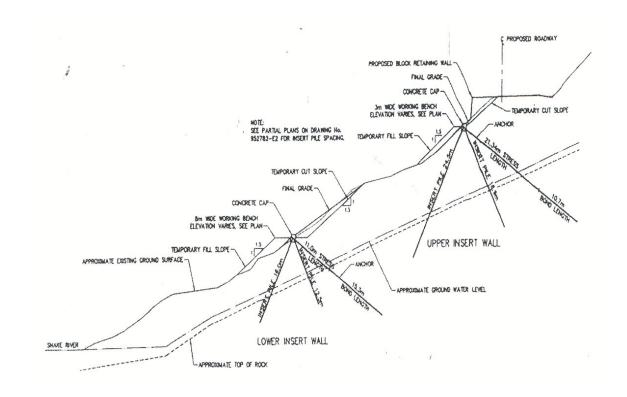


Figure 6-40. Typical Section of Micropile and Ground Anchor Wall for Blue Trail Landslide Project (after Hasenkamp, 1999).

The Blue Trail landslide was the first project in Wyoming in which micropiles and ground anchors were used to create a permanent landslide stabilization system. A comprehensive instrumentation and monitoring program was developed to assess the field performance of the walls. Instrumentation consisted of slope inclinometers, survey monuments, tilt plates, strain gauges attached to micropile steel casings, load cells attached to four ground anchors, and piezometers. Information collected included: (1) wall and slope movement; (2) load transfer to the micropiles and ground anchors; and (3) pore water pressures in the slide material (Hasenkamp, 1999).

The construction sequence followed installation of micropile walls and then ground anchors. In each case, the lower wall was built first, upper wall was built second, and middle wall was built last. A total of 478 micropiles and 40 ground anchors were installed to stabilize the slope. Instrumentation data indicated that this stabilization approach was effective in significantly reducing slope movements. Measured axial loads in the micropiles were less than those assumed in the design (Table 6-4). Measured maximum bending moments ranged from approximately 8 to 80 percent (average 30 percent) of the ultimate bending moment capacity for the steel pipe of the micropiles (Table 6-4). These results indicate that wall

performance was acceptable. The direction of axial load and bending moments in the micropiles of the lower wall was opposite to that assumed in the design. This resulted from the significant lock-off loads within the lower wall ground anchors. Micropiles in the upper wall showed compression for both the upslope and downslope directions. This is most likely the result of surcharge load associated with placement of the MSE wall and roadway over the upper insert wall.

Table 6-4. Comparison of Actual Loads to Design Loads for Blue Trail Landslide Project (after Hasenkamp, 1999).

Wall	Micropile Number	Micropile Orientation	L (m)	$P_{Design} (kN)^{(1)}$	$P_{\text{Measured}}$ $(kN)^{(1)}$	$M_{ult ext{-}Design}$ (kN-m)	M _{ult-Measured} (kN-m)
	62	Upslope	23.8	635	-686	35.2	15.4
Upper	63	Downslope	33.5	-894	-566	35.2	3.3
	123	Downslope	27.7	-739	153	35.2	4.0
	124	Upslope	23.8	635	-302	35.2	14.6
Lower	326	Downslope	19.2	-717	214	35.2	8.5
	327	Upslope	19.5	728	-594	35.2	2.9
	402	Downslope	19.5	-728	398	35.2	3.2
	403	Upslope	19.5	728	-450	35.2	3.8

Notes: (1) Negative values indicate compression.

 $P_{Design}$  and  $P_{Measured}$ : Design axial load and axial load measured in the field, respectively.

 $M_{ult\text{-}Design}$  and  $M_{ult\text{-}Measured}$ : Ultimate bending moment of micropile section and bending moment measured in the field, respectively.

#### 6.9.2 Stabilization of Sum-271 Landslide Using Micropiles, Ohio

The SUM-271 project is located on Interstate 271 northbound in Richfield Township, Summit County, Ohio. The site consists of approximately 21 m (70 ft) of valley fill overlying relatively thin and weak layers of normally consolidated fine grained lacustrine soils with strong overconsolidated lacustrine soils beneath. Over the years, slope movements resulted in pavement settlement and cracking. Two alternatives were considered for stabilization. One alternative consisted of regrading the slope and constructing toe buttress berms and the other alternative included using micropiles (Liang, 2000). The Ohio Department of Transportation (ODOT) selected the micropile option.

L: Length of the micropile.

The design of the micropiles was performed using the design approach presented in this chapter. Because micropiles were not able to completely develop the resisting forces required, ground anchors were added to the design. The wall consisted of 154 type A micropiles that were spaced 1.2- to 1.8-m (4- to 6-ft) apart and battered 30 degrees from the vertical and 41 ground anchors that were spaced 3.5 m (12 ft) apart and battered 30 degrees from the horizontal (Figure 6-41).

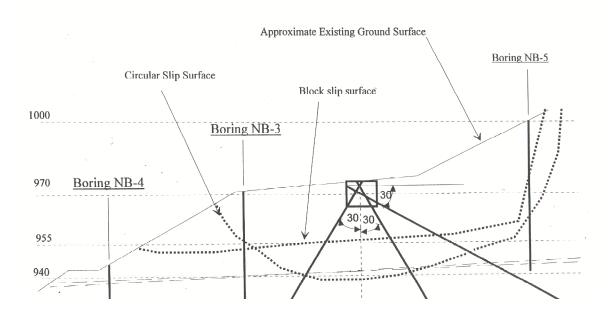


Figure 6-41. Typical Section of Micropile and Ground Anchor Wall at SUM-271 (after Liang, 2000).

A comprehensive instrumentation and monitoring program for the wall was developed for this project. Inclinometers were installed in the slope to monitor slope movement and strain gauges were attached to the micropiles to allow for measurements of axial loads and bending moments in the micropiles throughout construction. High capacity load cells were used to monitor ground anchor loads. Inclinometer data indicated that the installation of the NRM wall and ground anchors was effective in arresting the slope movement.

As part of this project, detailed finite element analyses were performed to model the wall behavior (Liang, 2000). These analyses simulated relevant stages of construction including earthwork, pile cap construction, drilling, and installation of micropiles and stressing of the ground anchors. Finite element analysis results were compared to field instrumentation monitoring data to validate the capability of the FEM modeling technique and to provide supplemental information. Based on the finite element analysis results and field

measurements of wall performance, the following observations and conclusions were developed:

1. The maximum axial force in each micropile occurred at the location near the slip surface of the slope (i.e., approximately 30 ft below the ground surface) (Figure 6-42). The direction and magnitude of the axial forces in the micropiles were consistent with loading conditions resulting from the various stages of construction. For example, the upslope micropile was initially in tension (following installation). When the ground anchor was tensioned, a portion near the top of the upslope micropile remained in tension, while the remaining portion of the wall was in compression. The axial forces in the downslope micropile were initially in compression but after the ground anchor tensioning, the compressive forces were reduced. However, no tension was developed in the downslope micropile.

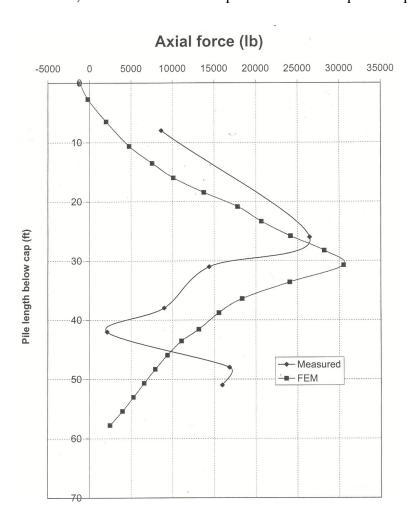


Figure 6-42. Comparison of Axial Loads for the SUM-271 Project (after Liang, 2000).

2. The bending moments were near zero at the location where the maximum axial forces occurred (Figure 6-43). The change in bending moments throughout the construction stages were small and were primarily due to small stiffness of the micropiles. The magnitude of the maximum bending moments was reasonably predicted by the finite element analyses.

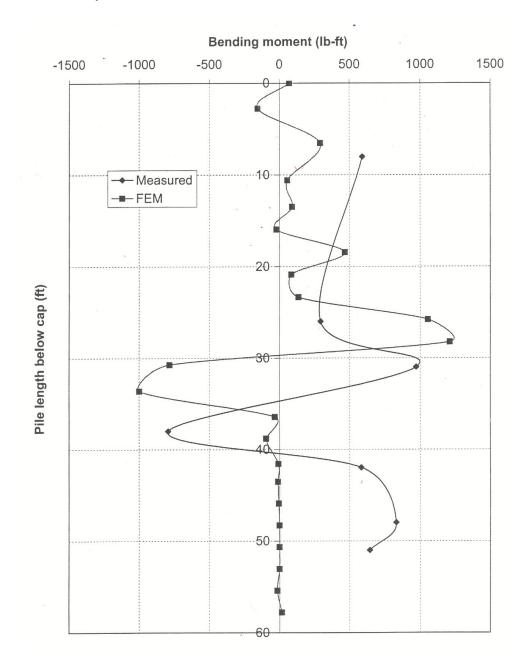


Figure 6-43. Comparison of Bending Moments for the SUM-271 Project (after Liang, 2000).

## 6.9.3 Stabilization of Littleville Landslide using Micropiles, Alabama

The Littleville landslide is located on a section of US Route 43, Alabama. The area of the landslide is a fill composed of sandstone and shale cut from adjacent hillsides. The underlying stratum is shale with some weathering along the top surface, which is believed to be the failure surface. A highway was constructed at the site in the 1950s. Soon after construction of the original roadway was finished, stability problems arose and the road surface dropped due to slides in the fill material. Initially the holes were filled and the road was repaved. In the 1970s, the roadway was widened and the slope was flattened. However, ensuing rainy periods brought on the onset of more slope failures. The creep of the slope continued until a micropile wall with additional stabilization provided by ground anchors was built in 1997 to stabilize the slope (Brown and Chancellor, 1997).

The design of micropile wall was performed following the same approach as is described in this chapter. A typical cross section of the slide and the reinforcement installed at the site are provided in Figure 6-44. The micropiles included 114-mm (4.5 in.) diameter steel casing with a wall thickness of 8 mm. Micropile design lengths were 7 m (23 ft) and were battered 30 degrees from vertical. A total of 432 micropiles and 44 ground anchors were installed for the project.

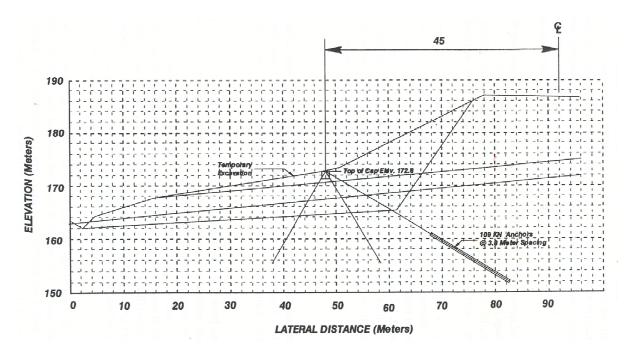


Figure 6-44. Typical Section of Micropile and Anchor Wall at Littleville, Alabama (after Brown and Chancellor, 1997).

Instrumentation data was collected for a period of two years. Data collected included inclinometer measurements of slope movement, pore water pressures, and stresses developed in the micropiles and anchors. Piezometers have shown relatively stable water levels over the two years with a fluctuation of approximately two or three feet.

Inclinometer data indicated that slope movement had effectively ceased as a result of the slope stabilization measure. Analysis of the strain gauge data indicated that this was accomplished without approaching potential failure conditions in the micropiles. The axial forces mobilized in the micropiles were found to be below the estimated ultimate axial load by a factor of approximately two, and the factor of safety was calculated to be approximately 1.3 as originally estimated. In addition, it was found that the upslope battered micropiles were in tension in the vicinity of the slide plane and the downslope battered piles were in compression. The strain gauges also indicated higher bending moments developed in the micropiles in the vicinity of the slide surface. Measured maximum bending moments ranged from approximately 5 to 9 percent of the ultimate bending moment capacity of the micropiles. Loads in the ground anchors were observed to decrease slightly over time and this was attributed to small movements that have occurred in the uphill direction.

#### 6.10 REFERENCES

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# CHAPTER 7 MICROPILE LOAD TESTING

#### 7.1 INTRODUCTION

On micropile foundation support projects and slope stabilization projects, "verification" load testing is performed on pre-production micropiles. The purpose of the pre-production testing is to verify design assumptions concerning bond zone strength and the adequacy of the contractor's installation methods. This testing is usually performed as the first order of work under the construction contract. Production micropiles are approved only after the design assumptions and the adequacy of the contractor's installation method have been verified. On large projects, additional load testing may be performed during the design stage under a separate contract.

The ability of the micropile to safely carry the design load in service is obtained through "proof" load testing on selected production micropiles. This proof testing provides a quality assurance means to confirm micropile installation procedures.

Micropiles are tested individually using the same conventional static load testing procedures as are used for driven piles and drilled shafts. These tests include incremental loading (which may be applied in compression, tension, or laterally and which may be cycled (i.e., load/unload)) until the micropile reaches the selected maximum test load, structural displacement limit, or ground creep (i.e., movement under constant load) threshold.

In this chapter, descriptions of "verification" and "proof" tests for micropiles are provided with information on typical testing equipment, schedule for load increments, and analysis of load-deformation data as a means to judge micropile acceptance for payment purposes.

#### 7.2 OVERVIEW OF MICROPILE LOAD TESTING

Micropiles are load tested in the field to verify that the required design loads can be carried without excessive movement and with an adequate factor of safety for the life of the structure. Load testing is also used to verify the adequacy of the contractor's drilling, installation and grouting operations prior to (verification testing) and during (proof testing) construction of production micropiles. Therefore, the ground conditions, as well as the method, equipment, and operator used for installing production piles must be similar to those

used for installing the test micropiles. If ground and/or installation procedures change from that used from the verification load testing program, additional testing should be required. If test results indicate faulty construction practice, or grout-to-ground load capacities less than required, the contractor may be required to modify the micropile installation methods. In the event that the required design grout-to-ground bond capacities are still not achievable, redesign may be necessary.

Load testing criteria will be included in the construction specifications and will typically include *ultimate* and/or *verification* tests. These tests usually require loading to a maximum test load that includes the factor of safety assigned to the design grout-to-ground bond (i.e., the verification test) and/or that which results in failure defined as the inability to maintain constant test load without excessive micropile movement (i.e., the ultimate test). The ultimate tests, taken to failure, are usually only specified as part of a research project or on very large projects where a design phase test program can be justified. The design phase test program will allow the micropile design to be optimized. On typical projects, one or two verification tests are commonly conducted prior to beginning production pile installation, and then one or more additional such tests may be conducted in each significantly different ground type encountered as construction proceeds. A larger number of verification tests may be specified for larger projects. The minimum required number of verification load tests to be performed for a project is provided in Section 7.6.2. Since ultimate and verification tests are typically carried to relatively high loads, in many cases these micropiles will not be used as part of the final structure, i.e., they are "sacrificial" micropiles.

During installation of production micropiles, "proof" testing is conducted on a specified number of the total production piles installed. Proof tests are performed on production piles that will be incorporated into the structure provided the maximum test loads are less than those required to cause geotechnical or structural failure and which do not result in damage to the micropile. Recommendations on minimum number of proof tests to be performed for various applications are provided in Section 7.6.3.

Creep tests are performed as part of verification and proof tests. Creep testing procedures are similar to the creep test used for ground anchors and soil nails. Creep is primarily of concern in organic soils and cohesive (clayey) soils with a liquid limit greater than 50 and a plasticity index greater than 20. The creep test consists of measuring the movement of the micropile at constant load over a specified period of time. This test is used to assess whether pile design loads can be safely carried throughout the project service life.

## 7.3 LOAD TESTING EQUIPMENT

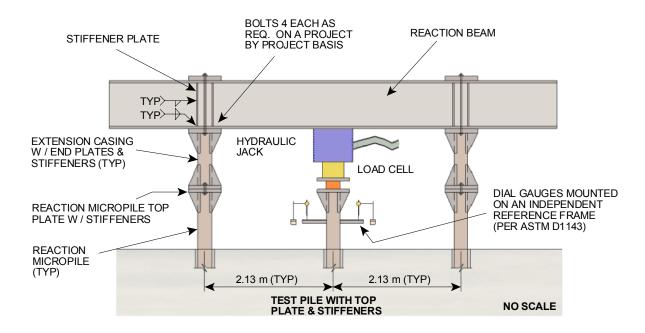
#### 7.3.1 General

The equipment and load testing methods used for micropiles are the same as those used for conventional load testing of driven piles and drilled shafts as codified in ASTM D 1143 for compression loading, ASTM D 3689 for tension loading, and ASTM D 3966 for lateral loading. Typical load test setups for compression, tension, and lateral load applications are shown in Figures 7-1, 7-2, and 7-3, respectively. Typical load testing equipment includes: (1) hydraulic jack and pump; (2) reaction and reference beams; (3) pressure gauges and load cells; (4) dial gauges; and (5) wire with mirror and scale.

## 7.3.2 Load Testing Equipment

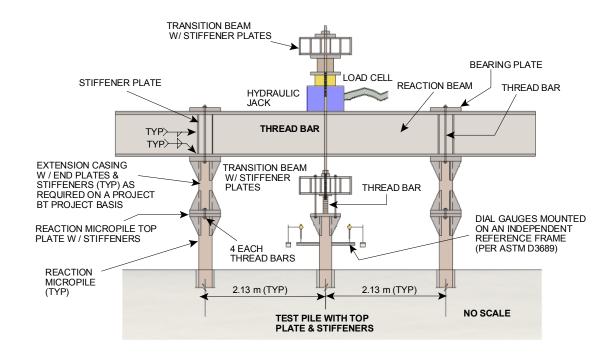
The most common and convenient system includes a hydraulic jack and reaction arrangement. For compression testing, the load is applied by hydraulically jacking against a beam that is anchored by piles, micropiles, ground anchors (Figure 7-4), or by jacking against a weighted platform. For tension tests, loads are applied by centering the hydraulic jack on top of a test beam and jacking against a reaction frame connected to the micropile to be tested (Figure 7-5). The test beam may be supported by cribbing. For lateral load tests, lateral loads are applied by a hydraulic jack against a reaction system or by a hydraulic jack acting between two piles (Figure 7-6). With the latter method, two micropile lateral load tests can be performed simultaneously.

The standard device used to monitor load is a pressure gauge attached to the jack pump. The readings on the jack pressure gauge are used to determine the absolute value of applied load. Calibration of pressure gauges should be performed within 45 working days of the date when they are submitted for approval for the project. Calibration certifications and graphs for pressure gauges and load cells must be provided by the contractor before use. An example of a typical pressure gauge calibration curve is given in Figure 7-7. A second certified pressure gauge, which is called master gage, should be kept on-site to be used for periodic check of jack pressure gauges.



Note: 2.13 m = 7 ft

Figure 7-1. Schematic of Compression Load Test Arrangement (ASTM D1143).



Note: 2.13 m = 7 ft

Figure 7-2. Schematic of Tension Load Test Arrangement (ASTM D3689).

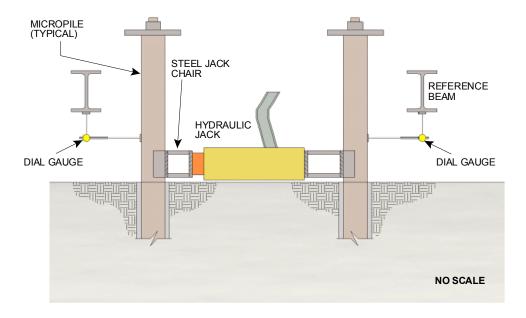


Figure 7-3. Schematic of Lateral Load Test Arrangement.



Figure 7-4. Compression Load Test Set-Up.

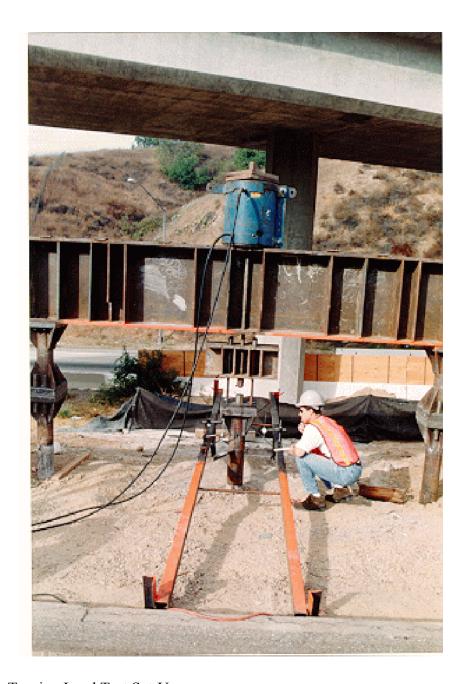
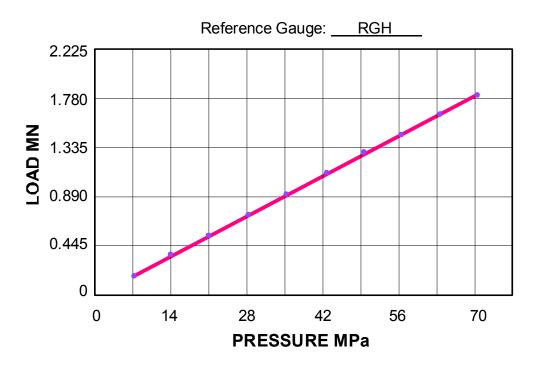


Figure 7-5. Tension Load Test Set-Up.



Figure 7-6. Photograph of Lateral Load Test Set-Up (Note: Two micropiles are tested simultaneously).



Note: 1 MN = 224.8 k and 1 MPa = 145.1 psi

Figure 7-7. Typical Pressure Gauge Calibration Curve.

Calibrated load cells should be used to verify that load remains constant during portions of an ultimate (and/or verification) load test in which the load is held for a specified period of time. When load cells are used, care should be taken to ensure that the cell is properly aligned with the axis of the micropile and jack. Load cells are used mainly to detect small changes in load and allow load adjustment and maintenance of constant holding load. As an example, assuming that the load cell reads "440" once the creep test load is reached, it is important that the "440" reading on the load cell be maintained through jack pressure adjustments for the duration of the test. This provides assurance that a constant load was indeed maintained throughout the creep test. It is specifically noted that load cells are not required for proof tests (except for extended creep testing, if needed to judge acceptability of proof-tested micropile).

Vertical and/or lateral movement of the micropile head is typically measured using a dial gauge and/or LVDT fixed to the reference beams. Dial gauges should be capable of measuring and being read to the nearest 0.025 mm (0.001 in). For an axial load test, the gauges are mounted on an independent reference beam whose supports are located at a distance of five times the diameter of the test micropile. The minimum allowable distance between the gauges and the test micropile is 2.13 m (7 ft) as shown in Figures 7-1 and 7-2.

The readings from three gauges are averaged to compensate for possible rotation of the pile head. The gauges are placed around the pile at an equal distance from the pile center.

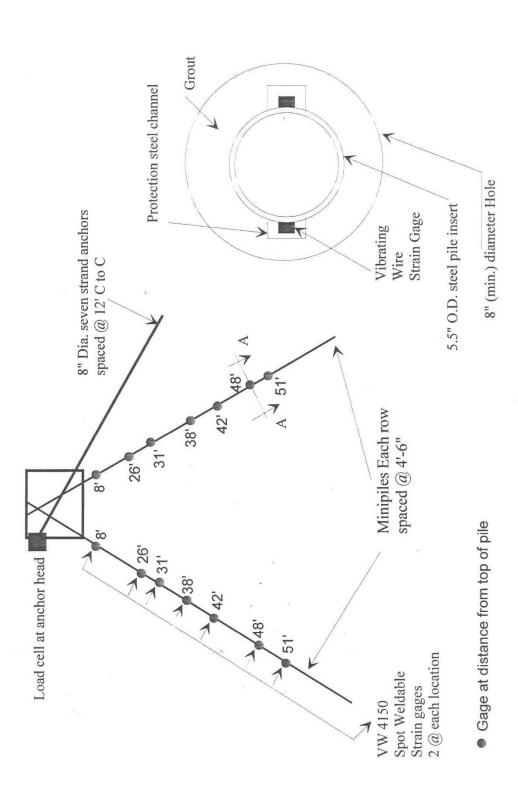
Micropile top displacement may be determined using a mirror with a scale mounted on the pile, and a wire mounted on a separate reference strung in front of the scale. The scale is read by adjusting the line of sight until the wire lines up with its reflection. This method should only be used as a backup to the dial gauge system, but it is less sensitive.

Although not usually required, axial displacement in micropiles can be measured at discrete elevations in a micropile using telltales. Telltales consist of metal or fiberglass rods that are anchored into the micropile grout. The rod tip is embedded into the grout at the point of interest, with the remainder sheathed to allow free movement of the micropile. Movement at the top of the rod is measured with a dial gauge or electronic measuring device. Multiple telltales can be installed to measure movement at several points. Care must be taken to avoid damage to the telltales during micropile installation, such as the rods becoming damaged during drill string rotation, or the sheath becoming partially filled with grout.

Strain gauges may be mounted on the reinforcing steel, allowing measurement of the level of strain in the reinforcement at various levels in the pile. Care must also be taken to avoid damage to the gauges and connecting wires during installation. If used, vibrating-wire-type strain gauges are recommended. From these strain measurements, axial load distribution

with depth can be determined. Measurements from strain gauge pairs located diametrically opposite each other on a micropile steel casing are used to evaluate micropile bending moments with depth (see Figure 7-8 as an example).

For lateral load testing, it is recommended to install an inclinometer in the micropile to obtain micropile lateral movement data with depth. This can be accomplished by installing the inclinometer to a depth of 10 to 20 micropile diameters. Specific termination depth should be based on lateral pile analyses performed during design.



Note: 1 in = 25.4 mm and 1 ft = 0.30 m

Figure 7-8. Strain Gauge Locations on Micropiles for SUM-271 Project (after Liang, 2000).

## 7.4 MICROPILE LOAD TESTING PROCEDURES

#### 7.4.1 Verification Tests

## 7.4.1.1 General

For verification tests, loads can be applied in compression, tension, or laterally. The maximum test load for a compression or tension test are typically defined by the grout-to-ground bond factor of safety used in design. For micropiles, the maximum verification test load will usually be 2.0 to 2.5 times the design axial (compression or tension) load. For lateral load tests, tests are performed to 2.0 times the design lateral load. Acceptance criteria based on load test results is provided in Section 7.4.3.

## 7.4.1.2 Procedures for Verification Test

Micropile verification testing is conducted by incrementally loading and unloading the micropile and measuring the movement of the micropile head at each load increment. The micropile-head movement reading is recorded just after the load has been applied and a second reading after the load has been maintained for a sufficient amount of time to ensure that pile-head movement has stabilized.

The load schedule for a verification test is shown in the first three columns of Table 7-1 and is consistent with the loading schedule codified in DFI (2004). The first step in a verification test comprises applying a nominal load to the micropile head. This load, termed the alignment load (AL), is typically no more than ten percent of the design load and its purpose is to ensure that the stressing and testing equipment are properly aligned. The displacement measuring equipment is zeroed upon stabilization of the AL as shown on the loaddisplacement curve in Figure 7-9. During the first load cycle, the load is raised to 15 percent of the design load and the incremental movement is recorded. The load is then reduced back to the alignment load. This procedure is repeated, using load increments as shown on Table 7-1, until the maximum testing load, referred to as the test load, is achieved. At the test load, a constant load is held for ten minutes prior to reducing the load. The load is assumed to remain reasonably constant if the deviation from the test pressure does not exceed 0.35 MPa (50 psi). During this ten minute load hold period, movements are measured and recorded at 1, 2, 3, 4, 5, 6, and 10 minutes. The purpose of this load hold is to measure time-dependent (i.e., creep) movements of the micropile. This portion of the verification test is referred to as creep test. If the total movement between 1 and 10 minutes exceeds the specified maximum creep movement, the test load is maintained for an additional 50 minutes and total movement is recorded at 20, 30, 40, 50 and 60 minutes.

# 7.4.1.3 Recording of Verification Test Data

The magnitude of each load is determined from the jack pressure gauge and the load cell measurement. The load-deformation data obtained for each load increment in a verification test are plotted as shown in Figure 7-10. The total movement ( $\delta_t$ ) is recorded at each load increment and for the alignment load. This total movement consists of elastic movement and residual movement. The residual movement for a given increment of load is the movement that corresponds to the net "irrecoverable" movement that occurs upon application of a load increment and the subsequent reduction of the load to the alignment load (see Figure 7-9 for definition of  $\delta_{r4}$ ). Residual movement ( $\delta_r$ ) includes elongation of the micropile and movement of the entire micropile through the ground. Elastic movement is simply the arithmetic difference between the total movement measured at the maximum load for a cycle and the movement measured at the alignment load (see Table 7-1). Although not used for micropile acceptance, residual movement is an indicator of the stress-strain behavior of the ground-to-grout bond in the micropile bond zone. Residual movement data should be collected and used for future testing or future design projects (in similar ground and load conditions) to estimate movements of the micropile within the bond zone.

During the creep test portion of the verification test, the movement measured at specified times (i.e., 1, 2, 3, 4, 5, 6, and 10 minutes) is recorded. The time at which the total movement is measured for the test load (i.e., time at which 1.30 DL is applied as shown in Figure 7-9) represents the start time for the creep test. The movement from one to ten minutes after this starting time is recorded and compared to the acceptance criterion for creep. If the creep acceptability criterion is not satisfied, the test load is held on the micropile for an additional 50 minutes. The total amount of movement between 6 and 60 minutes is recorded and compared to specified criteria.

Table 7-1. Verification Test Load Schedule (after DFI, 2004).

1		Load		Plot Total	Plot Residual	Movement
			Time (min)	Movement	Movement	Wiovement
			( )	$(\delta_{\rm ti})$	$(\delta_{ri})$	$(\delta_{ m ei})$
2	Apply AL		2.5	,		
2	Cycle 1	0.15DL	2.5	$\delta_1$		
		0.30DL	2.5	$\delta_1$		
		0.45DL	2.5	$\delta_{t1}$		
		AL	1		$\delta_{r1}$	$\delta_{t1}$ - $\delta_{r1}$ = $\delta_{e1}$
3	Cycle 2	0.15DL	1	$\delta_2$		
		0.45DL	1	$\delta_2$		
		0.60DL	2.5	$\delta_2$		
		0.75DL	2.5	$\delta_2$		
		0.90DL	2.5	$\delta_2$		
		1.00DL	2.5	$\delta_{t2}$		
		AL	1		$\delta_{r2}$	$\delta_{t2}$ - $\delta_{r2}$ = $\delta_{e2}$
4	Cycle 3	0.15DL	1	$\delta_3$		
		1.00DL	1	$\delta_3$		
		1.15DL	2.5	$\delta_3$		
		1.30DL	$\delta_{t3}$ , zero re creep test	eading for		
5	Hold load for at least 10 minutes while recording movement at specified times. If the total movement measured during the load hold exceeds the specified maximum value then the load hold should be extended to a total of 60 minutes.					
6	Cycle 3 cont'd.	1.45DL	2.5	$\delta_3$		
		AL	1		$\delta_{\rm r3}$	$\delta_{t3}$ - $\delta_{r3}$ = $\delta_{e3}$
7	Cycle 4	0.15DL	1	$\delta_4$		10 10
		1.45DL	1	$\delta_4$		
		1.60DL	1	$\delta_4$		
		1.75DL	2.5	$\delta_4$		
		1.90DL	2.5	$\delta_4$		
		2.00DL	10	$\delta_4$		
		1.50DL	5	$\delta_4$		
		1.00DL	5	$\delta_4$		
		0.50DL	5	$\delta_4$		
		AL	5		$\delta_{\rm r4}$	$\delta_{t4}$ - $\delta_{r4}$ = $\delta_{e4}$
8	Remove the load and compare results to acceptance criteria.					

Notes:  $AL = Alignment \ Load, \ DL = Design \ Load, \ \delta_i = total \ movement \ at \ a \ load \ other than maximum for cycle, i = number identifying a specific load cycle. Total movement is typically recorded from several dial gauges and the average movement is recorded.$ 

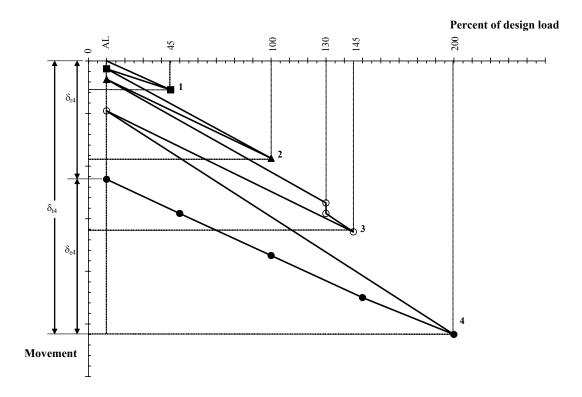


Figure 7-9. Load Displacement Curve of Verification Tests.

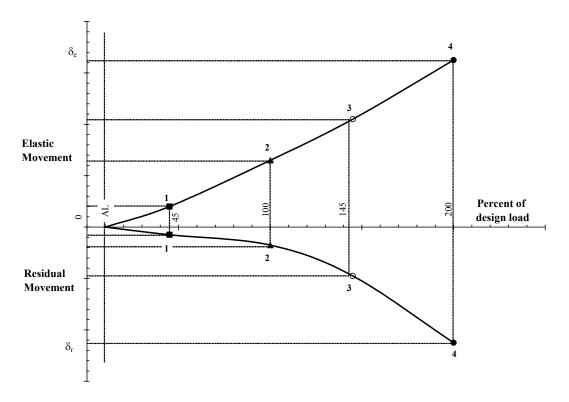


Figure 7-10. Plotting Elastic and Residual Movement of Verification Test Data.

#### 7.4.2 Proof Tests

# 7.4.2.1 General

Proof tests are conducted during construction on a percentage of the total production micropiles installed. Proof tests are intended to verify that the contractor's construction procedure has remained constant and that the micropiles have not been drilled and grouted in a soil zone not tested by the verification testing. Micropiles are proof tested to a load typically equal to 160 percent of the design load. During proof testing, loads can be applied in compression, tension, or laterally.

# 7.4.2.2 Proof Test Procedures and Recording and Analysis of Proof Test Data

The loading schedule for the proof test that is codified in DFI (2004) is outlined in Table 7-2. The results of an example proof test are plotted in Figure 7-11. The residual movements and elastic movements should be calculated for the test load from the unload cycle. This calculation is the same as that previously described for verification tests.

During the creep test portion of the proof test, the movement measured at specified times (i.e., 1, 2, 3, 4, 5, 6, and 10 minutes) is recorded. The time at which 1.3 DL is applied represents the start time for the creep test. As mentioned earlier, the creep movement at any time is the difference between the total movement and the movement measured at one minute. The creep rate is defined as the slope of the curve per log cycle of time. The movement from one to ten minutes after this starting time is recorded and compared to the acceptance criteria with respect to creep.

# 7.4.3 Micropile Acceptance Criteria

## 7.4.3.1 Acceptance of Verification Test

There are three primary acceptance criteria that must be met for a verification-tested micropile, as described below.

## Rate of Pile Head Movement at the Test Load

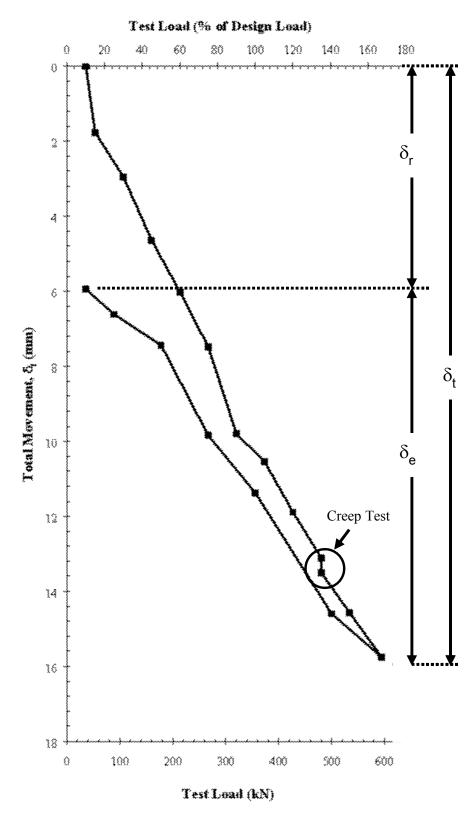
The acceptance criteria for verification tested micropiles include assessing whether failure has occurred at the test load (e.g., at 2.0 times the design load). Typically, at this load level, a plunging type failure will not be achieved, thus failure may be defined in terms of the rate of micropile head movement expressed as movement per unit of load. Herein, acceptance of a verification load-tested micropile requires that the slope of the load versus micropile head

settlement curve be less than or equal to 0.15 mm/kN (0.025 in/kip) at 2.0 times the design load (DFI, 2004). Restated, the failure load is defined as the load where the slope of the load versus micropile head settlement curve first exceeds 0.15 mm/kN (0.025 in/kip). It is specifically noted that driven piles and drilled shafts use the Davisson criteria to define maximum (or failure) load during a load test. This criterion is difficult to use for a micropile because of the change in axial stiffness over the length of the micropile (i.e., different stiffness for cased and uncased lengths). At this time, the use of the Davisson criterion for micropiles has not been evaluated.

Table 7-2. Proof Test Load Schedule (after DFI, 2004).

Step	Loading	Applied	Hold	Record and	Record and	Calculate Elastic
Бюр	Louding	Load	Time	Plot Total	Plot Residual	Movement
			(min)	Movement	Movement	3.20 ( 3.22022
			,	$(\delta_{ti})$	$(\delta_{ri})$	$(\delta_{\rm ei})$
1	Apply AL		2.5	( 11)	(/	( 0.7
2	Load Cycle	0.15DL	2.5	δ		
		0.30DL	2.5	δ	_	
		0.45DL	2.5	δ		
		0.60DL	2.5	δ		
		0.75DL	2.5	δ		
		0.90DL	2.5	δ		
		1.00DL	2.5	δ		
		1.15DL	2.5	δ	_	
		1.30DL	$\delta_t$ , zero rea	ading for		
			creep test	_		
3		least 10 minutes while recording movement at specified times. If the total				
		ared during the load hold exceeds the specified maximum value then the load stended to a total of 60 minutes.				
4		1.45DL	2.5	δ		
		1.60DL	2.5	δ		
5	Unload Cycle	1.30DL	4	δ		
		1.00DL	4	δ	_	
		0.75DL	4	δ		
		0.50DL	4	δ		
		0.25DL	4	δ		
		AL	4		$\delta_{\rm r}$	$\delta_{t}$ - $\delta_{r}$ = $\delta_{e}$
6	Remove the load and compare results to acceptance criteria					

Notes: AL = Alignment Load, DL = Design Load,  $\delta$  = total movement at a load. Total movement is typically recorded from several dial gauges and the average movement is recorded.



Note: 1 mm = 0.04 in and 1 kN = 0.225 kips

Figure 7-11. Plotting of Proof Test Data.

# Total Pile Head Movement at the Design Load

For this criterion, a maximum micropile head movement is prescribed for a single micropile corresponding to the design load. This criterion is used for micropiles tested in compression, tension, or laterally. The value selected by the design engineer is based on considerations of movements of the superstructure being supported by the micropile foundation and should be developed based on project-specific requirements.

# Total Pile Head Movement under Sustained Load (Creep)

The measured total movement for the required load hold at the 1.3 DL should not exceed 1 mm (0.04 in.) between 1 and 10 minutes. If the movements are less than the 1 mm for this period, the micropile is considered acceptable with respect to creep. For verification load tests in which the measured total movement exceeds the criteria described above, the load is held for an additional 50-minute period of time. If the measured total movement over this additional time period does not exceed 2 mm (0.08 in.) between 6 and 60 minutes, then the micropile is considered acceptable with respect to creep.

## 7.4.3.2 Acceptance of Proof Test

The previously described acceptance criteria for verification tests for total pile head movement at the design load and for total pile head movement under sustained load is used for a proof tested micropile. For a proof tested micropile, the creep test is performed at the maximum test load which is typically 1.3 DL. The evaluation of acceptable creep movements is the same as for verification-tested micropiles. It is noted that the creep criteria very rarely governs the acceptance of load tested micropiles.

## 7.4.3.3 Consequences of Failure

In the event a micropile fails to meet the specified acceptance criteria during verification load testing of pre-production micropiles, the contractor can modify the design of the micropile and/or the construction procedure in order to provide the required capacity. These modifications may include installing replacement micropiles, modifying the installation procedures, increasing the micropile bond length, regrouting via pre-placed re-grout tubes, or changing the micropile type. Any modification that requires changes to the structure shall have prior review and acceptance by the Owner. The cost of the changes should be incurred by the contractor.

If failure occurs during proof load testing of production piles, the contractor shall be directed to proof test another nearby micropile. For failed micropiles and further construction of

other micropiles, the contractor shall modify the design, the construction procedure, or both. These modifications may include installing replacement micropiles, incorporating micropiles of reduced load capacities, modifying installation methods, increasing the bond length, or changing the micropile type. Any modification that requires changes to the structure shall have prior review and acceptance by the Owner and should be at the contractor's expense.

#### 7.5 MICROPILE LOAD TEST REPORT

For each load test, a report must be written and submitted to the Owner, typically within 24 to 48 hours of the load test completion. The contents of this report should at least include the following:

- brief project description;
- description of site and subsurface conditions including information on the ground conditions at the location of the load test and a comparison to actual conditions encountered;
- key personnel including the drill rig operator, the superintendent, the grout plant operator, and any other personnel involved in the installation and testing of the micropile;
- micropile installation data including information such as length of the micropile (cased and uncased), number of bags of cement used to construct the micropile, size and type of casing and reinforcement, geology encountered (e.g. soil material, rock material, and water levels) during installation, and actual drilling and grouting records;
- results of load test including filled-out data sheets and data presentation figures;
- statement of load test requirements and acceptance criteria;
- comparison of load test requirements and acceptance criteria;
- summary statement on the load test results;
- hydraulic jack pressure gauge and load cell calibration report; and
- material certification, including grout compressive strength testing (e.g., 3 day test results may only be available) and steel mill certifications.

# 7.6 EVALUATION OF PROJECT LOAD TESTING REQUIREMENTS

## 7.6.1 Introduction

During the design phase of the project, consideration should be given to the scope of the micropile load testing program. The factors to be considered when determining the project testing requirements include the following:

- total number of production micropiles;
- magnitude and type of design loading (i.e., compression, tension, and/or lateral);
- sensitivity and importance of the supported structure;
- variance in ground subsurface conditions across the project site;
- types of subsurface conditions;
- site access and headroom/installation constraints; and
- contractor experience.

The project specification should include requirements for the following components of a load test program. These requirements are discussed in detail below, and include:

- number and location of pre-production verification load tests;
- number of production pile proof load tests;
- magnitude of the test loads;
- method of load application (single vs. multiple cycles, order of testing);
- duration for which the test loads are applied; and
- acceptance criteria for maximum total displacement and maximum creep displacement at a specified load.

# 7.6.2 Load Testing Program for Verification Tests

At least one pre-production verification micropile load test is required on all projects and the test is performed to at least 2.0 times the design load in accordance with Table 7-1. This micropile may be a sacrificial (non-production) pile or a production pile. Loading beyond the required minimum capacities may be conducted in an attempt to determine the ultimate capacity of the micropile.

The development of a verification load testing program should include the following steps and evaluations:

- A site map should be developed depicting all proposed structures for the project (e.g., pile cap) and locations of all geotechnical borings. In general, load testing should be performed in close proximity to a boring to allow for correlation of load test results to soil stratigraphy.
- The critical load combinations for each substructure unit should be reviewed to identify the types of load testing to be performed. In highly seismic regions, tension and/or lateral load testing may be required. In some cases, tension tests may be used as a substitute for compression testing, however, if compression loading is critical, at least one of the verification tests should be a compression test (where remaining tests may be substituted with tension tests).
- All subsurface information for the project site should be reviewed to identify strata
  where the micropile bond zone will be formed. This evaluation is performed for
  each structure location. This evaluation should include an assessment of the overall
  variability of the subsurface. Micropiles are often used in mixed ground conditions
  so it is essential to identify all soil/rock micropile support horizons which may be
  relatively weak or compressible compared to other strata.
- Based on the above evaluations, the total number of verification tests can be selected
  so that at least one verification load test is performed in each significantly different
  micropile support soil/rock stratum. The selection of testing locations must also
  consider access conditions and construction schedule. In cases where access to a
  proposed testing location is difficult, the engineer should consider if appropriate load
  testing information can be obtained at areas where greater access can be provided.

# 7.6.3 Load Testing Program for Proof Tests

Proof tests are performed primarily to confirm the contractor's construction procedures throughout the project. The Owner should provide the same information for proof testing as was previously discussed for verification testing. Although these tests will be performed during construction, the Owner should provide the Contractor with the number of micropiles to be proof tested as early as possible during construction. The specifications, however, should provide the Owner with the ability to request additional proof tests and to relocate them, if required, based on unacceptable results or varying ground conditions.

Proof testing may consist of compression and/or tension tests. Typically, tension tests are less expensive because the ground may be used for reaction to the test-load rather than adjacent piles or reaction tie-down anchors. Therefore, if the critical load condition is in tension, or if results of the production tension testing can be correlated to the pre-production tension and compression testing results then proof tests may consists of only tension tests.

A common requirement for proof testing is to test 5 percent of the production micropiles. This practice is similar to that used for driven piles associated with bridge foundations; however this "rule of thumb" percentage may not be appropriate for all applications. The following recommendations (Table 7-3) should be used in evaluating minimum proof testing requirements for a project.

Table 7-3. Recommendations on Minimum Number of Test Micropiles for Proof Testing.

Application	Proof Test Frequency		
Underpinning Applications	1 micropile proof test per substructure unit		
Seismic Retrofit	1 micropile proof test per substructure unit		
Structural Support of New	1 micropile proof test per substructure unit, but not less		
Construction	than 5 percent of total production micropiles		
Slope Stabilization	2 percent of total production micropiles to a test load of		
Stope Stabilization	2.0 times P _{ult} (P _{ult} is defined in Eq. 6-1 in Chapter 6)		

# 7.6.4 Test Load Magnitude

The test load magnitude is typically controlled by the geotechnical factor of safety desired. This geotechnical factor of safety is usually greater than factors of safety applied for ultimate structural capacity considerations. Therefore, excess structural capacity may be required for the micropile to support the test loads based on geotechnical capacities.

For magnitude of test loading (for structural support applications), this manual recommends:

Verification load testing to . . . . .  $2.0 \times \text{Design Load}$ 

Proof load testing to . . . . . . .  $1.6 \times \text{Design Load}$ .

The geotechnical capacity of a micropile can have an effect on the ultimate structural capacity, thus requiring that the same factor of safety be used for both geotechnical and structural considerations. Whether or not the reinforcement can be varied for the test piles should be considered carefully, and should be addressed in the project specifications. This issue has been reviewed in Chapter 5.

# 7.6.5 Method of Load Application

If the micropiles are designed for tension and compression loads, then both loading conditions should be tested. If the same micropile is to be tested in both tension and compression, it is suggested that the tension test be conducted first. This will allow the pile to be reseated during compression testing in the event some net upward residual movement occurs during the tension test. Because proof tests will be performed on random micropiles, the Contractor shall assure that all micropiles can be used for load testing.

It is usually not necessary to conduct the load test on an inclined micropile, even if the project includes them. Installing the micropile on an incline has little, if any, effect on difficulty of construction and resulting capacity, particularly for micropiles installed by the cased hole method. However, testing an inclined micropile can be difficult and increase the testing costs, particularly for compression testing.

For micropile load tests for slope stabilization, tension tests may be used.

## 7.7 OTHER LOAD TESTING TECHNIQUES

#### 7.7.1 General

In current practice, micropile proof testing is performed using the same load testing equipment and procedures as for verification testing. While proof testing is less expensive than verification testing because of reduced maximum test load magnitudes and reduced time to complete the test, the test set-up (which comprises a significant portion of the load test cost) is the same. For driven piles, for example, "proof" tests typically include the use of dynamic testing using a pile driver analyzer (PDA). PDA results can be correlated to project-specific load testing results and, therefore, is used as a quality control measure on driven pile projects. PDA testing is rapid and inexpensive compared to full-scale load static load testing and therefore provides a means to evaluate (approximately) the static capacity of a relatively

large number of production piles at a relatively low cost. Similarly, Statnamic testing may also be used as a quality control and assurance measure when used in concert with full scale static load tests.

In this section, information on the use of PDA and Statnamic testing for micropiles is presented. At this time, neither of these methods are used on a regular basis for micropiles, however, they may be used increasingly as more experience is gained with these methods for micropile applications.

## 7.7.2 Dynamic Load Testing

Although not commonplace in current practice, the use of PDA for micropile proof testing could provide the same advantages as for driven piles. Since micropiles are not driven, a pile hammer needs to be mobilized to the site to perform the testing. Details on the use of the PDA and data interpretation using CAPWAP analysis methods are provided in FHWA-HI-97-014 (1996). Currently, there is not sufficient field experience using PDA on micropiles to develop general procedures and recommendations for their use on micropile projects, however, one case history is reviewed herein.

On a recent project in Northern Virginia, Gomez et al. (2004) used PDA to evaluate the static capacity of micropiles installed through karstic limestone to competent rock (Figure 7-12). Static load testing on two of three test micropiles indicated that test loads (equal to two times the design load) could not be achieved. It was concluded that the causes for the failure of the two micropiles were contamination of the contact between the grout and the rock in the bond zone and the difficulties encountered in cleaning the bond zone by flushing with water. Because of these observations, the capacity of the production micropiles that had already been installed needed to be evaluated. PDA testing was performed on 22 production micropiles of varying lengths. Because of the relatively small cross sectional area of the micropiles, there was concerns over potential structural damage that could result from the hammer striking required for the dynamic testing. In PDA testing, sufficient energy must be imparted to the pile to cause sufficient movement to enable estimates of capacity to be made. For this project, a procedure to gradually increase hammer energy was used and a cushioning system was fabricated in the field to prevent structural damage to the micropile. Capacities based on PDA results were consistent with those measured from the three static load tests. The authors concluded that dynamic testing (using PDA) could provide reasonably accurate estimates of capacity for the rest of the production micropiles tested.



Figure 7-12. Dynamic Test Set-Up for Micropile (after Gomez et al., 2004).

As stated, specific cost advantages may be realized in using PDA as compared to static compression load testing for micropile proof tests. The volume of PDA tests in one day makes the PDA more cost effective. However, there are specific disadvantages associated with PDA testing of micropiles that need to be considered:

- The creep test, which is a part of proof testing program and which is currently used as a means to confirm acceptability of a micropile, cannot be performed with dynamic test equipment.
- Tension and lateral loading tests cannot be performed with dynamic test equipment.
- Perhaps even more for micropiles than other pile systems, the potential for structural damage to the micropile needs to be considered especially as a result of potential eccentric loading by the pile hammer.
- Data interpretation must be performed by an engineer with detailed knowledge of the testing method and its limitations (as should be required with any load testing).
- Where tension tests are sufficient to evaluate micropile bond zone capacities, it is unlikely that PDA testing will be more cost-effective than conventional tension tests

(unless test load magnitudes are very high thus requiring substantial reaction beams for a static load test).

# 7.7.3 Statnamic Load Testing

The Statnamic test method was developed by Bermingham and Jane (1989) and is used to evaluate capacity of foundations including drilled shafts, driven piles, augered cast-in-place piles, micropiles, stone columns, and shallow foundations. The use of this method to evaluate micropile capacity is increasing and several projects have been completed (although test data has not been published to date). Equipment, testing methods, and information on data interpretation are provided in Mullins et. al. (2001) for Statnamic load testing.

The Statnamic test method uses solid fuel burned within a pressure chamber to rapidly accelerate upward the reaction mass positioned on the pile head. As the gas chamber increases, an upward force is exerted on the reaction mass, while an equal and opposite force pushes downward on the pile. Loading increases to a maximum and then unloads by a venting of the gas pressure. The magnitude and duration of the applied load and the loading rate are controlled by the selection of piston and cylinder size, the fuel mass, fuel type, the reaction mass, and the gas venting technique.

The work area for the test set-up must be typically between 3 to 4 m (10 to 13 ft) in diameter and must be leveled (Figure 7-13). The set-up also requires at least 8.5 m (28 ft) of headroom clearance

The advantages of Statnamic testing for micropile load testing include:

- Statnamic testing does not require any reaction piles or reaction system. It takes less time to prepare the test set-up as compared to static load testing.
- Depending on the magnitude of load, site location, and labor costs, the cost of statnamic test could be on the order of one quarter to one half the cost of an equivalent capacity static load test.
- Statnamic test is readily adaptable to lateral load testing, batter micropiles and axial load testing on land or over water.
- Because the load duration is long enough to preclude stress wave formation, the analysis is simpler than for dynamic testing techniques.



Figure 7-13. Statnamic Test Set-Up (courtesy of Applied Foundation Testing (AFT), Inc.).

The disadvantages of Statnamic testing for micropiles include:

- The creep test, which is a part of proof testing program and which is currently used as a means to confirm acceptability of a micropile, cannot be performed with Statnamic test equipment.
- Tension tests have not been performed with the Statnamic device yet.
- For tight access conditions, unless the engineer allows the location of the test pile to be relocated to an area with better access, Statnamic testing may not be suitable.
- Data interpretation must be performed by an engineer with detailed knowledge of the testing method and current analysis methods (as should be required with any load test method).

## 7.8 REFERENCES

- ASTM D1143, "Standard Test Method for Piles Under Static Axial Compressive Load", American Society for Testing and Materials, pp. 104-114, New York.
- ASTM D3689, "Standard Test Method for Individual Piles Under Static Axial Tensile Load", American Society for Testing and Materials, pp. 416-426, New York.
- ASTM D3966, "Standard Test Method for Piles Under Lateral Loads", American Society for Testing and Materials, pp. 440-454, New York.
- Bermingham, P. and James, M. (1989), "An Innovative Approach to Load Testing of High Capacity Piles", *Proceedings of the International Conference on Piling and Deep Foundations*, V. 1, J. B. Burland and J. M. Mitchell, pp. 409-413.
- DFI (2004), "Guide to Drafting a Specification for Micropiles", *Deep Foundations Institute*, The International Association of Foundation Drilling, 60 pages, New Jersey..
- Gomez, J, Cadden, A., and Christopher, W. (2004), "Micropile Foundations on Karst: Static and Dynamic Testing Variability", *Proceedings of Fifth International Conference on Case Histories in Geotechnical Engineering*, April 13-17, New York.
- Mullins, G., Lewis, C. L., and Justason, M. D. (2001), "Advancements in Statnamic Data Regression Techniques", *Deep Foundations 2002: An International Perspective on Theory, Design, Construction, and Performance*, ASCE Geo Institute, GSP No.116, V. II, pp. 915-930.

# CHAPTER 8 MICROPILE CONSTRUCTION MONITORING AND INSPECTION

#### 8.1 INTRODUCTION

The purpose of this chapter is to provide guidance regarding construction monitoring and inspection (i.e., construction quality assurance (QA) and construction quality control (QC) inspection) for micropiles. Inspection is the primary mechanism to assure that micropiles are constructed in accordance with the project plans and specifications. Short-term and long-term monitoring may be conducted to assess the performance of the micropiles. Construction monitoring activities can be carried out by the owner agency, the contractor, or a combination of both, depending on the contracting approach (i.e., method, performance, or design-build (see Chapter 9)), while performance monitoring is usually conducted by the owner agency. Inspection and monitoring of micropile systems which are constructed using performance specifications are described in this chapter.

Quality assurance activities, if properly conducted, play a vital role in the production of high-quality micropiles because conformance to project plans and specifications should result in micropiles that will perform adequately for the intended service life. These activities may involve evaluation of the following: (1) conformance of system components to material specifications; (2) conformance of construction methods to execution specifications; and (3) conformance to short-term performance specifications.

Short-term (during construction) micropile monitoring is usually limited to monitoring measurements during load testing (i.e., verification, proof, and creep tests). In some cases, short-term monitoring may include, for example, monitoring, ground surface settlements or movements of nearby foundations (particularly where micropiles are used for underpinning applications). Long-term monitoring may be performed for micropiles used for slope stabilization as experience with this application of micropiles is limited to date, and this monitoring may include a continuation of measurements from short-term monitoring.

# 8.2 INSPECTION ROLES UNDER CERTAIN CONTRACT APPROACHES

For micropiles contracted using the method approach, QA activities are carried out by the owner agency based on comprehensive material and procedural requirements of owner-provided plans and specifications. The contractor responsibility is to follow the project plans

and specifications and provide quality assurance. The owner's inspection is conducted to assure strict compliance with each component of the specification.

For the performance contracting approach, the contractor carries out QC activities. The owner agency will carry out a limited number of QA activities as required by project specifications, primarily to verify that requirements are met for materials, equipment, construction tolerances, and sequencing. The contractor selects the equipment and construction procedures used and is responsible for satisfying specified performance criteria.

For the design-build approach, the performance of all required inspection activities are carried out by the contractor or are the responsibility of the contractor in accordance with the QA plan approved by the owner. Random quality assurance tests are done by the owner agency or through an independent third party inspection firm.

## 8.3 PRE-PROJECT PREPARATION

Prior to construction, the QA inspector must have an understanding of the project and specification requirements, particularly as related to inspection responsibilities, site and subsurface conditions, and material and construction requirements. Inspection responsibilities should be defined at a preconstruction meeting with the general contractor and all subcontractors (e.g., micropile installation contractor) involved in the project. The inspector must understand the intended function of the micropiles and other individual system components. Sources of information should include geotechnical reports, contract plans, and specifications. The inspector should contact the project engineer at the start of the project to discuss critical design aspects and potentially difficult site and subsurface conditions.

Prior to the commencement of any construction, the micropile contractor's work plan should be submitted to the engineer for review and approval. Work shall not proceed until the work plan has been approved. The contractor's work plan should describe, at a minimum, the following elements of the work:

- 1. Contractor and employee qualifications
- 2. Contractor's understanding of ground conditions with a discussion on anticipated difficulties related to these ground conditions
- 3. Performance criteria and tolerances
- 4. Location and orientation of each micropile
- 5. Size and configuration (i.e., description of micropile cross section) of each micropile

- 6. Capacity requirements for each micropile
- 7. Drilling equipment, including manufacturer and model numbers, flushing media, and a discussion of the precautions to be implemented to minimize drilling deviations
- 8. List of all equipment to be used for the project with equipment loads on structure or adjacent ground during construction
- 9. General installation plan, including proposed sequence of installation, phasing, and scheduling
- 10. Grout design mix, along with batching, mixing, and injection techniques
- 11. Reinforcement, including sizing, configuration, and corrosion protection
- 12. Postgrouting methods (if anticipated to be used), procedure, and equipment
- 13. Documentation of and protection methods for existing utilities and other sensitive elements that may be affected by the micropile work and proposed measures to minimize impacts of the micropile work on these elements
- 14. Plan to accommodate low headroom or nearby obstructions
- 15. Load testing information including identification of micropiles to be tested, type of testing to be performed (e.g., compression, tension, lateral), maximum anticipated test load for each micropile to be tested, allowable deformations under test loads, and details of the testing procedures for each type of test to be performed (i.e., compression, tension, or lateral) including sketches showing typical layout for load tests (e.g., location of reaction piles, position of dial gauges, etc.)
- 16. Calibration information for load cells, pressure gauges, dial gauges, and any other testing or monitoring devices
- 17. Details of connection to existing structures
- 18. Remedial action plan describing measures to be implemented in the event of excessive movement of existing structures, release of spills to environmentally sensitive areas, and other potential hazards that could reasonably be anticipated at the start of the project
- 19. Spoil handling procedures.

Most importantly, protection of the existing environment, including underground utilities, must be considered. The existing site conditions should be examined by the micropile contractor with the inspector. The contractor is responsible for furnishing equipment suitable for the specific site conditions.

Figure 8-1 provides a summary of QA inspector responsibilities for a typical micropile project.

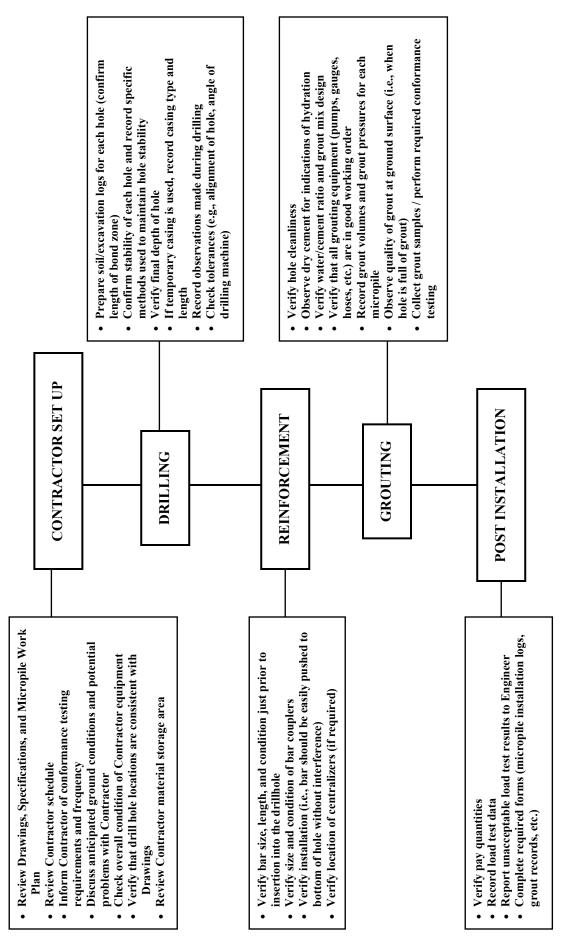


Figure 8-1. QA Inspector Responsibilities for a Typical Micropile Project.

Micropile Design & Construction

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## 8.4 INSPECTION OF MICROPILE MATERIALS

## 8.4.1 General

Specifications describe minimum requirements for micropile materials. These minimum requirements may be defined explicitly or by reference to standard specifications such as those set forth by AASHTO and ASTM. Because the materials used to construct a micropile are common civil engineering materials, prequalified products are not commonly required, however, certain proprietary features may be involved in, for example, the micropile to footing connection. Recommendations for the storage and handling of selected materials are commonly included in specifications.

Conformance to a specification requirement is commonly assessed in one of the following ways: (1) reviewing manufacturer or supplier certification submitted by the contractor; (2) reviewing of product literature and visual inspection; or (3) conformance testing. All materials and prefabricated elements delivered to the site must be visually examined prior to installation to verify required geometry and dimensions and to identify any defects in workmanship, contamination, or damage by handling. All nonconforming materials are unacceptable, unless appropriate corrections are made in accordance with specifications or by written approval of the project engineer.

# 8.4.2 Storing and Handling of Cement

Cement is typically supplied either in bagged (43 kg/sack) or bulk (1320 kg/bulk bag) form, depending on site conditions, job size, local availability, and cost. Cement should not be stored directly on the ground or anywhere where it may be subject to significant moisture absorption. An example of appropriate cement storage is provided in Figure 8-2. The contractor should avoid stacking the bags too high to prevent over compaction of the cement.

Cement should be visually examined for lumps or other indications of hydration or contamination by foreign matter immediately prior to its use. The water used for grout mixing must be potable, and not contain impurities harmful to the steel or the grout. The contractor should also handle admixtures with care following manufacturer's recommendations. Approved admixtures that have exceeded the manufacturer's recommended shelf life should not be used.



Figure 8-2. Cement Storage.

# 8.4.3 Storing and Handling of Reinforcing Steel

Steel reinforcement should be stored above the ground surface and be protected against mechanical damage and exposure to weather. Reinforcing bars should be lifted using fiber ropes or webbing and should be supported at several locations to prevent excessive bending.

The micropile contractor should use care in unloading and storing all reinforcing steel material. The storage area should be away from construction traffic and in a protected location. When reinforcing steel material is delivered to the job site, it should be visually checked for size and any signs of corrosion. Reinforcing steel elements should be accompanied by mill certificates. Mill secondary pipe materials, for which mill certificates will not be available, require verification of steel quality through tensile and chemical testing of steel samples. For *Buy America Contracts*, United States manufacturing of materials must be verified. All steel reinforcing materials shall conform to the proper standards as identified in the project specifications.

Properly stored steel reinforcing materials (see Figure 8-3) prevent corrosion or contamination by dirt, oils, and/or organics. Wood spacers placed between the ground and

the steel materials will prevent slight rusting that can occur if steel is exposed to the ground. A light coating of surface rust on the steel is normal and indicates that oil and grease are not present. Deep flaky corrosion or deep pitting of the steel is cause for rejection. All steel materials should be inspected just prior to their use.

Double corrosion-protected and/or epoxy-coated steel bars should be delivered to the job site pre-manufactured (Figure 8-4). Extra care in handling and storage shall be given to these materials. Epoxy-coated bars shall be properly wrapped with padded bands and placed on wooden or padded supports. Pre-manufactured corrosion-protected steel bars must be stacked with care to prevent any damage to the corrugated tube and/or epoxy coating. Any repairs to epoxy coatings shall be performed in accordance with manufacturer's recommendations.

Mechanical couplers, hex nuts, centralizers, and spacers are typically delivered to the job site in boxes. Mill certificates will be provided for the steel couplers and hex nuts. Storage of these materials shall follow the same procedures as other materials.



Figure 8-3. Storage of Reinforcing Steel.



Figure 8-4. Double Corrosion Protected (Encapsulated) Reinforcing Steel.

## 8.5 INSPECTION OF CONSTRUCTION ACTIVITIES

# **8.5.1** Inspection of Drilling Activities

The contractor's drilling operation should not cause unacceptable loss of ground. Signs of unacceptable loss of ground include the inability to withdraw the drill casing from the hole, large quantity of soil removal with little or no casing advancement, and subsidence of the ground above drilling location. The QA inspector should document this information and other observations of the drilling procedures in their daily reports.

When temporary casing is to be removed during the grouting process, it should be removed in a manner that does not cause the pile reinforcement to become disturbed, damaged, or allowed to loss contact with the in-situ soil. The casing should also be kept full of grout during the removal operation to minimize the potential for drillhole collapse. The contractor is responsible for implementing all measures required to maintain an open drillhole during construction. Fluid levels in the drillhole must always be kept above the ground water level to minimize potential ground losses into the drillhole from potentially unstable soils.

The drilling, installation of reinforcement, and grouting of each micropile should be completed by the contractor in a series of continuous processes as expeditiously as possible. Some materials, such as consolidated clays and weak rock, can deteriorate and soften when exposed to air or water. Under these conditions, drilling of the pile bond zone, reinforcement installation, and grouting of the bond zone should be completed in one day. Unless micropile construction is continuous, the contractor should temporarily plug or cover the drillhole at the ground surface to prevent debris from falling into the borehole and for safety of the personnel working on the site. It is also recommended that casing material be placed (temporary or permanent project) a minimum of 0.3 m (1 ft) above the ground surface elevation to avoid drill spoils and flushing water from other operations flowing down and contaminating the completed hole.

The micropile contractor shall provide for proper disposal and containment of the drilling spoils from the site in accordance with the approved work plan. The drill water should be controlled at all times to prevent erosion and to prevent accumulation of standing water which may freeze or otherwise create sloppy working conditions.

Micropile inclination and position may need to deviate from that specified in the contract documents. Any deviation outside the tolerances provided in the Specifications, however, should be viewed as a design change and the contractor must notify the engineer of his intended change before implementing this change. In general, any deviations from the Drawings and Specifications should be recorded by the QA inspector and this information provided to the engineer.

## 8.5.2 Inspection of Reinforcement Installation Activities

Reinforcement may be placed either prior to drillhole grouting, or placed into the grout-filled borehole before temporary casing (if used) is withdrawn. In any case, the inspector shall record the total pile length and bond zone length for each installed micropile. The reinforcement shall be capable of being inserted to its prescribed length in the hole without force. Inability to achieve this penetration in uncased holes usually means caving of soil into the hole has occurred, and withdrawal of the reinforcement and redrilling is necessary. Driving the reinforcement to full length or cutting off the reinforcement shall not be allowed.

Care should be exercised so as not to damage corrosion protection measures or centralizers during reinforcement installation. Neither epoxy-coated, double corrosion-protected, or uncoated steel reinforcements should be dragged across abrasive surfaces or through the surface soil. All splices and couplings should be checked for proper seating. The reinforcement must be clean of deleterious substances such as surface soil, oil, and mud,

which may contaminate the grout or coat the reinforcement. Centralizers and spacers shall be checked to ensure placement at specified intervals, typically 2.5 to 3 m (8 to 10 ft) (Figure 8-5). Attachment of the centralizers to the reinforcement should also be checked to ensure that the reinforcement remains centered in the borehole. Typically centralizers are attached with tie-wire or duct tape. If tremie grout tubes are placed after the reinforcement has been positioned, care should be exercised so that the tremie tube does not interfere with the centralizers.

# **8.5.3** Inspection of Grouting Activities

Before any grouting begins, the condition of the grouting equipment should be checked by the contractor and the grout-mix design should be verified. Care in execution of the grouting process can greatly impact the quality of the completed micropile and its load carrying capacity.

Prior to grouting, the inspector should verify the diameters of micropiles drilled without casings. Ideally, the contractor should grout the micropiles immediately after drilling the bond zone. However, if this is not possible, grouting should be performed before degradation of the drill hole.



Figure 8-5. Reinforcement Centralizers.

The primary grouting operation involves injecting cement grout at the lowest point of the borehole so the hole will fill evenly without air voids. A tremie tube is typically tied to the reinforcing steel before insertion in the borehole. After placement of the reinforcement steel and tremie tube, the grout is pumped to the bottom of the pile until grout of suitable quality (of the same consistency as that being injected) returns to the top of the pile. The tremie tube is then removed from the micropile hole or left in the hole and filled with grout.

The Contractor should perform grouting in one continuous operation. Care should be taken to maintain a positive head at the grout holding tank to avoid drawing air into the injected grout. Pressure grouting may be applied to the primary grout during casing withdrawal. Care must be taken with such pressures to avoid distress to the ground or adjacent structures. The pressure grouting process should be discontinued if grout is observed escaping at the ground surface.

Grout pressures are measured as close to the point of injection as possible to account for line losses between the pump and the borehole. Typically, a pressure gauge is mounted on the drill rig and monitored by the drill rig operator as a guide during pressure grouting and casing withdrawal (Figure 8-6).



Figure 8-6. Drill Rig Pressure Gauge.

For micropiles installed with a hollow-stem auger, the grout should be pumped under continuous pressure with a grout head maintained above the tip of the auger during auger withdrawl. The auger should be withdrawn in a controlled manner to minimize the potential for "necking" of the borehole to occur.

If post grouting is performed, it is very important to monitor grout pressures and volumes throughout the injection of each sleeve. This will help prevent dangerous or needless over injection and progressively verify the effectiveness of the treatment. Post grouting pressures have been documented in excess of 6.5 MPa (943 psi). Typical range during injection is 2 to 4 MPa (290 to 580 psi).

Grouting records are of vital importance on every project and are described in Section 8.6.3.

## 8.6 REQUIRED PROJECT DOCUMENTATION

## 8.6.1 Micropile Load Testing

During micropile load testing, the inspector must verify that the: (1) test pile installation method used is the same as will be used for the installation of the production piles; (2) pile load test setup is in accordance with the approved working drawings; and (3) pile is load tested in accordance with the project specifications. During load testing, the following general guidelines should be observed:

- at no time should the micropile be loaded such that the axial stresses within the micropile exceed maximum allowable stresses provided in the Specifications;
- at no time should the applied load be reduced below the alignment load; and
- test measurements should be plotted as the test proceeds in order to identify unusual behavior.

The QA inspector should check the following:

- testing apparatus alignment;
- use of properly calibrated jacks and gauges;
- dial gauge arm alignment and travel length;
- dial gauge point of contact;
- application of the proper loads and sequencing and duration of each load; and
- potential interference points due to pile deflection.

# **8.6.2** Production Micropiles

Comprehensive records of the micropile installation are required to establish the basis of payment and to identify potentially significant deviations from the Contract Documents. Table 8-1 shows an example micropile installation log to be used by the micropile contractor and the inspector. A completed micropile installation log is provided in Table 8-2 as an example.

# **8.6.3** Grouting Records for Production Micropiles

Because the grout is such a vital component of the micropile, close attention should be paid to the quality and control of the grout. Grout production and consumption records must be kept daily. It is important that the actual pressure and volume of grout pumped for each micropile be recorded by the contractor and the inspector.

Unconfined compressive strength of grout is determined according to AASHTO T106/ASTM C-109. Compressive strength is typically checked through a set of three each, 50-mm (2 in) grout cubes (Figure 8-7). Tests are typically performed at 3, 7, and 28 days after grouting. Seven-day tests are considered the most crucial, as the grout will typically attain the required design strength within this time period. Anticipated strength will depend upon project need, but compressive cube strengths can be very high, as much as 24 MPa (3,500 psi) after only 24 hours of set time. The unconfined compressive strength is largely dependent on project needs, but a 28-day strength requirement between 25 and 40 MPa (3,600 and 5,800 ksi) is considered common for micropiles. The inspector needs to verify that the grout cube break strengths comply with the project specifications. Grout samples should be taken directly from the grout plant. It is recommended that one set of three grout cubes be taken for every 10 micropiles installed, or every day for each grout plant in operation, whichever occurs more frequently.

Table 8-1. Example Micropile Installation Log.

Project Name:			Pile Designation #					
Contract No.:			Design Load Compress = Tensi		Tension =			
		Ι	DESIGN	AS-BUILT	Installation Date			
Pile Inclin	ation				Time @			
Casing Di	a./Wall Thickness				Star	t of Drilling		
Reinforce	ment Size/Length				Start	of Grouting		
Casing Le	ngth below B.O.F.				Pile	Completion		
Cased Boa	nd Length (Plunge)				Tot	tal Duration		
Bond Len	gth Below Casing				ABBREVIATIONS			
Total Pile	Length below B.O.F.				B.O.F. = Bottom of F	ooting		
Casing Le	ngth above B.O.F.							
				PILE DR	ILLING			
	Drill Method					D	rill Rig#	
Drill	Bit Type and Size					Dri	ll Operator	
Time	Depth from B.O.F	Soil	l / Rock D	escription	Flush Return Description	Comments		
. <u> </u>					<b>F</b>			
					+			
			1	PILE GRO	DUTING	ı		
(	Grout Plant #, Operator	r			Cement Type			
Trei	nie Grout Quantity (ba	ags)			Admixtures			
Press	sure Grout Quantity (b	ags)			w/c Ratio			
Gro	outing after plunge (ba	gs)			Grout Ratio (bags/m bond)			
Tot	tal Grout Quantity (bag	gs)						
Depth from B.O.F Pressure Range Max/Average			C	omments				

Table 8-2. Example Completed Micropile Installation Log.

Project Name: Keeley Palace				Pile Designation #: Pile 1			
Contract No.: 0064			Design Load Compress =		Tension =		
		DESIGN	AS-BUILT	Installat	ion Date	12-25-96	
Pile Inclin	ation	0 degrees		Т	ime @	8:00 am – 9:20 am	
Casing Di	a./Wall Thickness	177/13 (mm)		Star	t of Drilling	8:00 am	
Reinforce	ment Size/Length	57( mm)/15.5 (m)		Start	of Grouting	9:00 am	
Casing Le	ength below B.O.F.	8 m		Pile	Completion	9:20 am	
Cased Bond Length (Plunge)		2 m		Total Duration		1:20	
Bond Length Below Casing		6 m		ABBREVIATIONS			
Total Pile Length below B.O.F.		16.5 m		B.O.F. = Bottom of Footing			
Casing Le	ength above B.O.F.	0.5 m					
			PILE DRI	LLING			
	Drill Method	Cased Rotary			Dı	rill Rig#	10-1
Drill	Bit Type and Size	Casing Teeth – 175 mm			Drill Operator Kil		Kilian
Time	Depth from B.O.F	Soil / Rock Description Flush Return Description Comm		Comments			
	0 – 5 m	Gravel and C	obbles	Brown, full return			
	5 – 10 m	Sand Gravel w	/Cobbles	Brown, full return			

#### PILE GROUTING

Gray, full return

Occasional Sand Seams

Cobbles w/Gravel

Grout Plant #. Operator	8-1, Holder	Cement Type	I/II
Tremie Grout Quantity (bags)	12	Admixtures	None
Pressure Grout Quantity (bags)	13	w/c Ratio	0.45
Grouting after plunge (bags)	2	Grout Ratio (bags/m bond)	
Total Grout Quantity (bags)	27		

Depth from B.O.F	Pressure Range Max/Average (MPa)	Comments
15 – 10 m	0.55 / 0.45	Grouted first 3 m under pressure, pulled remainder under static head
10 – 5 m	0.55 / 0.47	Grouted first 3 m under pressure, pulled remainder under static head
Plunge, 5 – 6.5 m	1.2	After plunging casing, pumped additional 2 bags at max pressure = 1.2 MPa

10 – 15 m



Figure 8-7. Grout Cubes for Compressive Strength Testing.

Specific gravity measurements of grout are frequently checked to determine the water content of the grout because the water content of the grout is the prime control over grout properties. Neat cement grout density can be determined per the American Petroleum Institute (API) Recommended Practice (RP) 13B-1 by the Baroid Mud Balance Test (Figure 8-8). The test is extremely quick and inexpensive and should be performed at least once per micropile. By monitoring the water/cement ratio during grouting, the inspector can ensure that the grout is being prepared according to the specified project mix design. A common specific gravity for grout is between 1.8 and 1.9, which corresponds to a water/cement ratio of 0.45.

Tests that permit quality assessment prior to installation are more valuable since they permit immediate reaction in case of anomalies. Compressive strength values; however may only be established 48 hours after the sampling at the earliest. Pre-construction testing of the grout should be performed prior to production drilling to verify acceptability of grout mix design such as prior to and/or during micropile verification load testing.



Figure 8-8. Baroid Mud Balance Test.

#### 8.7 REFERENCES

- ASTM C109, "Standard Test Method for Compressive Strength of Hydraulic Cement Mortars Using 2 in (50 mm) Cube Specimens", American Society for Testing and Materials, New York.
- AASHTO T106, "Standard Test Method for Compressive Strength of Hydraulic Cement Mortars Using 2 in (50 mm) Cube Specimens", American Association of State Highway Transportation Officials, Washington, DC.

## CHAPTER 9 CONTRACTING METHODS

#### 9.1 INTRODUCTION

The purpose of this chapter is to describe contracting approaches that are commonly used in developing contract documents for projects involving micropiles. Two types of contracting methods are used to develop contract drawings and specifications for micropiles. Some agencies prefer one approach to the other or a mix of approaches for micropiles based on the criticality and complexity of a particular project, experience of the owner and their engineering consultants, and the availability of specialty contractors. The selection of a contracting method may also depend on the experience of the agency with micropile technology. Both contracting approaches are valid if properly implemented and each has advantages and disadvantages. These contracting methods include:

Method (or Procedural) Approach. All details of design, construction materials, and methods are specified in the contract documents. A variant to this method allows the contractor to select micropile drilling and grouting methods required to achieve specified pile capacities.

*Performance or End-Result Approach.* Lines and grades with specific design criteria and methods and performance requirements are provided in the contract documents. With this approach, a project-specific review and detailed plan submittal occurs in conjunction with the submittal of working drawings.

Because specialty contractors often introduce innovative, cost-competitive solutions, it is recommended that the contract documents for micropile projects be structured to allow specialty contractors to make use of the latest available construction techniques. Thus, contract documents that are performance-based, with respect to drilling and grouting methods, are recommended. The performance approach and the variant of the method approach allow this flexibility.

#### 9.2 CONTRACTOR QUALIFICATION

The procedures for micropile construction need to be followed closely to provide a high quality product. Selecting an experienced and qualified contractor to install micropiles is

critical to obtain a satisfactory installation. The likelihood of success further increases when comprehensive construction quality assurance procedures are developed and enforced by the owner. Agencies or owners with no previous micropile experience should seek a qualified third-party quality assurance provider.

Contract documents for micropile projects should clearly define: (1) the contractor prequalification requirements; (2) submittal procedures for this qualification information; and (3) the means by which the owner will enforce these requirements. Such pre-qualification requirements are commonly being used by many transportation agencies for other specialty construction techniques, such as permanent ground anchors, soil nail walls, drilled shaft foundations, and shotcreting. However, where formal pre-qualification may not be allowed, agencies should request that bidders demonstrate that they meet specific micropile experience requirements.

The recommended minimum qualifications for each micropile contractor are provided below.

- The contractor firm and its proposed employees for the project should provide evidence of previous successful experience in the design and installation of micropiles. Owner references in the design and installation of micropiles of similar scope to those proposed for the application project should be provided. Documentation shall include at least five successful projects performed in the last five years.
- 2. The contractor firm shall assign an engineer to supervise the work who has at least three years of experience in micropile design and construction of at least 3 successfully completed projects over the past 5 years.
- 3. The contractor firm must have previous drilling experience in similar ground to anticipated project conditions. The contractor firm must submit at least three successful load test reports from different projects of similar scope to project.
- 4. Project superintendents and drill operators responsible for installation of micropile system must have micropile installation experience on at least 3 successfully completed projects over the past 5 years.

#### 9.3 METHOD CONTRACTING APPROACH

The method contracting approach includes the development of a detailed set of plans and specifications to be provided in the bidding documents. The advantage of this approach is that complete design details and specifications are developed and reviewed by experienced

representatives. This approach further empowers agency engineers to examine options that may be available during design but requires engineering staff trained in micropile design and construction methods. The staff then also becomes a valuable asset during construction, when questions and/or design modifications are required.

Under this contracting procedure, the agency is fully responsible for the design and performance of the micropile, as long as the contractor has installed each component (e.g., pile casing, grout, steel reinforcement) in strict accordance with the contract documents. The agency assumes all risks and is responsible for directing the work if changes to the design are required based on actual field conditions. The use of a method specification is recommended only for agencies that have developed sufficient in-house expertise and consider micropile design and construction control as a conventional or standard method for foundation system or slope stabilization.

The use of a variant to this method, in which the contractor is responsible for developing the required pile capacity by varying the drilling and grouting methods, drill hole diameter, and length of piles from specified minimums, has several advantages. It empowers contractors to maximize the use of their experience and specialized equipment and allows the agency to share the major risk, (i.e., pile capacity for a specified length), with the contractor. The owner typically establishes the following:

- scope of work;
- micropile design loadings and spacing;
- footing details;
- corrosion protection;
- micropile testing procedures and requirements;
- instrumentation requirements (if any);
- special design considerations (e.g., scour and liquefaction potential); and
- performance criteria.

The micropile contractor specifies the following:

- micropile construction process;
- micropile type;

- micropile design; and
- pile top to footing connection design.

This division of work allows the qualified specialty contractors to provide an economical micropile design, while satisfying the design requirements. This method also allows responsibility for the work to be shared between the owner and the micropile contractor. While this is slightly more restrictive than the contractor design/build specification method, it is still flexible enough to allow for some innovation and cost savings. Various types of owner-controlled design specifications are described subsequently.

#### 9.3.1 Standard Design

The contract documents for the Standard Design Type are prepared to allow for various qualified micropile designs. The owner's engineer provides the micropile design loadings, footing design, and pile layout for foundation support. In addition, the owner provides the following:

- geotechnical reports and data;
- micropile design parameters (foundation support projects only) including maximum pile sizes, axial pile loads, lateral pile loads, displacement requirements, and ductility requirements;
- existing utility plans;
- site limitations, including: (1) access limitations; (2) right of way; (3) scour potential; (4) liquefaction potential; (5) noise requirements; (6) vibration requirements; and (7) potential for hazardous and/or contaminated materials;
- contractor working drawing/design submittal and review requirements including time frame and information on penalties;
- material specifications;
- testing requirements;
- instrumentation requirements (if any);
- micropile acceptance criteria; and
- method of measurement and payment.

It is recommended that micropile measurement and payment be performed on a unit-permicropile basis separately for: (1) furnished and installed production piles; (2) verification testing; and (3) proof testing, except for piles founded in rock, for which an add/deduct footage price may be included.

During the bidding process, micropile contractors prepare a preliminary design and a firm cost proposal based on the owner's plans and specifications. If the project is to be subcontracted, general contractors will receive bids from each specialty subcontractor and includes the best offer in their proposal. The name of the recommended micropile subcontractor is included in the general contractor's bid, which is then submitted. Once the contract has been awarded, the selected specialty contractor prepares working drawings and design calculations and submits them to the engineer for review and approval. After acceptance of the design, construction begins.

#### 9.3.2 Alternate Micropile Design

For the Alternate Microple Design method, the owner provides a base design in the contract documents utilizing a more traditional foundation support system. The contract documents allow alternate micropile designs to be submitted by the listed specialty contractors on a one-for-one pile replacement of the owner-designed pile system. The information described under Standard Design Type is also required. Alternatively, this approach can be used to allow micropile contractors to submit designs which include fewer higher capacity micropiles than the conventional pile footing design requires, and allows the owner's engineer to maintain control of the footing design.

The information necessary in the contract documents is similar to that previously mentioned, except the owner provides two to three alternative pile footing designs on the plans with the associated pile design and load criteria.

#### 9.3.3 Cost Reduction Incentive Proposal (Value Engineering)

The Cost Reduction Incentive Proposal is another long-established form of alternate proposal used in the United States. When Cost Reduction Incentive Proposals are permitted, it is important that the owner specify any additional restrictions that may apply, such as right-of-

way restrictions. Foundation support elements are usually the first order of work, so review and approval of the Cost Reduction Incentive Proposal needs to be performed in a timely manner.

#### 9.4 PERFORMANCE SPECIFICATIONS

This approach is often called "line and grade" or "conceptual plans". Under this approach, the agency: (1) prepares drawings defining the geometric requirements for the structure and material specifications for the components; (2) defines performance requirements including factors of safety; and (3) indicates the range of acceptable construction and design methods.

This approach, when coupled with sound specifications and pre-qualification of contractors, offers several benefits. Design of the structure is performed by trained and experienced staff and can utilize contractors' proprietary equipment and methods along with material components successfully and routinely used in the past. Also, the performance specification approach lessens engineering costs and manpower requirements for the agency and transfers some of the project design costs to construction. The disadvantage is that agency engineers must have adequate expertise to perform a design review, approve construction modifications, and engage a consultant with demonstrated proficiency in micropile technology. It is noted that the limitations previously described under the method approach for pre-qualification of contractors for certain public agencies also apply to pre-qualification with the performance contracting approach.

Bid quantities are obtained from specified pay limits denoted on the drawings and can be bid on a lump sum or unit-price basis. The basis for detailed designs to be submitted after contract award is detailed as a special provision, as would construction control and monitoring requirements. The special provision should clearly identify the required submittals, schedule for submittals, and schedule for review and approval of these submittals. Items to be contained in the special provision are calculations and shop drawing submittals.

In the design/build method, the owner's engineer typically provides the following information:

- scope of work;
- total structure loads;
- footing details;
- corrosion protection;

- micropile testing procedures and requirements;
- instrumentation requirements (if any);
- special design considerations (e.g., scour and liquefaction potential); and
- performance criteria.

The micropile contractor specifies the following:

- micropile construction process;
- micropile type and quantity;
- micropile design;
- revisions to footing details to accommodate micropile design; and
- pile top to footing connection design.

Based upon specified limitations and requirements, a design/build proposal is submitted, either before the bid advertisement (pre-bid), or after contract award (post-bid). Measurement and payment is typically made on a lump-sum basis.

#### 9.5 DESIGN/BUILD APPROACH

#### 9.5.1 General

In design/build construction, the specialty contractor becomes an important part of the project team and is involved in all foundation and ground-support aspects of the project. The micropile contractor is responsible for the adequacy of the design and construction and the owner is responsible for the accuracy of the information upon which the design is based. The two recommended types of contractor design/build specifications follow.

#### 9.5.2 Postbid Design

The contract documents for the postbid design/build method are prepared to allow for various contractor-designed alternatives. The owner's engineer provides design and detailing of ancillary structures, and the performance criteria and objectives necessary for the micropile system design and installation. This information includes, as a minimum, the following:

- geotechnical reports and data;
- structure loadings (axial, lateral and moment);
- existing utility drawings;
- design criteria and parameters;
- site limitations (e.g., right of way);
- design and details of ancillary structures;
- contractor working drawing/design submittal and review requirements; and
- micropile acceptance criteria.

During the bidding process, the micropile contractors prepare a preliminary design and a firm cost proposal based on the owner's plans and specifications. For subcontracted items, general contractors will receive bids from each specialty subcontractor and include the best cost proposals in their bids. The name of the recommended micropile subcontractors are included in the general contractor's bid, which is then submitted. Once the contract has been awarded, the selected specialty contractor prepares their detailed design calculations and working drawing and submits them to the engineer for review and approval. After acceptance of the design, construction begins.

#### 9.5.3 Prebid Design

The contract documents for the prebid design/build method are also prepared to allow for contractor-designed micropiling alternatives. The major difference in this method is the timing of the design and the bidding. Performance criteria and necessary project design information are usually made available 60 to 90 days prior to the contract advertisement date. Micropile contractors prepare and submit final design calculations and working drawings for the owner's review and approval. Once the designs (typically two to three total) are approved, a list of specialty contractors with approved designs are included in the contract documents. Often the specialty contractors' proprietary working drawings are included in the contract bid documents. These drawings illustrate the proposed construction and assist the general contractors in understanding and coordinating their other project tasks with the proposed micropile construction. General contractors then receive bids from each subcontractor, bidding only on their own proprietary design, and include the best cost proposal in their bid. The name of the recommended micropile subcontractor is included in

the general contractor's bid, which is then submitted. Once the contract is awarded, the selected general contractor and specialty micropile contractor can begin work immediately.

#### 9.6 CONTRACT PLANS

For all of the specification methods mentioned, the contract plans must include sufficient information to allow the contractor to develop a bid proposal that meets the owner's objectives. The quality of the subsurface information, existing utility plan, and micropile design criteria are very important for a successful project. Inadequate subsurface information and conservative pile design criteria may create expensive contractor contingencies, higher pile prices and increase claim potential.

Sample contract plans and guide construction specifications utilizing owner controlled design methods is provided in Appendix C-1 and utilizing contractor design/build methods is provided in Appendix C-2.

#### CHAPTER 10 COST ESTIMATING

#### 10.1 INTRODUCTION

The purpose of this chapter is to present an approach that may be used to develop a cost estimate for any micropile project. The cost estimate method described is similar to that commonly used in engineering to develop a conceptual cost estimate. That is, sufficient detail is used to identify the cost components which may have the largest effect on total project cost, however specific bid quantities and potential bidding contractors is not necessarily known.

The method requires that a baseline cost for micropiles be known. Over the past ten years, numerous micropile projects have been completed in the United States and typical micropile costs have decreased during this time period mostly due to experience gained by specialty micropile contractors and advances in micropile installation equipment. In 2004, a reasonable "average" price for micropiles is on the order of \$300 per linear meter of micropile. This value is considered to be appropriate for any region of the U.S. and for any type of micropile project. The cost estimate method presented herein is used to adjust this baseline average price to account for project-specific technical and non-technical constraints.

Prior to describing the cost estimating method for micropiles, a discussion on the key factors which affect micropile costs is presented.

#### 10.2 FACTORS THAT INFLUENCE MICROPILE COSTS

#### **10.2.1 Overview**

Table 10-1 provides a breakdown of the typical ranges of costs for materials, labor, and equipment for micropiles. Also listed as a separate component is load testing costs. In many cases, load testing costs may be paid for as a separate pay item.

#### **10.2.2** Micropile Material Costs

The principal material components of micropiles include threaded steel casings, cement grout, steel reinforcing bars, and centralizers. Because of higher load capacities that continue to be achieved by micropiles, it is clear that costs for structural steel within the micropile cross section represent a significant cost component.

Table 10-1. Typical Breakdown of Micropile Unit Costs.

Unit Cost Breakdown	Percent
Material	25 – 40
Equipment	20 – 30
Labor	25 – 60
Load Testing	<5

#### Threaded Steel Casing

The most commonly used casings for micropile applications in the United States have outside diameters of 140 mm (5.5 in.), 175 mm (7 in.), and 241 mm (9-5/8 in.). The cost of each casing type (without threads) is provided in Table 10-2. These costs are subject to relatively large fluctuations in the prevailing cost of steel and the costs provided are considered to be representative for 2004. In some cases, contractors may have access to previously used casings which would likely reduce steel material costs.

Table 10-2. Material Costs of Steel Casings Used for Micropiles.

Casing Outside Diameter		Casing Wal	ll Thickness	Cost of casing (\$)	
(mm)	(in)	(mm)	(in)	per meter	per foot
139.7	5.500	10.5	0.415	15 – 25	5 – 8
177.8	7.000	12.6	0.498	35 – 45	11 – 14
244.5	9.625	13.8	0.545	50 – 60	15 – 18

Note: Representative early 2004 costs.

Because of low headroom conditions or difficult access, micropile casings are oftentimes installed in relatively short sections, thereby requiring a means to connect individual casing sections. Joints for casing are typically flush threaded joints. Threading costs wherein both ends are threaded (i.e., male and female threads) will typically cost in the range of \$50 to \$70 (2004) per casing. Therefore, where short casing lengths are required, threading costs can be relatively significant and the Owner should carefully assess the specific requirements for casing section lengths for a project. For example, where the cost of a 1-m-long 140-mm-

casing may be on the order of \$20, threading costs for each 1-m section may be on the order of \$60, or 3 times the casing cost. Alternatively, the threading cost of a 4-m-long 140-mm-casing would be less than the cost of the casing itself.

#### Steel Reinforcing Rods

The most commonly used reinforcement bars for micropile applications in the United States have outside diameter of 57 mm (2-1/4 in.) and 64 mm (2-1/2 in.). The 2004 material costs for these reinforcement bars are provided in Table 10-3. Centralizer material costs are relatively insignificant.

Table 10-3. Material Costs of Steel Reinforcing Bars Used for Micropiles.

Bar Size #	Outside D	Outside Diameter		Cost of reinforcing bar (\$)		
Dai Size#	(mm)	(in)	per meter	per foot		
18	57	2.25	20 – 26	6 – 8		
20	64	2.5	26 – 32	8 – 10		

Note: Representative early 2004 costs

#### **10.2.3** Equipment Cost

Overall equipment costs for micropile projects have decreased in recent years mostly due to the greater availability of drilling and grouting equipment. While it is difficult to assign specific costs for equipment, since they represent fixed costs for a contractor on a given project, the Owner should recognize that drilling equipment costs will be linked to ground conditions and the relative ease of drilling. Drilling costs for micropiles in excessively hard or bouldery ground to relatively great depths (e.g., greater than say 30 m (100 ft)) will be significant. Usually smaller drilling equipment may be less costly than larger equipment; however, for very tight access conditions with low headroom (e.g., less than say 3 m (10 ft)) and difficult drilling conditions, specialized equipment will be required. Depending on the specialty contractor, the use of this equipment may represent a significant cost.

#### 10.2.4 Labor Cost

A typical micropile crew consists of four individuals including a project superintendent, drilling operator, and two laborers. The effect of labor on micropile unit costs are directly linked to the ease of installation and daily micropile installation rates.

For projects involving relatively easy drilling and low to moderate capacity micropiles, a typical crew may install up to 6 to 20, 15-m (50-ft) long (maximum) micropiles per day. For such a project, labor may comprise 25 to 30 percent of the total project cost. However, in tight access areas and difficult drilling conditions the labor cost may increase to 30 to 45 percent of the total cost due to extra time and effort required. In extra labor-intensive projects and where prevailing labor costs are high (e.g., major urban areas), labor cost may comprise up to 60 percent of the micropile costs.

#### 10.2.5 Load Testing Costs

Load testing costs depend on the access conditions of the site, the type of testing (i.e., compression, tension, and/or lateral load testing), the number of tests, testing protocol (i.e., "quick" load or standard load tests), and the required load capacity.

The engineer will typically select the number and type of load tests, however, compression load tests will always be more expensive than a comparable (i.e., similar maximum testing load) tension test. The primary reason for this is that reaction piles or anchors need to be constructed for the compression test. The cost range for verification load tests range from \$10,000 to \$25,000 per test with the lower end of the range being representative for tension tests and the upper end being representative for compression tests. Proof tests (which are commonly carried to significantly lower loads than verification tests and which are performed in less time) range in cost from \$6,000 to \$10,000. These costs are considered representative for typical projects.

Where very difficult access limits equipment access, load testing costs can be significantly higher. For example, high load capacity load tests in an easy access area may be on the order of \$25,000 per test whereas for difficult access areas and where relatively high load capacities need to be verified (e.g., greater than 200 tons), load tests could be greater than \$50,000 per test.

#### 10.3 MICROPILE COST ANALYSIS

#### 10.3.1 Overview

An Owner considering the use of micropiles for a project may use the previously provided average cost of \$300 per linear meter with the modifications provided in Table 10-4 to develop a preliminary cost estimate for their specific project. Table 10-4 has been developed based on micropile contractor input and reflects the relative effect of project-specific factors on micropile construction costs. The use of this table is described subsequently using two example projects and additional discussion on the specific factors provided in this table is also provided.

Table 10-4. Effects of Project-Specific Factors on Micropile Cost.

Cost Factor	Influence Range	Cost Influence
Physical and access conditions	Very easy to very difficult	0% to +100%
Geology/ground conditions	Very easy to very difficult	0% to +50%
Pile capacity	Very low to very high ⁽¹⁾	-30% to +30%
Pile lengths	Very short to very long ⁽²⁾	-25% to +25%
Pile quantities	Very high to very low ⁽³⁾	-50% to +100%
Testing requirements	Very low to very high ⁽⁴⁾	-10% to +10%
Mobilization/demobilization	One to multiple	0% to +10%
Continuous drilling operations	Continuous to not continuous ⁽⁵⁾	0% to +25%
Union agreements	Nonunion to very strong	-15% to +30%
Overhead and profit	Very low to very high	-10% to +100%

Notes: (1)Moderate pile capacity = 1,000 kN (225 kips).

 $^{^{(2)}}$ Average pile length = 15 m (50 ft).

 $^{^{(3)}}$ Average pile quantity = 50.

⁽⁴⁾ Average is one verification test and proof testing 5% of all piles.

⁽⁵⁾ Not continuous drilling operation implies significant down time periods during drilling operations.

#### 10.3.2 Effects of Project-Specific Constraints on Cost

The first two factors in Table 10-4 concerning access and ground conditions are shown to have a large effect on micropile cost. Effects related to difficult access and difficult ground conditions (e.g., drilling in excessively hard ground), however, would likely have a similar cost implication for driven piles and drilled shafts as well.

Pile capacity affects cost since higher capacity micropiles will require longer bond zone lengths which may comprise longer rock sockets than would be required for more moderately loaded micropiles. Also, greater structural requirements (i.e., increased steel area) are associated with higher capacity micropiles.

The length of a pile effects costs in several ways, for example:

- the longer the pile length, the more individual sections of steel casing will be required;
- beyond certain lengths, drilling costs may increase because of the need for more robust equipment to reach greater depths; and
- greater need may exist for hole stabilization at significant depths.

Table 10-4 indicates that the most significant relative cost reduction is associated with pile quantities. Large pile projects will enable the contractor to define project backlog and long-term personnel requirements.

The last entry in Table 10-4 (i.e., overhead and profit) relates to perceived contractor risk for a particular project. While this factor may be difficult for an Owner to assess as part of a preliminary cost estimate, should other factors in Table 10-4 generally result in increases above the average cost, it is reasonable to assume that a contractor may view the project as containing relatively significant risk, especially where ground conditions are expected to result in difficult drilling and low productivity.

#### **10.3.3** Micropile Cost Estimate Examples

The use of Table 10-4 is demonstrated in two sample problems provided below.

#### 10.3.3.1 Sample Problem No. 1 (Bridge Abutment Support)

Given: Single-span bridge located in mountainous terrain approximately 125 km northwest of Denver, Colorado. Each abutment is to be supported on 12 CASE 1, Type B micropiles with ultimate capacities of 1,190 kN (270 kips) in compression, and 490 kN (110 kips) in tension, and approximately 12 m (40 ft)

in length. Testing requirements are one verification pile load test (compression only) on a sacrificial pile and two proof tests. Access to each work bench must be established. Drilling of bond zone is expected to be very difficult, due to cobbles and boulders. Drilling will be continuous at each location with an additional set-up of Abutment 2.

Solution: Evaluate each influence factor as shown in Table 10-5 below and multiply by cost of micropile per meter price.

Based on Table 10-5 the cost is adjusted as:

Average cost (\$) = \$300 x 
$$\left[1 + \frac{85}{100}\right]$$
 = \$555 / linear meter of micropile

The length of each micropile is 12 m (40 ft), therefore the unit price would be;

Average cost (\$) = 
$$$555 \times 12 \text{ m} = $6,660 / \text{ each}$$

Table 10-5. Sample Problem No. 1 – Cost Analysis (Bridge Abutment Support).

Cost Factor	Influence	Cost Influence (%)
Physical and access conditions	Easy access	10
Geology/ground conditions	Difficult drilling	30
Pile capacity	Moderate pile capacity	0
Pile lengths	Average pile lengths	0
Pile quantities	Low pile quantities	25
Testing requirements	Average # of testing	10
Mobilization/demobilization	One mobilization	0
Continuous drilling operations	Two setups	5
Union agreements	Standard union agreements	0
Overhead and profit	High-risk project	5
	Total:	85%

#### 10.3.3.2 Sample Problem No. 2 (Seismic Retrofit)

Given: Seismic retrofit of a 200-m (650-ft) long concrete viaduct located in San Francisco, California. A total of 30 footings need retrofitting with 12 Type B micropiles per footing (resulting in a total of 360 micropiles for the project). Ultimate capacities are 2,500 kN (560 kips) in compression and 1,500 kN (340 kips) in tension. Subsurface profile includes approximately 10 to 12 meters (330 to 40 ft) of medium dense silty sands over weathered to moderately weathered serpentine bedrock. Micropiles average approximately 20 meters (66 ft) in length. Testing requirements include 1 verification pile load test (compression only) on a sacrificial pile and 30 proof tests. Access to each pile location is good, and overhead clearance varies between 5 to 12 meters (16 to 40 ft) for each footing. Drilling is assumed to be continuous allowing setups between each footing.

Solution: Evaluate each influence factor as shown in Table 10-6 below and multiply by cost of micropile per meter price.

Based on Table 10-6 the cost could be adjusted as:

Average cost (\$) = \$300 x 
$$\left[1 + \frac{10}{100}\right]$$
 = \$330 / linear meter of micropile

The length of each micropile is 20 m, therefore the unit price would be;

Average cost (
$$\$$$
) =  $\$330 \times 20 = \$6,600 / each$ 

#### 10.4 MEASUREMENT AND PAYMENT FOR MICROPILES

Table 10-7 provides a summary of typical pay items for a micropile project. It is recognized that design-build projects may use lump sum units for most of the pay items. With respect to payment for the micropile itself, alternative pricing may include payment per unit length of micropile or payment per pile with an add or deduct if actual pile lengths vary from a predetermined pile length used for the bid.

Table 10-6. Sample Problem No. 2 – Cost Analysis (Seismic Retrofit).

Cost Factor	Influence	Cost Influence (%)
Physical and access conditions	Easy access	10
Geology/ground conditions	Easy drilling	10
Pile capacity	High pile capacities	10
Pile lengths	Moderate pile lengths	0
Pile quantities	Large pile quantity	-30
Testing requirements	Relatively extensive	5
Mobilization/demobilization	One mobilization	0
Continuous drilling operations	Continuous drilling	0
Union agreements	Strong union	10
Overhead and profit	Lower risk project	-5
	Total	10%

Additional pay items will be required for projects involving difficult ground in which specific problems may be anticipated during the bid period. For example, where micropiles are to be installed in karstic regions, a pay item should be developed for grout volume above some minimum volume. However, specifications should require that where grout volumes are no greater than two times the theoretical volume of the drillhole, that there is no additional compensation for grouting, i.e., the per pile cost for a micropile shall include grout volumes up to two times the theoretical grout volume. Also, if obstructions are anticipated, the specifications should include a pay item for removal of obstructions. Payment for obstruction removal may be performed on a time and material basis. Where this approach is used, it is important to use a contractor with previous experience in similar ground conditions and to provide full-time construction inspection during obstruction removal. Whenever a time and material basis may be used for payment on a project, the Owner should request detailed information on labor and material charges as part of the contractor's bid.

Table 10-7. Micropile Measurement and Payment Units.

Description	Unit
Mobilization/Demobilization	Lump sum
Conduct Preproduction Test Pile Program	Lump sum
Verification Load Test	Per each
Proof Load Test	Per each
Furnish and install micropile (foundation support)	Per each
Furnish and install micropile (slope stabilization)	Per lineal meter of cap beam

#### **GLOSSARY OF TERMS**

- **Admixture:** Substance added to the grout to control bleed and/or shrinkage, improve flowability, reduce water content, or retard setting time.
- **Alignment Load (AL):** A minimum load applied to micropile during testing to keep the testing equipment correctly positioned.
- **Bond Length or Bond Zone:** The length of the micropile that is bonded to the ground and used to transfer the applied axial loads to the surrounding soil or rock.
- **Bond-breaker:** A sleeve placed over the steel reinforcement to prevent load transfer.
- **CASE 1 Micropile:** A pile designed to accept vertical or lateral load directly, and transfer it to an appropriate bearing stratum. Usually includes significant steel reinforcement.
- **CASE 2 Micropile:** One of a network of low-capacity piles used to delineate and internally reinforce a volume of soil.
- **Casing:** Steel tube introduced during the drilling process in overburden soil to temporarily stabilize the drill hole. This is usually withdrawn as the pile is grouted, although in certain types of micropiles, some casing is permanently left in place to reinforce the unbonded length or provide additional capacity.
- **Centralizer:** A device to support and position the reinforcing steel in the drill hole and/or casing so that a minimum grout cover is provided.
- **Coarse-grained Soils:** Soils with more than 50 percent of the material by weight, larger than the No. 200 (0.075 mm) sieve size.
- **Cohesive Soils:** Fine-grain soils that exhibit plasticity. Atterberg limits are commonly used to determine plasticity and better define a soil as cohesive or noncohesive.
- **Contractor:** The person/firm responsible for performing the micropile work.
- **Corrosion-inhibiting Compound:** Material used to protect against corrosion and/or lubricate the reinforcing steel.
- **Coupler:** A device by which the pile load capacity can be transmitted from one partial length of reinforcement to another.

- **Creep Movement:** The movement that occurs during the creep test of a micropile under a constant load.
- **Design Load (DL):** The maximum load expected to be applied to the micropile during its service life.
- **Duplex Drilling:** An overburden drilling system involving the simultaneous advancement of (inner) drill rod and (outer) drill casing. Flush from the inner drill rod exits the hole via the annulus between rod and casing.
- **Elastic Movement:** The recoverable movement measured during a micropile test.
- **Encapsulation:** A grout filled corrugated or deformed tube protecting the reinforcing steel against corrosion.
- **Fine-grained Soils:** Soils with at least 50 percent of the material, by weight, smaller than the No. 200 (0.075 mm) sieve size.
- **Free (unbonded) Length:** The designed length of the micropile that is not bonded to the surrounding ground or grout during stressing.
- **Maximum Test Load:** The maximum load to which the micropile is subjected during testing.
- **Micropile:** A small-diameter (typically less than 300 mm) drilled and grouted replacement pile which is typically reinforced.
- **Non-cohesive Soils:** Granular soils that are generally nonplastic.
- **Overburden:** Material, natural or placed, that requires cased drilling methods to provide an open borehole to underlying strata.
- **Permanent Micropile:** Any micropile for permanent use, generally with more than a 24-month service life. May require special design, corrosion protection, and supervision during installation.
- **Plunge Length:** The length that the pile casing is inserted into the bond zone.
- **Post-grouting:** The injection of additional grout into the load transfer length of a micropile after the primary grout has set. Also known as regrouting or secondary grouting.
- **Preloading:** Loading the micropile prior to the connection to the structure, to minimize or eliminate any structural movement in service.

- **Primary Grout:** Portland-cement-based grout injected into the micropile hole prior to or after the installation of the reinforcement to direct the load transfer to the surrounding ground.
- **Proof Test:** Incremental loading of a production micropile, recording the total movement at each increment.
- **Reinforcement:** The steel component of the micropile that accepts and/or resists applied loadings.
- **Residual Movement:** The nonrecoverable movement of a micropile measured during load testing.
- **Sheath:** A smooth or corrugated pipe or tube that protects the reinforcing steel against corrosion.
- **Single-tube Drilling:** The advancement of a steel casing through overburden, usually aided by water flushing through the casing. The water may or may not return to the surface around the casing, depending largely on the permeability of the overburden.
- **Spacer:** A device to separate elements of a multiple-element reinforcement to ensure full bond development of each steel element.
- **Temporary Micropile:** Any micropile for temporary use, generally with less than a 24-month service life
- **Ultimate Grout-to-Ground Bond Values:** The estimated ultimate geotechnical unit grout-to-ground bond strength selected for use in design.
- **Verification Load Test:** Non-production (sacrificial) pile load test performed to verify the design of the pile system and the construction methods proposed, prior to installation of production piles.
- Working Load: Equivalent term of Design Load.

#### **APPENDIX A**

# DESIGN CONCEPT OF CASE 2 MICROPILE NETWORKS FOR SLOPE STABILIZATION

The CASE 2 micropile network design concept developed by Dr. Lizzi and illustrated in Figure 3-14 consists of "a three-dimensional lattice structure built into the soil according to a pre-established scheme depending on the purpose that the structure has to carry out," (Lizzi 1971). The purpose of the micropile network for slope stability is two fold:

- a) The micropiles must retain the soil and prevent its "flow" through the network formed by the piles, which would cause a reduction of the continuity and the unity of the composite gravity structure.
- b) The micropiles must supply a nailing of the various soil layers by providing additional shear resistance along the possible critical sliding surfaces.

The soil-pile interaction for such micropile networks is very complex and there are many factors whose influence on the final behavior of the structure cannot be conveniently assessed. Lizzi suggested that designs be based on "some simple assumptions" using the concept of reinforced soil, and those used for reinforced concrete. The soil supplies the weight in a manner more or less as supplied in a monolithic gravity wall, whereas the micropiles, introducing reinforcing elements into the soil, supply the lines of force, allowing the composite mass to support compression, tension, and shear stresses. The system is based on the micropile-soil interaction, which results in a network (or "knot") effect provided the micropiles are not too far apart.

The first official test on a full-size reticulated micropile structure was performed in 1957 for the Milan, Italy subway system. The knot affect has been confirmed by both model and earlier field tests (Lizzi 1978, Plumelle 1984, and Korfiatis 1984). Apart from several earlier tests on models and full-scale structures, a recent French National Project on micropiles (FOREVER 2003) includes experimental studies on the behavior of micropile networks. The findings of this research indicates that in loose to medium dense granular soils, a positive network effect can be obtained if adequate densification of the soil is assured and if the micropiles are concentrated as much as possible under the applied load. According to the researchers, this implies that the micropiles do not move apart or diverge from the surface of the foundation but, rather turn inwards in order to ensure a maximum densification of the soil. No design guidelines have been developed as yet from this project.

The design of Case 2 micropiles assumes a highly redundant system in which no tension is applied to any of the piles. Therefore, the system is subjected to compression and shear and the micropile network provides confinement to the in-situ soil, thereby improving its deformation modulus and increasing its shear resistance. The behavior of this system depends to a great extent on the knot effect concept and the reinforced concrete analogy. Once the knot effect is assured, the micropile enclosed soil mass behaves as a coherent body

and is analyzed as a gravity retaining structure. Using this concept, the following steps can be followed for preliminary design of Case 2 micropile networks:

- 1. Conduct a slope stability analysis to determine the increased resistance required ( $H_{req}$ ) along an existing failure surface to provide a specified target factor of safety,  $FS_{TARGET}$ .
- 2. Develop the initial geometry of the micropile structure. Assume a pile configuration that is dense enough to assure a knot effect and minimize the possibility of plastic flow between piles. A preliminary configuration can be based on density of 6 to 7 piles per linear meter along the wall alignment. Stability related to the plastic flow of soil between piles can be verified using the methods presented in Section 6.6.7.
- 3. Check the external stability of the micropile structure
  - 3.1. Estimate the earth pressure against the micropile structure using conventional earth pressure theories.
  - 3.2. Check the factor of safety against overturning  $(FS_{OV})$  assuming the micropile structure is a rigid body:

$$FS_{OV} = \frac{\sum M_{\text{resisting}}}{\sum M_{\text{overturning}}} \ge 2.0$$
 (Eq. A-1)

To resist the overturning moment and to maintain compression stresses in the soil and in all micropiles, the resultant vertical force (from earth pressures and other external forces) should act in the middle third of the micropile structure.

3.3. Check the factor of safety against sliding (FS_{SL}):

$$FS_{SL} = \frac{(\sum Vertical\ Loads)(Shear\ strength\ of\ base\ soil) + (Shear\ capacity\ of\ piles)}{\sum Horizontal\ Loads} \geq 1.5\ (Eq.\ A-2)$$

3.4. Assume a micropile cross section and determine the contact stresses at the edge of the base of the micropile structure for a given micropile cross section. The contact stresses at the edges of the micropile structure is calculated according to:

$$\sigma = \frac{P}{A_{trans}} \pm \frac{Pe}{I_{trans}} \left(\frac{b}{2}\right)$$
 (Eq. A-3)

Where:

P = vertical component of the resultant force acting on the structure;

e = eccentricity of the force P;

 $A_{trans}$  = area of the transformed micropile section;

 $I_{trans}$  = moment of inertia at the base of the structure; and

b = width of the transformed section.

The transformed section area, A_{trans} is calculated as:

$$\mathbf{A}_{\text{trans}} = \mathbf{A}_{\text{conc}} \frac{\mathbf{E}_{\text{conc}}}{\mathbf{E}_{\text{soil}}} + \mathbf{A}_{\text{stl}} \frac{\mathbf{E}_{\text{stl}}}{\mathbf{E}_{\text{soil}}}$$
 (Eq. A-4)

Where:

 $A_{conc}$  = area of the concrete;

 $A_{stl}$  = area of the steel;

 $E_{conc}$  = Young's modulus of the concrete;

 $E_{stl}$  = Young's modulus of the reinforcing steel; and

 $E_{\text{soil}}$  = Young's modulus of the soil.

The moment of inertia at the base at the structure, I_{trans}, is computed by assigning equivalent areas of soil to the concrete and steel based upon the ratios of Young's moduli.

The minimum stress calculated according to Eq. A-3 should be positive indicating that all contact stresses are in compression.

- 3.5. Using the stresses computed, determine the maximum compression stresses in each component of the composite section (i.e., concrete, steel reinforcement, and soil). Check these compression stresses against allowable design values.
- 4. Check the internal stability of the micropile structure

Design each micropile to resist the stresses calculated in Step 3.5. Compute shear resistance of the piles and the lateral resistance of the soil in contact with the piles. The smaller of the two resistances is considered as the additional shear resistance due to micropiles  $(R_1)$ .

5. Determine the number of micropiles (n) for the micropile structure using:

$$FS_{TARGET} = \frac{\left(R + H_{req}\right)}{D} \text{ and } H_{req} = n R_1$$
 (Eq. A-5)

Where:

R = horizontal component of the soil resisting forces along the critical slip surface; and

D = horizontal component of the driving force along the critical slip surface.

The above referenced design procedure has not yet been proven by long term instrumented field performance. It is recommended that owners considering the use of these types of slope stabilization structures implement a long-term instrumentation program to fully understand the behavior and performance of the structure.

#### APPENDIX B

### LPILE ANALYSIS RESULTS FOR SLOPE STABILIZATION PROBLEM

```
LPILE Plus for Windows, Version 4.0 (4.0.8)
                  Analysis of Individual Piles and Drilled Shafts
                 Subjected to Lateral Loading Using the p-y Method
                         (c) Copyright ENSOFT, Inc., 1985-2003
                                    All Rights Reserved
Path to file locations: L:\Programs\LPILE
Name of input data file: 1st analysis.lpd
Name of output file: 1st analysis.lpo
Name of plot output file: 1st analysis.lpp
Name of runtime file: 1st analysis.lpr
Path to file locations:
                                   L:\Programs\LPILE\Chapter 6\Ch. 6 Example with P=474.5\
Time and Date of Analysis
                  Date: May 4, 2005 Time: 15:26: 0
______
                              Problem Title
1<sup>st</sup> Analysis
(To Determine M<sub>ult</sub> for P=0 and P=P<sub>ult</sub> Cases)
______
                                      Program Options
Units Used in Computations - SI Units, meters, kilopascals
Basic Program Options:
Analysis Type 3:
- Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment
  Capacity with Pile Response Computed Using Nonlinear EI
Computation Options:
Computation Options:

Only internally-generated p-y curves used in analysis

Analysis uses p-y multiplers for group action

Analysis assumes no shear resistance at pile tip

Analysis for fixed-length pile or shaft only

No computation of foundation stiffness matrix elements

Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths
Solution Control Parameters:
Number of pile increments =Maximum number of iterations allowed =
                                                             145
100
- Deflection tolerance for convergence =
- Maximum allowable deflection =
                                                     10.000E-07 m
- Maximum allowable deflection
                                                     2.5400E+00 m
Printing Options:
- Values of pile-head deflection, bending moment, shear force, and soil reaction are printed for full length of pile.
- Printing Increment (spacing of output points) = 1
                     Pile Structural Properties and Geometry
Pile Length = 14.50 m 
 Depth of ground surface below top of pile = .00 m 
 Slope angle of ground surface = .00 deg.
Structural properties of pile defined using 2 points
```

Point	Depth X m	Pile Diameter m	Moment of Inertia m**4	Pile Area Sq. m	Modulus of Elasticity kN/Sq. m
1	0.0000	.1778	1.0000	.0248	200000000.000
2	14.5000	1778	1.0000	.0248	200000000.000

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of moment of inertia and modulus of are not used for any computations other than total stress due to combined axial loading and bending.

Soil and Rock Layering Information

The soil profile is modelled using 3 layers

Layer 1 is stiff clay without free water Distance from top of pile to top of layer = .000 m Distance from top of pile to bottom of layer = 4.700 m p-y subgrade modulus k for top of soil layer = 1.000 kN/ m**3 p-y subgrade modulus k for bottom of layer = 1.000 kN/ m**3

Layer 2 is stiff clay without free water Distance from top of pile to top of layer = 4.700 m Distance from top of pile to bottom of layer = 10.000 m p-y subgrade modulus k for top of soil layer = 1.000 kN/ m**3 p-y subgrade modulus k for bottom of layer = 1.000 kN/ m**3

Layer 3 is stiff clay without free water Distance from top of pile to top of layer = 10.000 m Distance from top of pile to bottom of layer = 16.000 m p-y subgrade modulus k for top of soil layer = 1.000 kN/ m**3 p-y subgrade modulus k for bottom of layer = 1.000 kN/ m**3

(Depth of lowest layer extends 1.50 m below pile tip)

Effective Unit Weight of Soil vs. Depth

Distribution of effective unit weight of soil with depth is defined using  $\,$  6 points

Point No.	Depth X m	Eff. Unit Weight kN/ m**3
1	.00	21.20000
2	4.70	21.20000
3	4.70	11.40000
4	10.00	11.40000
5	10.00	13.20000
6	16.00	13.20000

Shear Strength of Soils

Distribution of shear strength parameters with depth defined using  $\ 6\ \text{points}$ 

Point No.	Depth X m	Cohesion c kN/ m**2	Angle of Friction Deg.	E50 or k_rm	RQD %
1	.000	120.00000	.00	.00500	. 0
2	4.700	120.00000	.00	.00500	. 0
3	4.700	168.00000	.00	.00400	. 0
4	10.000	168.00000	.00	.00400	. 0
5	10.000	480.00000	.00	.00250	. 0
6	16.000	480.00000	.00	.00250	.0

Notes:

(1) Cohesion = uniaxial compressive strength for rock materials.

- (2) Values of E50 are reported for clay strata.(3) Default values will be generated for E50 when input values are 0.
- (4) RQD and k_rm are reported only for weak rock strata.

p-y Modification Factors

Distribution of p-y multipliers with depth defined using 2 points

Point No.	Depth X m	p-mult	y-mult
1	.000	1.0000	1.0000
2	.000	1.0000	1.0000

Loading Type _____

Static loading criteria was used for computation of p-y curves

Pile-head Loading and Pile-head Fixity Conditions _______

Number of loads specified = 1

Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1) Shear force at pile head = .000 kN Bending moment at pile head = .000 m- kN Axial load at pile head = .000 kN (Zero moment at pile head for this load indicates a free-head condition)

Output of p-y Curves at Specified Depths

p-y curves are generated and printed for verification at 8 depths.

Depth No.	Depth Below Pile Head m	Depth Below Ground Surface $\ensuremath{\mathfrak{m}}$
1	.000	.000
2	1.000	1.000
3	2.000	2.000
4	4.690	4.690
5	4.710	4.710
6	9.990	9.990
7	10.010	10.010
8	14.500	14.500

Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness

Pile Description:

The sectional shape is a circular shaft with steel casing.

.1778 m Outside Diameter Outside Diameter = .1778 m Wall thickness of steel shell = .0115 m Cross-sectional area of shell = .00601 m**2 Moment of inertia of steel shell = 2.08692E-05 m**4

Material Properties:

Compressive Strength of Concrete = 27600.000 kN/ m**2 Yield Stress of Reinforcement = 0. kN/ m**2 Steel shell or core yield stress = 552000. kN/ m**2

Modulus of Elasticity of Reinforcement = 200000000. kN/ m**2 Cover Thickness (edge to bar center) = .000 m

Number of Reinforcing Bars = 10 Area of Single Bar = .00000 m**2 Number of Rows of Reinforcing Bars = 5 Ultimate Axial Squash Load Capacity = 3758.02 kN

Distribution and Area of Steel Reinforcement

Row Number	Area of Reinforcement m**2	Distance to Centroidal Axis m
1	.000000	.0736
2	.000000	.0455
3	.000000	.0000
4	.000000	0455
5	.000000	0736

Axial Thrust Force = .00 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
Moment kN-m  1.73583660 2.50651820 3.27670667 4.04640201 4.81560422 5.58431330 6.35252925 6.55060560 7.25778201 7.96476385 8.67155112 9.37814382 10.085 10.791 11.497 12.203 12.908 13.614 14.319 15.024	Stiffness kN-m2  4898.917  4897.351  4895.785  4894.220  4892.654  4891.088  4889.522  4496.284  4495.667  4495.049  4494.431  4493.196  4492.578  4491.960  4491.342  4490.725  4490.107  4489.489	Curvature rad/m	Strain m/m	Position m08889729 .08889729 .08889729 .08889729 .08889729 .08889729 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207
16.433 17.138 17.842 23.118 28.383 33.636 38.879 44.111 49.332 54.542 57.662 62.752 67.845 72.947 78.054 83.173 88.306 93.456 98.635 103.850 109.135 116.274 121.355 126.423 131.480	4488.254 4487.636 4487.018 4482.385 4477.752 4473.118 4468.485 4463.852 4459.219 4454.586 4295.045 4296.211 4297.412 4298.973 4300.601 4302.638 4305.127 4308.127 4312.080 4317.171 4324.538 4401.446 4397.159 4392.803 4388.413	.00366142 .00381890 .00397638 .00515748 .00633858 .00751969 .00870079 .00988189 .01106299 .01224409 .01342520 .01460630 .01578740 .01696850 .01814961 .01933071 .02169291 .02287402 .02405512 .02523622 .02641732 .02759843 .02877953 .028996063	.00026169 .00027294 .00028420 .00028420 .00045303 .00053745 .00062186 .00070628 .00079069 .00087511 .00095982 .00104577 .00113196 .00121848 .00130527 .00147993 .00156786 .00165633 .00174537 .00183532 .00194228 .00203107	.08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08297207 .08299377 .08309687 .08319996 .08330848 .08341700 .08353095 .08365032 .08377512 .08391077 .08405727 .08402548 .08502310 .08509364 .08516418

136.408	4380.233	.03114173	.00229741	.08527270
141.002	4362.312	.03232283	.00238314	.08522929
145.110	4331.145	.03350394	.00246586	.08509907
145.110	4183.660	.03468504	.00250950	.08385108
147.008	4098.795	.03586614	.00257802	.08337902
153.523	4143.973	.03704724	.00264784	.08297207
155.871	4077.375	.03822835	.00273226	.08297207
157.833	4004.950	.03940945	.00281667	.08297207
159.521	3929.994	.04059055	.00290109	.08297207
161.057	3855.647	.04177165	.00298551	.08297207
162.411	3781.163	.04295276	.00306992	.08297207
163.614	3707.213	.04413386	.00315434	.08297207
164.745	3635.565	.04531496	.00323875	.08297207
165.711	3563.988	.04649606	.00332317	.08297207
166.656	3495.506	.04767717	.00340759	.08297207
167.455	3427.355	.04885827	.00349200	.08297207
168.240	3362.162	.05003937	.00357642	.08297207
168.926	3298.012	.05122047	.00366083	.08297207
169.575	3236.065	.05240157	.00374525	.08297207
170.188	3176.179	.05358268	.00382966	.08297207

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 161.289 m- kN

Axial Thrust Force = 474.50 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
1.69826245	4792.874	.00035433	.00031727	.90691267
2.45303965	4792.862	.00053133	.00032949	.65527803
3.20781175	4792.848	.00066929	.00034172	.52206775
3.96257836	4792.833	.00082677	.00031172	.43960844
4.71733626	4792.814	.00098425	.00033533	.38354674
5.47208598	4792.792	.00114173	.00037843	.34295465
6.22682760	4792.770	.00121173	.00037013	.31220536
6.98155916	4792.746	.00145669	.00040293	.28810838
7.73628058	4792.720	.00161417	.00041519	.26871577
8.49098340	4792.688	.00177165	.00042746	.25277953
9.24568013	4792.659	.00192913	.00043973	.23944236
10.000	4792.625	.00208661	.00045201	.22812367
10.755	4792.590	.00224409	.00046429	.21839481
11.510	4792.551	.00240157	.00047658	.20994649
12.264	4792.509	.00255906	.00048888	.20253996
13.019	4792.470	.00271654	.00050118	.19599075
13.774	4792.426	.00287402	.00051348	.19016320
14.528	4792.379	.00303150	.00052579	.18494336
15.283	4792.326	.00318898	.00053812	.18024442
16.035	4791.716	.00334646	.00055042	.17597957
16.774	4787.090	.00350394	.00056260	.17206198
17.571	4799.091	.00366142	.00057505	.16855677
18.301	4792.220	.00381890	.00058745	.16532828
19.053	4791.556	.00397638	.00059979	.16233854
24.610	4771.704	.00515748	.00068957	.14520315
29.767	4696.101	.00633858	.00078032	.13460612
35.334	4698.840	.00751969	.00087092	.12731897
39.786	4572.710	.00870079	.00095706	.12149685
45.804	4635.195	.00988189	.00105014	.11776917
50.555	4569.762	.01106299	.00113526	.11411745
56.180	4588.341	.01224409	.00122769	.11176798
61.386	4572.465	.01342520	.00131523	.10946735
64.845	4439.494	.01460630	.00139171	.10678147
71.647	4538.208	.01578740	.00149414	.10614120
74.736	4404.370	.01696850	.00156633	.10380800
81.890	4511.946	.01814961	.00167053	.10354213
85.716	4434.167	.01933071	.00175060	.10206082
92.018	4486.089	.02051181	.00183074	.10075315
97.124	4477.213	.02169291	.00193616	.10075315
102.139	4465.294	.02287402	.00202929	.10021598
105.295	4377.229	.02405512	.00210249	.09890288
109.026	4320.217	.02523622	.00218134	.09793705
113.742	4305.584	.02641732	.00227957	.09779054
118.611	4297.758	.02759843	.00238148	.09779054
127.233	4420.944	.02877953	.00247762	.09758978
131.954	4404.252	.02996063	.00257166	.09733476
136.319	4377.388	.03114173	.00266730	.09715027
140.277	4339.870	.03232283	.00276706	.09710686
143.850	4293.538	.03350394	.00287126	.09719911

```
      147.136
      4242.066
      .03468504
      .00297869

      150.123
      4185.651
      .03586614
      .00308557

      152.748
      4123.053
      .03704724
      .00319502

      152.748
      3995.667
      .03822835
      .00329874

      152.748
      3875.917
      .03940945
      .00340066

      154.387
      3803.521
      .04059055
      .00350258

      155.966
      3733.787
      .04177165
      .00360450

      157.340
      3663.103
      .04295276
      .00370642

      158.551
      3592.498
      .04413386
      .00380833

                                                                                                                               .09737816
                                                                                                                                 .09753009
                                                                                                                              .09779054
                                                                                                                              .09779054
                                                                                                                                 .09779054
                                                                                                                                 .09779054
                                                                                                                                 .09779054
                                                                                                                                 .09779054
 Ultimate Moment Capacity at a Concrete Strain of 0.003 =
                                                                                                                                    147.732 m- kN
p-y Curve Computed Using Criteria for Stiff Clay without Free Water
 Soil Layer Number
                                                                  .000 m
Depth below ground surface =
Depth below ground surface = .000 m

Equivalent Depth = .000 m

Diameter = .178 m

Undrained cohesion, c = 120.00000 kN/ m**2

Avg. Undrained cohesion, c = 120.00000 kN/ m**3

Epsilon-50 = .00500

Pct = 64.008 kN/ m

Pcd = 192.024 kN/ m

y50 = .002 m

p-multiplier = 1.00000

y-multiplier = 1.00000
                                           p, kN/ m
 y, m
                     .0000
                                                          .000
                     .0000
                                                    3.555
5.382
6.401
9.571
                                                         3.599
                     .0000
                     .0000
                     .0000
                     .0000
                                                     11.382
                                                     17.021
20.241
                      .0002
                     .0004
                      .0009
                                                       25.452
                                                     30.268
                      .0018
                      .0027
                                                     35.994
                      .0036
                      .0089
                                                      45.260
                                                      53.824
                      .0178
                      .0356
                                                      64.008
                      .0400
                                                      64.008
                      .0445
                                                       64.008
p-y Curve Computed Using Criteria for Stiff Clay without Free Water
```

```
      Soil Layer Number
      =
      1

      Depth below pile head
      =
      1.000 m

      Depth below ground surface
      =
      1.000 m

      Equivalent Depth
      =
      1.78 m

      Diameter
      =
      120.00000 kN/ m**2

      Avg. Undrained cohesion, c
      =
      120.00000 kN/ m**2

      Average Eff. Unit Weight
      =
      21.20000 kN/ m**3

      Epsilon-50
      =
      .00500

      Pct
      =
      127.777 kN/ m

      Pcd
      =
      192.024 kN/ m

      y50
      =
      .002

      p-multiplier
      =
      1.00000

      y-multiplier
      =
      1.00000
```

y, m	p, kN/m
.0000	.000
.0000	7.185
.0000	10.745
.0000	12.778
.0000	19.107
.0000	22.722
.0002	33.978
.0004	40.407
.0009	50.809
.0018	60.422
.0027	66.868
.0036	71.854
.0089	90.352

```
.0178 107.448
.0356 127.777
.0400 127.777
.0445 127.777
```

p-y Curve Computed Using Criteria for Stiff Clay without Free Water

```
      Soil Layer Number
      =
      1

      Depth below pile head
      =
      2.000 m

      Depth below ground surface
      =
      2.000 m

      Equivalent Depth
      =
      2.000 m

      Diameter
      =
      .178 m

      Undrained cohesion, c
      =
      120.00000 kN/ m**2

      Avg. Undrained cohesion, c
      =
      120.00000 kN/ m**3

      Epsilon-50
      =
      .00500

      Pct
      =
      191.547 kN/ m

      Pcd
      =
      192.024 kN/ m

      y50
      =
      .002 m

      p-multiplier
      =
      1.00000

      y-multiplier
      =
      1.00000
```

y, m	p, kN/m
.0000	.000
.0000	10.771
.0000	16.107
.0000	19.155
.0000	28.643
.0000	34.062
.0002	50.935
.0004	60.572
.0009	76.166
.0018	90.577
.0027	100.240
.0036	107.715
.0089	135.444
.0178	161.071
.0356	191.547
.0400	191.547
.0445	191.547

p-y Curve Computed Using Criteria for Stiff Clay without Free Water

```
      Soil Layer Number
      =
      1

      Depth below pile head
      =
      4.690 m

      Depth below ground surface
      =
      4.690 m

      Equivalent Depth
      =
      4.690 m

      Diameter
      =
      1.178 m

      Undrained cohesion, c
      =
      120.00000 kN/ m**2

      Avg. Undrained cohesion, c
      =
      120.00000 kN/ m**2

      Average Eff. Unit Weight
      =
      21.20000 kN/ m**3

      Epsilon-50
      =
      .00500

      Pct
      =
      363.086 kN/ m

      Pcd
      =
      192.024 kN/ m

      y50
      =
      .002 m

      p-multiplier
      =
      1.00000

      y-multiplier
      =
      1.00000
```

y, m	p, $kN/m$
y, m .0000 .0000 .0000 .0000 .0000 .0000 .0002 .0004 .0009 .0018 .0027 .0036 .0089 .0178	p, kN/m  .000 10.798 16.147 19.202 28.714 34.147 51.062 60.723 76.356 90.803 100.490 107.983 135.781 161.472
.0178 .0356 .0400 .0445	161.472 192.024 192.024 192.024

p-y Curve Computed Using Criteria for Stiff Clay without Free Water

```
Soil Layer Number = 2
Depth below pile head = 4.710 m
Depth below ground surface = 4.710 m
Equivalent Depth = 4.710 m
Diameter = .178 m
Undrained cohesion, c = 168.00000 kN/ m**2
Avg. Undrained cohesion, c = 168.00000 kN/ m**2
Average Eff. Unit Weight = 21.17919 kN/ m**3
Epsilon-50 = .00400
Pct = 502.977 kN/ m
Pcd = 268.834 kN/ m
y50 = .002 m
p-multiplier = 1.00000
```

y, m	p, $kN/m$
.0000	.000
.0000	15.118
.0000	22.606
.0000	26.883
.0000	40.200
.0000	47.806
.0001	71.487
.0003	85.013
.0007	106.898
.0014	127.124
.0021	140.685
.0028	151.176
.0071	190.094
.0142	226.061
.0284	268.834
.0320	268.834
.0356	268.834

p-y Curve Computed Using Criteria for Stiff Clay without Free Water

```
      Soil Layer Number
      =
      2

      Depth below pile head
      =
      9.990 m

      Depth below ground surface
      =
      9.990 m

      Equivalent Depth
      =
      9.990 m

      Diameter
      =
      1.78 m

      Undrained cohesion, c
      =
      168.00000 kN/ m**2

      Average Eff. Unit Weight
      =
      16.01061 kN/ m**3

      Epsilon-50
      =
      .00400 pct

      Pct
      =
      957.200 kN/ m

      Pcd
      =
      268.834 kN/ m

      y50
      =
      .002 m

      p-multiplier
      =
      1.00000

      y-multiplier
      =
      1.00000
```

```
p, kN/ m
y, m
        .0000
                        .000
                       15.118
        .0000
                      22.606
        .0000
        .0000
                     26.883
        .0000
                      40.200
        .0000
                      47.806
         .0001
                      71.487
        .0003
                      85.013
                    106.898
         .0007
                     127.124
        .0014
         .0021
                      140.685
         .0028
                     151.176
         .0071
                      190.094
                     226.061
         .0142
         .0284
                      268.834
         .0320
                      268.834
         .0356
                      268.834
```

p-y Curve Computed Using Criteria for Stiff Clay without Free Water

```
      Soil Layer Number
      =
      3

      Depth below pile head
      =
      10.010 m

      Depth below ground surface
      =
      10.010 m

      Equivalent Depth
      =
      8.863 m

      Diameter
      =
      .178 m

      Undrained cohesion, c
      =
      480.00000 kN

      Avg. Undrained cohesion, c
      =
      480.00000 kN

      Average Eff. Unit Weight
      =
      16.00320 kN

      Epsilon-50
      =
      .00250

      Pct
      =
      2408.297 kN

                                                                               kN/ m**2
                                                                               kN/ m**2
                                                                               kN/ m**3
                                                         .00250
2408.297
768.096
Pct
                                                                               kN/ m
Pcd
                                                                              kN/ m
y50
                                                                              m
                                                           1.00000
p-multiplier
y-multiplier
                                                              1.00000
                                p, kN/ m
 y, m
                .0000
                                                   .000
                  .0000
                                              43.193
                                       43.193
64.589
76.810
114.857
136.589
                  .0000
                  .0000
                  .0000
                  .0000
                                           204.248
242.893
305.422
363.210
401.958
431.932
                   .0001
                  .0002
                   .0004
                   .0009
                   .0013
                   .0018
                   .0044
                                           543.126
                   .0089
                                             645.889
                   .0178
                                             768.096
                   .0200
                                              768.096
                   .0222
                                             768.096
p-y Curve Computed Using Criteria for Stiff Clay without Free Water
Soil Layer Number = 3
Depth below pile head = 14.500
Depth below ground surface = 14.500
Equivalent Depth = 13.353
Diameter = .178
Undrained cohesion, c = 480.00000
Avg. Undrained cohesion, c = 480.00000
Average Eff. Unit Weight = 15.13517
Epsilon-50 = .00250
Pct = 3496.612
                                                                               kN/ m**2
                                                                               kN/ m**2
kN/ m**3
                                               = .00250
= 3496.612
= 768.096
= .001
= 1.00000
                                                                               kN/ m
Pcd
                                                                              kN/ m
y50
                                                                              m
p-multiplier
y-multiplier
                                   p, kN/ m
              y, m
                                      .000
                .0000
                  .0000
                                              43.193
                                            64.589
                  .0000
                  .0000
                                               76.810
                                      114.857
136.589
204.248
                  .0000
                  .0000
                   .0001
                                           204.248
242.893
305.422
363.210
401.958
431.932
543.126
                  .0002
                   .0004
                   .0009
                   .0013
                   .0018
                   .0044
                   .0089
                                            645.889
                   .0178
                                             768.096
                                             768.096
                   .0200
                   .0222
                                             768.096
                  Computed Values of Load Distribution and Deflection
                          for Lateral Loading for Load Case Number 1
Pile-head boundary conditions are Shear and Moment (BC Type 1)
Specified shear force at pile head =
                                                                                             .000 kN
```

(Zero moment for this load indicates free-head conditions)

0.000 0.000 0.000 0.0 0.0 0.0 0.0 0.0 0	Depth X m	Deflect. Y m	Moment M kN- m	Shear V kN	Slope S Rad.	Total Stress kN/ m**2	Flx. Rig. EI kN- m**2	Soil Res p kN/ m
.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .300 0.000 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.000 0.000 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.100 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.300 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.300 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 1.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4898.317 0.000 2.200 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0	0.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
.300 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .500 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 4888.317 0.000 .700 0.000 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0								
. \$400								
.500								
.700								
.800				0.0				0.000
1,900								
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4.100       0.000       0.0       0.000       0.0       4898.917       0.000         4.200       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         4.300       0.000       0.0       0.000       0.0       4898.917       0.000         4.400       0.000       0.0       0.000       0.0       4898.917       0.000         4.500       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         4.600       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         4.700       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         4.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         4.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         5.100       0.000       0.0       0.0       0.0       0.0       4898.917       0.000         5.200       0.000       0.0       0.0       0.0       0.0       4898.917       0.000         5.300       0.000 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>								
4.200       0.000       0.0       0.000       0.0       4898.917       0.000         4.300       0.000       0.0       0.000       0.000       0.000       4898.917       0.000         4.400       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         4.500       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         4.600       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         4.700       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         4.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         4.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         5.100       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         5.200       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         5.300       0.000       0.0       0.0       0.000       0.0       4898.917       0.000								
4.300       0.000       0.0       0.000       0.0       4898.917       0.000         4.400       0.000       0.0       0.000       0.0       4898.917       0.000         4.500       0.000       0.0       0.000       0.0       4898.917       0.000         4.600       0.000       0.0       0.000       0.0       4898.917       0.000         4.700       0.000       0.0       0.000       0.0       4898.917       0.000         4.800       0.000       0.0       0.000       0.0       4898.917       0.000         4.800       0.000       0.0       0.000       0.0       4898.917       0.000         4.900       0.000       0.0       0.000       0.0       4898.917       0.000         5.000       0.000       0.0       0.000       0.0       4898.917       0.000         5.100       0.000       0.0       0.000       0.0       4898.917       0.000         5.200       0.000       0.0       0.000       0.0       4898.917       0.000         5.300       0.000       0.0       0.000       0.0       4898.917       0.000         5.400       0.000								
4.400       0.000       0.0       0.000       0.0       4898.917       0.000         4.500       0.000       0.0       0.000       0.0       4898.917       0.000         4.600       0.000       0.0       0.000       0.0       4898.917       0.000         4.700       0.000       0.0       0.000       0.0       4898.917       0.000         4.800       0.000       0.0       0.000       0.0       4898.917       0.000         4.900       0.000       0.0       0.000       0.0       4898.917       0.000         5.000       0.000       0.0       0.000       0.0       4898.917       0.000         5.100       0.000       0.0       0.000       0.0       4898.917       0.000         5.200       0.000       0.0       0.000       0.0       4898.917       0.000         5.300       0.000       0.0       0.000       0.0       4898.917       0.000         5.400       0.000       0.0       0.000       0.0       4898.917       0.000         5.700       0.000       0.0       0.0       0.0       4898.917       0.000         5.800       0.000								
4.600       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0					0.000		4898.917	
4.700       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0								
4.800       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0								
5.000         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0								
5.100         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0								
5.200         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0								
5.300         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0								
5.500         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0	5.300	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
5.600         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0								
5.700         0.000         0.0         0.00         0.000         0.00         4898.917         0.000           5.800         0.000         0.0         0.000         0.000         0.0         4898.917         0.000           5.900         0.000         0.0         0.000         0.0         4898.917         0.000           6.000         0.000         0.0         0.000         0.0         4898.917         0.000           6.100         0.000         0.0         0.000         0.0         4898.917         0.000           6.200         0.000         0.0         0.000         0.0         4898.917         0.000           6.300         0.000         0.0         0.000         0.0         4898.917         0.000           6.400         0.000         0.0         0.000         0.0         4898.917         0.000           6.500         0.000         0.0         0.000         0.0         4898.917         0.000           6.600         0.000         0.0         0.000         0.0         4898.917         0.000           6.700         0.000         0.0         0.000         0.0         4898.917         0.000           6.800 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>								
5.900       0.000       0.0       0.000       0.000       0.04898.917       0.000         6.000       0.000       0.0       0.000       0.0       4898.917       0.000         6.100       0.000       0.0       0.000       0.0       4898.917       0.000         6.200       0.000       0.0       0.000       0.0       4898.917       0.000         6.300       0.000       0.0       0.000       0.0       4898.917       0.000         6.400       0.000       0.0       0.000       0.0       4898.917       0.000         6.500       0.000       0.0       0.000       0.0       4898.917       0.000         6.600       0.000       0.0       0.000       0.0       4898.917       0.000         6.700       0.000       0.0       0.000       0.0       4898.917       0.000         6.800       0.000       0.0       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000								
6.000       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0								
6.100       0.000       0.0       0.00       0.000       0.04898.917       0.000         6.200       0.000       0.0       0.000       0.000       0.04898.917       0.000         6.300       0.000       0.0       0.000       0.0       4898.917       0.000         6.400       0.000       0.0       0.000       0.0       4898.917       0.000         6.500       0.000       0.0       0.000       0.0       4898.917       0.000         6.600       0.000       0.0       0.000       0.0       4898.917       0.000         6.700       0.000       0.0       0.000       0.0       4898.917       0.000         6.800       0.000       0.0       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000								
6.200       0.000       0.0       0.000       0.000       4898.917       0.000         6.300       0.000       0.0       0.000       0.0       4898.917       0.000         6.400       0.000       0.0       0.000       0.0       4898.917       0.000         6.500       0.000       0.0       0.000       0.0       4898.917       0.000         6.600       0.000       0.0       0.000       0.0       4898.917       0.000         6.700       0.000       0.0       0.000       0.0       4898.917       0.000         6.800       0.000       0.0       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000								
6.400       0.000       0.0       0.000       0.000       4898.917       0.000         6.500       0.000       0.0       0.000       0.0       4898.917       0.000         6.600       0.000       0.0       0.000       0.0       4898.917       0.000         6.700       0.000       0.0       0.000       0.0       4898.917       0.000         6.800       0.000       0.0       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000				0.0				
6.500     0.000     0.0     0.000     0.000     4898.917     0.000       6.600     0.000     0.0     0.000     0.0     4898.917     0.000       6.700     0.000     0.0     0.000     0.0     4898.917     0.000       6.800     0.000     0.0     0.000     0.0     4898.917     0.000       6.900     0.000     0.0     0.000     0.0     4898.917     0.000								
6.600       0.000       0.0       0.00       0.000       0.0       4898.917       0.000         6.700       0.000       0.0       0.000       0.0       4898.917       0.000         6.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000								
6.700       0.000       0.0       0.000       0.000       0.04898.917       0.000         6.800       0.000       0.0       0.00       0.000       0.0       4898.917       0.000         6.900       0.000       0.0       0.000       0.0       4898.917       0.000								
6.900 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	6.700	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
7.100 0.000 0.0 0.0 0.000 0.0 4898.917 0.000								

7.400       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0	7.200 7.300	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
7.600         0.000         0.0         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0.000         0	7.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
7.800       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0	7.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
8.000       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0	7.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
8.200       0.000       0.0       0.00       0.000       0.004       4898.917       0.000         8.300       0.000       0.0       0.00       0.000       0.0       4898.917       0.000         8.400       0.000       0.0       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         8.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         8.600       0.000       0.0       0.000       0.0       0.0       0.0       4898.917       0.000         8.700       0.000       0.0       0.0       0.000       0.0       0.0       4898.917       0.000         8.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         8.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.100       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.200       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.300       0.000       0.0       0.0       0.000	8.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
8.400       0.000       0.0       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0.000       0	8.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
8.600       0.000       0.0       0.00       0.000       0.004       4898.917       0.000         8.700       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         8.800       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         8.900       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.000       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.100       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.200       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.300       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.400       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.700       0.000       0.0       0.0       0.000       0.0       4898.917       0	8.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
8.800       0.000       0.0       0.00       0.000       0.004       4898.917       0.000         8.900       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.000       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.100       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.200       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.300       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.400       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000	8.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
9.000       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.100       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.200       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.300       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.400       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.600       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.700       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         10.000       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         10.000       0.000       0.0       0.0       0.000       0.0       4898.917       0.000<	8.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
9.200       0.000       0.0       0.00       0.000       0.004       4898.917       0.000         9.300       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.400       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.500       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.600       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.700       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.800       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         10.000       0.000       0.0       0.000       0.0       0.0       4898.917       0.000	9.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
9.400       0.000       0.0       0.00       0.000       0.004898.917       0.000         9.500       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         9.600       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.700       0.000       0.0       0.000       0.0       0.000       0.0       4898.917       0.000         9.800       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         9.900       0.000       0.0       0.0       0.000       0.0       4898.917       0.000         10.000       0.000       0.0       0.0       0.000       0.0       4898.917       0.000	9.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
9.600     0.000     0.0     0.00     0.000     0.0     4898.917     0.000       9.700     0.000     0.0     0.000     0.000     0.0     4898.917     0.000       9.800     0.000     0.0     0.000     0.000     0.0     4898.917     0.000       9.900     0.000     0.0     0.0     0.000     0.0     4898.917     0.000       10.000     0.000     0.000     0.0     0.000     0.0     4898.917     0.000	9.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
9.800       0.000       0.0       0.00       0.000       0.004       4898.917       0.000         9.900       0.000       0.0       0.000       0.000       0.0       4898.917       0.000         10.000       0.000       0.0       0.000       0.0       4898.917       0.000	9.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.000 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	9.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.100 0.000 0.0 0.0 0.000 0.0 4696.917 0.000	10.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.200 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	10.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.400 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	10.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.600 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	10.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
10.800 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	10.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
11.000 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	11.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
11.200 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	11.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
11.400 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	11.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
11.600 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	11.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
11.800 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	11.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
12.000 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	12.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
12.200 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	12.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
12.400 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	12.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
12.600 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	12.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
12.800 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	12.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
13.000 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	13.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
13.200 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	13.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
13.400 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	13.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
13.600 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	13.600	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
13.800 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	13.800	0.000	0.0	0.0	0.000	0.0	4898.917	0.000 0.000 0.000
14.000 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	14.000	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
14.200 0.000 0.0 0.0 0.000 0.0 4898.917 0.000	14.200	0.000	0.0	0.0	0.000	0.0	4898.917	0.000
14.400 0.000 0.0 0.0 0.00 0.0 4898.917 0.000	14.400	0.000	0.0	0.0	0.000	0.0	4898.917	0.000

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of total stress due to combined axial stress and bending may not be representative of actual conditions.

# Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

Pile-head deflection	=	0.000 t	m
Computed slope at pile head	=	0.000	
Maximum bending moment	=	0.000	kN- m
Maximum shear force	=	0.000	kN
Depth of maximum bending moment	=	0.000	m
Depth of maximum shear force	=	0.000	m
Number of iterations	=	5	
Number of zero deflection points	=	0	

```
LPILE Plus for Windows, Version 4.0 (4.0.8)
                  Analysis of Individual Piles and Drilled Shafts
                 Subjected to Lateral Loading Using the p-y Method
                         (c) Copyright ENSOFT, Inc., 1985-2003
                                   All Rights Reserved
Path to file locations: L:\Programs\LPILE\Chapter 6\Ch. 6 Example with P=474.5\P=0 case\
Name of input data file: Up analysis(P=0)2.lpd
Name of output file: Up analysis(P=0)2.lpo
Name of plot output file: Up analysis(P=0)2.lpo
Name of plot output file: Up analysis(P=0)2.lpp
Name of runtime file: Up analysis(P=0)2.lpr
                              Time and Date of Analysis
                  Date: May 4, 2005 Time: 16:58:55
                           Problem Title
Up Analysis with P=0 case
                                     Program Options
Units Used in Computations - SI Units, meters, kilopascals
Basic Program Options:
Analysis Type 3:
- Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment
  Capacity with Pile Response Computed Using Nonlinear EI
Computation Options:
- User-specified p-y curves used in analysis
- Analysis uses p-y multiplers for group action

- Analysis assumes no shear resistance at pile tip

- Analysis for fixed-length pile or shaft only
- No computation of foundation stiffness matrix elements
- Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths
Solution Control Parameters:
- Number of pile increments
- Maximum number of iterations allowed = 2.5400E-07 m

Maximum allowable deflection = 2.5400E+00 m
- Maximum number of iterations allowed =
                                                             100
Printing Options:

    Values of pile-head deflection, bending moment, shear force, and soil reaction are printed for full length of pile.
    Printing Increment (spacing of output points) = 1

_____
                                           _____
                     Pile Structural Properties and Geometry
______
                                                          10.00 m
Pile Length
                                                          .00 m
.00 deg.
Depth of ground surface below top of pile =
Slope angle of ground surface
Structural properties of pile defined using 2 points
                    Pile Moment of Pile Modulus of Diameter Inertia Area Elasticity m m**4 Sq. m kN/Sq. m
```

1	0.0000	.17780000	1.0000	.024800	200000000.000
2	10.0000	.17780000	1.0000	.024800	200000000.000

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of moment of inertia and modulus of are not used for any computations other than total stress due to combined axial loading and bending.

Soil and Rock Layering Information

The soil profile is modelled using 4 layers

Layer 1 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = .000 m 5.290 m Layer 2 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = 5.290 m 5.310 m Layer 3 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = 5.310 m 8.000 m Layer 4 is modelled using user-specied p-y curves Distance from top of pile to top of layer = 8.000 mDistance from top of pile to bottom of layer = 10.000 m

(Depth of lowest layer extends .00 m below pile tip)

______ Effective Unit Weight of Soil vs. Depth

Distribution of effective unit weight of soil with depth is defined using 8 points

Point No.	Depth X m	Eff. Unit Weight kN/ m**3
1	.00	11.40000
2	5.29	11.40000
3	5.29	11.40000
4	5.31	21.20000
5	5.31	21.20000
6	8.00	21.20000
7	8.00	21.20000
8	10.00	21.20000

______ Shear Strength of Soils

Distribution of shear strength parameters with depth defined using 0 points

No.	m	kN/ m**2	Deg.	k_rm	%
Point	Depth X	Cohesion c	Angle of Friction	E50 or	RQD

# Notes:

- Cohesion = uniaxial compressive strength for rock materials.
- (2) Values of E50 are reported for clay strata.
- (3) Default values will be generated for E50 when input (4) RQD and k_rm are reported only for weak rock strata. Default values will be generated for E50 when input values are 0.

p-y Modification Factors

Distribution of p-y multipliers with depth defined using 5 points

Point No.	Depth X m	p-mult	y-mult
1	.000	1.0000	1.0000
2	5.290	1.0000	1.0000
3	5.310	1.0000	1.0000
4	8.000	1.0000	1.0000
5	10.000	1.0000	1.0000

User-specified p-y Curves

User-specified p-y curves defined using 8 curves.

User-specified curve number  $\,$  1 at depth =  $\,$  .000 m

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.248

User-specified curve number 2 at depth = 5.290 m

Point No.	y m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.248

User-specified curve number  $\mbox{3}$  at depth =  $\mbox{5.290 m}$ 

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.298

User-specified curve number 4 at depth = 5.310 m

Point	Y	p,
No.	m	kN/ m

```
      1
      .0000
      .000

      2
      .0002
      65.766

      3
      .0005
      78.209

      4
      .0011
      98.343

      5
      .0023
      116.950

      6
      .0034
      129.427

      7
      .0046
      139.078

      8
      .0115
      174.882

      9
      .0229
      207.971

      10
      .0458
      247.320

      11
      .0515
      247.320

      12
      .0573
      247.320
```

User-specified curve number 5 at depth = 5.310 m

Point No.	Y m	p, kN/ m
1	.0000	.000
2	.0002	65.766
3	.0005	78.209
4	.0011	98.343
5	.0023	116.950
6	.0034	129.427
7	.0046	139.078
8	.0115	174.882
9	.0229	207.971
10	.0458	247.320
11	.0515	247.320
12	.0573	247.320

User-specified curve number 6 at depth = 8.000 m

Point No.	y m	p, kN/ m
1	.0000	.000
2	.0002	56.414
3	.0005	67.088
4	.0011	84.358
5	.0023	100.319
6	.0034	111.022
7	.0046	119.300
8	.0115	150.012
9	.0229	178.396
10	.0458	212.150
11	.0515	212.150
12	.0573	212.150

User-specified curve number 7 at depth = 8.000 m

Y m	p, kN/ m
.0000	.000
.0002	56.414
.0005	67.088
.0011	84.358
.0023	100.319
.0034	111.022
.0046	119.300
.0115	150.012
.0229	178.396
.0458	212.150
.0515	212.150
.0573	212.150
	.0000 .0002 .0005 .0011 .0023 .0034 .0046 .0115 .0229 .0458

User-specified curve number 8 at depth = 10.000 m

Point No.	y m	p, kN/ m
1	.0000	.000
2	.0005	26.070
3	.0011	32.781
4	.0020	21.922
5	.0023	38.983
6	.0034	43.142
7	.0046	46.359
8	.0115	58.294
9	.0151	82.440

10	.0229	69.324
11	.0458	82.440
12	.0573	82.440

Loading Type

Static loading criteria was used for computation of p-y curves

Pile-head Loading and Pile-head Fixity Conditions

Number of loads specified = 1

Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1)

Shear force at pile head = 365.000 kN

Bending moment at pile head = -83.500 m- kN

Axial load at pile head = .000 kN .000 kN Axial load at pile head =

Non-zero moment at pile head for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment) condition.

Output of p-y Curves at Specified Depths

p-y curves are generated and printed for verification at 5 depths.

Depth No.	Depth Below Pile Head m	Depth Below Ground Surface m
1	.000	.000
2	5.290	5.290
3	5.310	5.310
4	8.000	8.000
5	10.000	10.000

Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness

# Pile Description:

The sectional shape is a circular shaft with steel casing.

.1778 m Outside Diameter .0115 m**2 Wall thickness of steel shell = .0115 m Cross-sectional area of shell = .00601 m**2 Moment of inertia of steel shell = 2.08692E-05 m**4

# Material Properties:

Compressive Strength of Concrete = 27600.000 kN/ m**2 Yield Stress of Reinforcement = 0. kN/ m**2 Steel shell or core yield stress = 552000. kN/ m**2 Modulus of Elasticity of Reinforcement = 200000000. kN/ m**2 .000 m Cover Thickness (edge to bar center) = Number of Reinforcing Bars = 10 Area of Single Bar = .00000 m**2 Number of Rows of Reinforcing Bars = 5 Ultimate Axial Squash Load Capacity = 3758.02 kN

Row Number	Area of Reinforcement m**2	Distance to Centroidal Axis m
1	.000000	.0736
2	.000000	.0455
3	.000000	.0000
4	.000000	0455
5	.000000	0736

Axial Thrust Force = .00 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
1.73583660	4898.917	.00035433	.00002742	.08889729
2.50651820	4897.351	.00053433	.00003961	.08889729
3.27670667	4895.785	.00066929	.00005301	.08889729
4.04640201	4894.220	.00082677	.00006399	.08889729
4.81560422	4892.654	.00098425	.00007618	.08889729
5.58431330	4891.088	.00114173	.00008837	.08889729
6.35252925	4889.522	.00129921	.00010056	.08889729
6.55060560	4496.902	.00145669	.00010411	.08297207
7.25778201	4496.284	.00161417	.00011537	.08297207
7.96476385	4495.667	.00177165	.00012662	.08297207
8.67155112	4495.049	.00192913	.00013788	.08297207
9.37814382	4494.431	.00208661	.00014913	.08297207
10.085	4493.813	.00224409	.00016039	.08297207
10.791	4493.196	.00240157	.00017165	.08297207
11.497	4492.578	.00255906	.00018290	.08297207
12.203	4491.960	.00271654	.00019416	.08297207
12.908 13.614	4491.342 4490.725	.00287402 .00303150	.00020541 .00021667	.08297207 .08297207
14.319	4490.107	.00303130	.00021007	.08297207
15.024	4489.489	.00316696	.00022732	.08297207
15.729	4488.871	.00350394	.00025043	.08297207
16.433	4488.254	.00366142	.00026169	.08297207
17.138	4487.636	.00381890	.00027294	.08297207
17.842	4487.018	.00397638	.00028420	.08297207
23.118	4482.385	.00515748	.00036862	.08297207
28.383	4477.752	.00633858	.00045303	.08297207
33.636	4473.118	.00751969	.00053745	.08297207
38.879	4468.485	.00870079	.00062186	.08297207
44.111	4463.852	.00988189	.00070628	.08297207
49.332	4459.219	.01106299	.00079069	.08297207
54.542	4454.586	.01224409	.00087511	.08297207
57.662	4295.045	.01342520	.00095982	.08299377
62.752 67.845	4296.211 4297.412	.01460630 .01578740	.00104577 .00113196	.08309687 .08319996
72.947	4298.973	.01696850	.00113196	.08330848
78.054	4300.601	.01814961	.00130527	.08341700
83.173	4302.638	.01933071	.00139241	.08353095
88.306	4305.127	.02051181	.00147993	.08365032
93.456	4308.127	.02169291	.00156786	.08377512
98.635	4312.080	.02287402	.00165633	.08391077
103.850	4317.171	.02405512	.00174537	.08405727
109.135	4324.538	.02523622	.00183532	.08422548
116.274	4401.446	.02641732	.00194228	.08502310
121.355	4397.159	.02759843	.00203107	.08509364
126.423	4392.803	.02877953	.00212002	.08516418
131.480	4388.413	.02996063	.00220914	.08523472
136.408 141.002	4380.233	.03114173 .03232283	.00229741	.08527270 .08522929
145.110	4362.312 4331.145	.03232263	.00236314	.08509907
145.110	4183.660	.03468504	.00250950	.08385108
147.008	4098.795	.03586614	.00257802	.08337902
153.523	4143.973	.03704724	.00264784	.08297207
155.871	4077.375	.03822835	.00273226	.08297207
157.833	4004.950	.03940945	.00281667	.08297207
159.521	3929.994	.04059055	.00290109	.08297207
161.057	3855.647	.04177165	.00298551	.08297207
162.411	3781.163	.04295276	.00306992	.08297207
163.614	3707.213	.04413386	.00315434	.08297207
164.745	3635.565	.04531496	.00323875	.08297207
165.711 166.656	3563.988 3495.506	.04649606 .04767717	.00332317	.08297207
100.036	3473.306	.04/0//1/	.00340759	.08297207

```
      167.455
      3427.355
      .04885827
      .00349200
      .08297207

      168.240
      3362.162
      .05003937
      .00357642
      .08297207

      168.926
      3298.012
      .05122047
      .00366083
      .08297207

      169.575
      3236.065
      .05240157
      .00374525
      .08297207

      170.188
      3176.179
      .05358268
      .00382966
      .08297207
```

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 161.289 m- kN

p-y Curve Computed by Interpolation from User-input Curves

Soil Layer Number	=	1	
Depth below ground surface	=	.000	m
Depth below pile head	=	.000	m
p-multiplier	=	1.00000	
v-multiplier	=	1.00000	

y, m	p, kN/m
.0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356 .0667	.000 140.575 143.795 171.931 189.761 201.500 211.627 221.754 231.882 242.009 248.913 254.570 260.227 265.884 343.117 346.248

# p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 2
Depth below ground surface = 5.290 m
Depth below pile head = 5.290 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

у, т	p, kN/m
.0000	.000
.0010	140.575
.0011	143.795
.0022	171.931
.0033	189.761
.0044	201.500
.0056	211.627
.0067	221.754
.0078	231.882
.0089	242.009
.0100	248.913
.0111	254.570
.0122	260.227
.0133	265.884
.0356	343.117
.0667	346.248
.0889	346.248

p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 3
Depth below ground surface = 5.310 m
Depth below pile head = 5.310 m
p-multiplier = 1.00000
```

```
y-multiplier = 1.00000
```

У,	m	p, kN/	m
.00 .00 .00 .00 .00 .00 .00 .00 .00 .00	m 000 010 011 022 033 044 056 067 078 089 100 111 122 133 5667	94 98 115 128 137 144 149 155 161 167 172 176 180 229	m
	889		.320

p-y Curve Computed by Interpolation from User-input Curves

Soil Layer Number	=	4	
Depth below ground surface	=	8.000	m
Depth below pile head	=	8.000	m
p-multiplier	=	1.00000	
y-multiplier	=	1.00000	

y, m	p, kN/m
.0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356	
.0889	212.150

p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 4
Depth below ground surface = 10.000 m
Depth below pile head = 10.000 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

y, m	p, kN/m
y, m .0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089	p, kN/ m
.0122 .0133 .0356 .0667	63.148 70.602 76.575 82.440

.0889 82.440

Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1) Specified shear force at pile head = 365.000 kN Specified bending moment at pile head = -83.500 m- kN Specified axial load at pile head = .000 kN

Non-zero moment for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment )condition.

Depth X	Deflect. Y	Moment M	Shear V	Slope S	Total Stress	Flx. Rig. EI	Soil Res
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
0.000	.047472	-83.5000	365.0	035587	7.4232	4295.386	-346.250
.06897	.044972	-59.1510	341.1	036732	5.2585	4295.386	-346.250
.138	.042406	-36.4489	317.2	037500	3.2403	4295.386	-346.250
.207	.039799	-15.3936	293.4	037911	1.3685	4489.165	-346.250
.276	.037177	4.0149	269.5	038001	.3569	4894.284	-346.250
.345	.034558	21.7765	245.8	037805	1.9359	4483.564	-340.101
.414	.031962	37.9205	222.6	037345	3.3711	4469.333	-332.288
.483	.029407	52.4840	200.0	036646	4.6658	4456.417	-324.595
.552	.026907	65.5037	177.9	035714	5.8233	4296.860	-317.072
.621 .690	.024481	77.0154 87.0537	156.2 135.1	034571 033256	6.8467 7.7391	4300.270 4304.520	-309.766 -302.717
.759	.019894	95.6522	114.5	031793	8.5035	4309.804	-295.958
.828	.017754	102.8	94.3234	030206	9.1427	4316.189	-288.380
.897	.015727	108.7	74.7909	028518	9.6601	4323.880	-278.063
.966	.013820	113.2	55.9489	026758	10.0598	4368.125	-268.355
1.034	.012036	116.4	37.7548	024953	10.3461	4401.357	-259.275
1.103	.010378	118.4	20.1648	023114	10.5228	4399.681	-250.834
1.172	.008848	119.2	3.1833	021252	10.5934	4399.011	-241.630
1.241	.007447	118.8	-13.0405	019387	10.5618	4399.311	-228.860
1.310	.006174	117.4	-28.4240	017536	10.4335	4400.529	-217.261
1.379	.005028	114.9	-43.0474	015713	10.2133	4386.630	-206.818
1.448	.004007	111.4	-56.9897	013927	9.9056	4349.413	-197.509
1.517	.003107	107.0	-70.2385	012189	9.5145	4321.598	-186.705
1.586	.002326	101.7	-82.6744	010522	9.0444	4315.109	-173.935
1.655	.001656	95.6211	-94.1745	008944	8.5007	4309.780	-159.567
1.724	.001092	88.7468	-104.6	007468	7.8896	4305.384	-143.240
1.793	6.26E-04	81.1913	-113.8	006107	7.2179 6.4945	4301.850	-122.234
1.862	2.50E-04 -4.58E-05	73.0544 64.4589	-121.3 -123.9	004870 003767	5.7304	4299.007 4296.613	-96.405 21.074
2.000	-2.70E-04	55.9637	-119.8	002809	4.9752	4384.308	98.154
2.069	-4.33E-04	47.9353	-112.6	001998	4.2614	4460.460	111.365
2.138	-5.46E-04	40.4366	-104.7	001316	3.5948	4467.107	117.695
2.207	-6.15E-04	33.4977	-96.4211	-7.45E-04	2.9779	4473.241	121.597
2.276	-6.48E-04	27.1372	-87.9698	-2.78E-04	2.4125	4478.849	123.492
2.345	-6.53E-04	21.3640	-79.4438	9.50E-05	1.8993	4483.926	123.761
2.414	-6.35E-04	16.1794	-70.9433	3.84E-04	1.4383	4488.476	122.753
	-6.00E-04	11.5787	-62.5457	5.97E-04	1.0293	4492.506	120.779
	-5.53E-04	7.5524	-54.3080	7.44E-04	.6714	4496.027	118.113
2.621	-4.98E-04	4.0879	-46.2697	8.30E-04	.3634	4894.135	114.997
	-4.38E-04	1.1704	-38.4540	8.67E-04	.1040	4898.917	111.657
2.759 2.828	-3.78E-04	-1.2161 -3.0909	-30.8942	8.67E-04	.1081	4898.917 4896.163	107.577 102.421
	-3.19E-04 -2.63E-04	-4.4786	-23.6529 -16.7582	8.37E-04 7.83E-04	.2748	4893.340	97.525
	-2.11E-04	-5.4024	-10.1880	7.14E-04	.4803	4891.459	93.009
	-1.64E-04	-5.8838	-4.3749	6.34E-04	.5231	4890.478	75.572
	-1.23E-04	-6.0058	.1882	5.50E-04	.5339	4890.229	56.756
3.172	-8.83E-05	-5.8579	3.5463	4.67E-04	.5208	4890.531	40.629
3.241	-5.89E-05	-5.5167	5.8826	3.86E-04	.4904	4891.226	27.125
3.310	-3.50E-05	-5.0465	7.3728	3.12E-04	.4486	4892.184	16.090
3.379	-1.59E-05	-4.4997	8.1798	2.45E-04	.4000	4893.297	7.314
3.448	-1.20E-06	-3.9182	8.4510	1.85E-04	.3483	4894.480	.551315
3.517	9.68E-06	-3.3341	8.3163	1.34E-04	.2964	4895.669	-4.458
3.586	1.73E-05	-2.7711	7.8875	9.13E-05	.2464	4896.813	-7.977
3.655	2.23E-05	-2.2461	7.2587	5.60E-05	.1997	4897.880	-10.257
3.724 3.793	2.51E-05 2.61E-05	-1.7699 -1.3486	6.5074 5.6954	2.77E-05	.1573	4898.847 4898.917	-11.532 -12.016
3.793	2.51E-05 2.58E-05	-1.3486	4.8707	5.76E-06 -1.07E-05	.1199 8.75E-02	4898.917	-12.016
3.931	2.46E-05	6767		-2.23E-05	6.02E-02	4898.917	-11.340
4.000	2.28E-05	4231		-3.01E-05	3.76E-02	4898.917	-10.479

4.069 2.05E-05	2192	2.6306	-3.46E-05	1.95E-02	4898.917	-9.429
4.138 1.80E-05	-6.02E-02	2.0199	-3.66E-05	5.35E-03	4898.917	-8.281
4.207 1.54E-05	5.94E-02		-3.66E-05	5.28E-03	4898.917	-7.106
4.276 1.29E-05	.1452		-3.51E-05	1.29E-02	4898.917	-5.958
4.345 1.06E-05	.2027	.6652	-3.27E-05	1.80E-02	4898.917	-4.875
4.414 8.43E-06	.2370	. 3633	-2.96E-05	2.11E-02	4898.917	-3.882
4.483 6.51E-06	.2528		-2.62E-05	2.25E-02	4898.917	-2.995
4.552 4.83E-06	.2544	-5.37E-02	-2.26E-05	2.26E-02	4898.917	-2.221
4.621 3.39E-06	.2454	1842	-1.91E-05	2.18E-02	4898.917	-1.561
4.690 2.20E-06	.2290		-1.57E-05	2.04E-02	4898.917	-1.011
4.759 1.22E-06	.2077		-1.27E-05	1.85E-02	4898.917	562507
4.828 4.50E-07	.1838	3536	-9.90E-06	1.63E-02	4898.917	207195
4.897 -1.43E-07	.1590	3585	-7.48E-06	1.41E-02	4898.917	.065948
4.966 -5.82E-07	.1344		-5.42E-06		4898.917	.268043
				1.19E-02		
5.034 -8.91E-07	.1111	3236	-3.69E-06	9.88E-03	4898.917	.410071
5.103 -1.09E-06	8.98E-02	2922	-2.28E-06	7.98E-03	4898.917	.502444
5.172 -1.20E-06	7.08E-02	2557		6.29E-03	4898.917	.554701
5.241 -1.25E-06	5.45E-02		-2.66E-07	4.84E-03	4898.917	.575313
5.310 -1.24E-06	4.09E-02	1828	4.06E-07	3.64E-03	4898.917	.408260
5.379 -1.19E-06	2.93E-02	1553	9.00E-07	2.60E-03	4898.917	.391097
5.448 -1.12E-06	1.95E-02	1292	1.24E-06	1.73E-03	4898.917	.364773
5.517 -1.02E-06	1.15E-02	1051	1.46E-06	1.02E-03	4898.917	.332477
5.586 -9.16E-07	4.99E-03	-8.34E-02	1.58E-06	4.44E-04	4898.917	.296806
5.655 -8.05E-07	-5 84F-05	-6 43E-02	1.61E-06	5.19E-06	4898.917	.259826
			1.58E-06			
5.724 -6.94E-07				3.44E-04	4898.917	.223131
5.793 -5.86E-07	-6.62E-03	-3.34E-02	1.51E-06	5.89E-04	4898.917	.187906
5.862 -4.86E-07	-8.48E-03	-2.16E-02	1.40E-06	7.54E-04	4898.917	.154992
5.931 -3.93E-07			1.28E-06	8.54E-04	4898.917	.124939
6.000 -3.10E-07	-1.01E-02	-4.26E-03	1.14E-06	9.00E-04	4898.917	.098061
6.069 -2.36E-07	-1.02E-02	1.69E-03	9.94E-07	9.06E-04	4898.917	.074488
6.138 -1.72E-07	-9 90E-03	6.13E-03	8.53E-07	8.80E-04	4898.917	.054201
						.037077
6.207 -1.18E-07		9.28E-03	7.17E-07	8.31E-04	4898.917	
6.276 -7.34E-08	-8.62E-03	1.13E-02	5.91E-07	7.66E-04	4898.917	.022912
6.345 -3.69E-08	-7.78E-03	1.25E-02	4.76E-07	6.92E-04	4898.917	.011456
6.414 -7.83E-09		1.30E-02	3.72E-07	6.12E-04	4898.917	.002426
	-5.98E-03	1.29E-02	2.82E-07	5.32E-04	4898.917	004472
6.552 3.10E-08	-5.10E-03	1.25E-02	2.04E-07	4.54E-04	4898.917	009532
6.621 4.26E-08	-4.27E-03	1.17E-02	1.38E-07	3.79E-04	4898.917	013035
	-3.49E-03	1.07E-02	8.31E-08	3.10E-04	4898.917	015249
6.759 5.41E-08	-2.79E-03	9.61E-03	3.89E-08	2.48E-04	4898.917	016415
6.828 5.54E-08	-2.17E-03	8.47E-03	4.04E-09	1.93E-04	4898.917	016752
	-1.62E-03	7.32E-03	-2.26E-08	1.44E-04	4898.917	016453
	-1.16E-03	6.22E-03	-4.22E-08	1.03E-04	4898.917	015683
7.034 4.88E-08	-7.64E-04	5.17E-03	-5.57E-08	6.79E-05	4898.917	014584
7.103 4.46E-08	-4.42E-04	4.21E-03	-6.42E-08	3.93E-05	4898.917	013272
	-1.83E-04		-6.86E-08	1.63E-05	4898.917	011843
7.241 3.51E-08	1.92E-05	2.58E-03	-6.97E-08	1.70E-06	4898.917	010372
7.310 3.03E-08	1.72E-04	1.91E-03	-6.84E-08	1.53E-05	4898.917	008918
7.379 2.57E-08	2.83E-04	1.35E-03	-6.52E-08	2.52E-05	4898.917	007525
7.448 2.13E-08	3.58E-04		-6.07E-08	3.18E-05	4898.917	006224
7.517 1.73E-08	4.04E-04		-5.53E-08	3.59E-05	4898.917	005033
7.586 1.37E-08	4.25E-04	1.74E-04	-4.95E-08	3.78E-05	4898.917	003966
7.655 1.05E-08	4.28E-04	-6.68E-05	-4.35E-08	3.80E-05	4898.917	003026
7.724 7.71E-09		-2.47E-04		3.70E-05	4898.917	002213
7.793 5.33E-09		-3.76E-04		3.50E-05	4898.917	001522
7.862 3.32E-09	3.64E-04	-4.61E-04	-2.65E-08	3.24E-05	4898.917	-9.45E-04
7.931 1.67E-09	3.30E-04	-5.10E-04	-2.16E-08	2.93E-05	4898.917	-4.74E-04
8.000 3.41E-10		-5.30E-04		2.61E-05		-9.62E-05
8.069 -7.05E-10		-5.27E-04		2.28E-05	4898.917	1.93E-04
8.138 -1.50E-09		-5.06E-04		1.96E-05	4898.917	4.00E-04
8.207 -2.08E-09	1.87E-04	-4.74E-04	-7.13E-09	1.66E-05	4898.917	5.38E-04
8.276 -2.49E-09		-4.34E-04		1.38E-05	4898.917	6.22E-04
				1.13E-05		
8.345 -2.74E-09		-3.89E-04			4898.917	6.63E-04
8.414 -2.86E-09		-3.43E-04		9.05E-06	4898.917	6.71E-04
8.483 -2.89E-09	7.97E-05	-2.98E-04	1.59E-10	7.09E-06	4898.917	6.55E-04
8.552 -2.84E-09		-2.54E-04	1.15E-09	5.40E-06	4898.917	6.21E-04
8.621 -2.73E-09		-2.12E-04	1.89E-09	3.98E-06	4898.917	5.76E-04
8.690 -2.58E-09	3.15E-05	-1.75E-04	2.43E-09	2.80E-06	4898.917	5.23E-04
8.759 -2.40E-09	2.07E-05	-1.40E-04	2.79E-09	1.84E-06	4898.917	4.67E-04
8.828 -2.19E-09		-1.10E-04	3.02E-09	1.08E-06	4898.917	4.10E-04
8.897 -1.98E-09						3.54E-04
		-8.38E-05	3.15E-09	4.86E-07	4898.917	
8.966 -1.76E-09		-6.12E-05	3.19E-09	4.74E-08	4898.917	3.01E-04
9.034 -1.54E-09	-2.97E-06	-4.22E-05	3.17E-09	2.64E-07	4898.917	2.51E-04
9.103 -1.32E-09			3.12E-09	4.70E-07	4898.917	2.05E-04
9.172 -1.11E-09			3.03E-09	5.88E-07	4898.917	1.63E-04
9.241 -9.04E-10			2.93E-09	6.38E-07	4898.917	1.26E-04
9.310 -7.05E-10	-7.13E-06	3.80E-06	2.83E-09	6.34E-07	4898.917	9.27E-05
9.379 -5.13E-10		9.18E-06	2.74E-09	5.91E-07	4898.917	6.34E-05
9.448 -3.28E-10		1.27E-05	2.65E-09	5.22E-07	4898.917	3.79E-05
9.517 -1.48E-10		1.45E-05	2.57E-09	4.36E-07	4898.917	1.59E-05
9.586 2.72E-11	-3.86E-06	1.50E-05	2.51E-09	3.43E-07	4898.917	-2.72E-06

```
      9.655
      1.99E-10
      -2.84E-06
      1.43E-05
      2.46E-09
      2.52E-07
      4898.917
      -1.82E-05

      9.724
      3.67E-10
      -1.90E-06
      1.26E-05
      2.43E-09
      1.69E-07
      4898.917
      -3.08E-05

      9.793
      5.34E-10
      -1.10E-06
      1.01E-05
      2.41E-09
      9.81E-08
      4898.917
      -4.05E-05

      9.862
      6.99E-10
      -5.02E-07
      7.07E-06
      2.40E-09
      4.47E-08
      4898.917
      -4.76E-05

      9.931
      8.65E-10
      -1.28E-07
      3.64E-06
      2.39E-09
      1.13E-08
      4898.917
      -5.19E-05

      10.000
      1.03E-09
      0.0
      0.0
      2.39E-09
      0.0
      4898.917
      -5.37E-05
```

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of total stress due to combined axial stress and bending may not be representative of actual conditions.

# Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

```
Pile-head deflection = .04747209 m
Computed slope at pile head = -.03558708

Maximum bending moment = 119.161 kN- m
Maximum shear force = 365.000 kN

Depth of maximum bending moment = 1.17241379 m
Depth of maximum shear force = 0.000 m

Number of iterations = 37

Number of zero deflection points = 6
```

# Summary of Pile-head Response

Definition of symbols for pile-head boundary conditions:

```
y = pile-head displacment, m
M = pile-head moment, kN- m
V = pile-head shear force, kN
S = pile-head slope radians
```

S = pile-head slope, radians R = rotational stiffness of pile-head, m- kN/rad

BC	Boundary	Boundary	Axial	Pile Head	Maximum	Maximum
Type	Condition	Condition	Load	Deflection	Moment	Shear
	1	2	kN	m	m- kN	kN
1	V = 365.000	M = -83.500	0.0000	.047472	119.1608	365.0000

```
LPILE Plus for Windows, Version 4.0 (4.0.8)
                 Analysis of Individual Piles and Drilled Shafts
                Subjected to Lateral Loading Using the p-y Method
                        (c) Copyright ENSOFT, Inc., 1985-2003
                                 All Rights Reserved
Path to file locations: L:\Programs\LPILE\Chapter 6\Ch. 6 Example with P=474.5\P=0 case\
Name of input data file: Down analysis(P=0)2.1pd
Name of output file: Down analysis(P=0)2.1po
Name of plot output file: Down analysis(P=0)2.1pp
Name of runtime file: Down analysis(P=0)2.1pr
Time and Date of Analysis
                 Date: May 4, 2005 Time: 16:57:32
______
                          Problem Title
Down Analysis with P=0 Case
______
                                     Program Options
Units Used in Computations - SI Units, meters, kilopascals
Basic Program Options:
Analysis Type 3:
 · Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment
  Capacity with Pile Response Computed Using Nonlinear EI
Computation Options:
- User-specified p-y curves used in analysis
- Analysis uses p-y multiplers for group action
- Analysis assumes no shear resistance at pile tip
- Analysis for fixed-length pile or shaft only
- No computation of foundation stiffness matrix elements
- Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths
Solution Control Parameters:
- Number of pile increments
- Number of pile increments = 145
- Maximum number of iterations allowed = 100
- Deflection tolerance for convergence = 2.5400E-07 m

- Maximum allowable deflection = 2.5400E+00 m
Printing Options:
- Values of pile-head deflection, bending moment, shear force, and soil reaction are printed for full length of pile.
- Printing Increment (spacing of output points) =
                    Pile Structural Properties and Geometry
Pile Length
                                                          4.50 m
                                                         .00 m
.00 deg.
Depth of ground surface below top of pile =
Slope angle of ground surface
Structural properties of pile defined using 2 points
                  Pile Moment of Pile Modulus of
Diameter Inertia Area Elasticity
          Depth
Point
```

	m	m	m**4	Sq. m	kN/Sq. m	
1	0.0000	.17780000	1.0000	.024800	200000000.000	
2	4.5000	.17780000	1.0000	.024800	200000000.000	

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of moment of inertia and modulus of are not used for any computations other than total stress due to combined axial loading and bending.

Soil and Rock Layering Information ______

The soil profile is modelled using 1 layers

Layer 1 is modelled using user-specied p-y curves Distance from top of pile to top of layer = 0.000 m Distance from top of pile to bottom of layer = 0.000 m

(Depth of lowest layer extends 1.50 m below pile tip)

Effective Unit Weight of Soil vs. Depth

Distribution of effective unit weight of soil with depth is defined using 2 points

 Point
 Depth X m
 Eff. Unit Weight kN/ m**3

 ---- 1
 .00
 12.20000

 2
 6.00
 12.20000

Shear Strength of Soils

Distribution of shear strength parameters with depth defined using 0 points

Point Depth X Cohesion c Angle of Friction E50 or RQD No. m kN/ m**2 Deg. k_rm % -----

#### Notes:

- (1) Cohesion = uniaxial compressive strength for rock materials.
  (2) Values of E50 are reported for clay strata.
  (3) Default values will be generated for E50 when input values are 0.
  (4) RQD and k_rm are reported only for weak rock strata.

p-y Modification Factors

Distribution of p-y multipliers with depth defined using 2 points

No.	Depth X m	p-mult	y-mult
1	.000	1.0000	1.0000
2	6.000	1.0000	1.0000

User-specified p-y Curves

User-specified p-y curves defined using 2 curves.

User-specified curve number 1 at depth = .000 m

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0001	263.064
3	.0002	312.838
4	.0006	393.373
5	.0011	467.802
6	.0017	517.708
7	.0023	556.313
8	.0057	699.527
9	.0115	831.882
10	.0229	989.280
11	.0258	989.280
12	.0286	989.280

User-specified curve number 2 at depth = 6.000 m

Point No.	Y m	p, kN/ m
1	.0000	.000
2	.0001	263.064
3	.0002	312.838
4	.0006	393.373
5	.0011	467.802
6	.0017	517.708
7	.0023	556.313
8	.0057	699.527
9	.0115	831.882
10	.0229	989.280
11	.0258	989.280
12	.0286	989.280

Loading Type

Static loading criteria was used for computation of p-y curves

Pile-head Loading and Pile-head Fixity Conditions

Number of loads specified = 1

Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1)
Shear force at pile head - 365 000 kN

Shear force at pile head = 365.000 kN

Bending moment at pile head = 83.550 m-kN

Axial load at pile head = .000 kN

Non-zero moment at pile head for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment) condition.

Output of p-y Curves at Specified Depths

p-y curves are generated and printed for verification at 2 depths.

Depth Depth Below Pile Head Depth Below Ground Surface No. m m

Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness

## Pile Description:

The sectional shape is a circular shaft with steel casing.

Outside Diameter	=	.1778	m
Wall thickness of steel shell	=	.0115	m
Cross-sectional area of shell	=	.00601	m**2
Moment of inertia of steel shell	=	2.08692E-05	m**4

## Material Properties:

Compressive Strength of Concrete	=	27600.000	kN/ m**2
Yield Stress of Reinforcement	=	0.	kN/ m**2
Steel shell or core yield stress	=	552000.	kN/ m**2
Modulus of Elasticity of Reinforcement		200000000.	kN/ m**2
Cover Thickness (edge to bar center)	=	.000	m
Number of Reinforcing Bars	=	10	
Area of Single Bar	=	.00000	m**2
Number of Rows of Reinforcing Bars	=	5	
Ultimate Axial Squash Load Capacity	=	3758.02	kN

Distribution and Area of Steel Reinforcement

Row Number	Area of Reinforcement m**2	Distance to Centroidal Axis m
1	.000000	.0736
2	.000000	.0455
3	.000000	.0000
4	.000000	0455
5	.000000	0736

Axial Thrust Force = .00 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
Moment kN-m  1.73583660 2.50651820 3.27670667 4.04640201 4.81560422 5.58431330 6.35252925 6.55060560 7.25778201 7.96476385 8.67155112 9.37814382 10.085 10.791 11.497 12.203 12.908 13.614 14.319 15.024 15.729 16.433 17.138	Stiffness kN-m2 	rad/m	m/m	m
17.842 23.118 28.383 33.636 38.879 44.111 49.332	4487.018 4482.385 4477.752 4473.118 4468.485 4463.852 4459.219	.00397638 .00515748 .00633858 .00751969 .00870079 .00988189	.00028420 .00036862 .00045303 .00053745 .00062186 .00070628	.08297207 .08297207 .08297207 .08297207 .08297207 .08297207

```
.01224409
          4454.586
4295.045
                                      .00087511
                                                     .08297207
 54.542
 57.662
                         .01342520
                                       .00095982
                                                      .08299377
                                      .00104577
           4296.211
                         .01460630
                                                     .08309687
 62.752
 67.845
            4297.412
                         .01578740
                                       .00113196
                                                      .08319996
                         .01696850
 72.947
           4298.973
                                       .00121848
                                                     .08330848
            4300.601
                         .01814961
                                       .00130527
 78.054
                                                      .08341700
 83.173
                                       .00139241
                                                     .08353095
                         .01933071
            4302.638
            4305.127
                         .02051181
                                       .00147993
 88.306
                                                      .08365032
           4308.127
                         .02169291
93.456
                                       .00156786
                                                     .08377512
           4312.080
4317.171
 98.635
                         .02287402
                                       .00165633
                                                      .08391077
                                       .00174537
103.850
                         .02405512
                                                     .08405727
           4324.538
                         .02523622
109.135
                                       .00183532
                                                      .08422548
116.274
                         .02641732
                                       .00194228
                                                      .08502310
121.355
            4397.159
                         .02759843
                                        .00203107
                                                      .08509364
                         .02877953
                                       .00212002
126.423
            4392.803
                                                      .08516418
           4388.413
4380.233
                         .02996063
                                       .00220914
131.480
                                                      .08523472
                         .03114173
                                       .00229741
                                                      .08527270
136.408
                         .03232283
                                       .00238314
                                                      .08522929
141.002
            4362.312
                         .03350394
                                       .00246586
                                                      .08509907
145.110
            4331.145
                         .03468504
                                       .00250950
                                                      .08385108
145.110
            4183.660
147.008
           4098.795
                         .03586614
                                       .00257802
                                                      .08337902
                         .03704724
                                       .00264784
           4143.973
4077.375
                                                      .08297207
153.523
                                       .00273226
                                                      .08297207
155.871
           4004.950
3929.994
                         .03940945
                                       .00281667
                                                      .08297207
157.833
                                                      .08297207
159.521
                         .04059055
                                       .00290109
            3855.647
                         .04177165
                                                     .08297207
                                       .00298551
161.057
162.411
            3781.163
                         .04295276
                                       .00306992
                                                      .08297207
                         .04413386
           3707.213
3635.565
                                       .00315434
                                                     .08297207
163.614
                                       .00323875
164.745
                                                      .08297207
           3563.988
                         .04649606
165.711
                                       .00332317
                                                     .08297207
166.656
            3495.506
                         .04767717
                                       .00340759
                                                      .08297207
                         .04885827
167.455
            3427.355
                                       .00349200
                                                     .08297207
168.240
            3362.162
                         .05003937
                                       .00357642
                                                      .08297207
                         .05122047
                                                     .08297207
           3298.012
                                       .00366083
168.926
169.575
             3236.065
                         .05240157
                                       .00374525
                                                      .08297207
170.188
            3176.179
                         .05358268
                                       .00382966
                                                     .08297207
```

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 161.289 m-kN

#### p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 1
Depth below ground surface = .000 m
Depth below pile head = .000 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

y, m	p, kN/m
.0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356	.000 452.916 468.738 551.327 599.856 646.664 693.472 721.605 746.964 772.322 797.681 823.039 841.875 857.218 989.280
.0889	989.280

## p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 1
Depth below ground surface = 4.500 m
Depth below pile head = 4.500 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

```
y, m p, kN/ m
```

.0000	.000
.0010	452.916
.0011	468.738
.0022	551.327
.0033	599.856
.0044	646.664
.0056	693.472
.0067	721.605
.0078	746.964
.0089	772.322
.0100	797.681
.0111	823.039
.0122	841.875
.0133	857.218
.0356	989.280
.0667	989.280
.0889	989.280

Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1) Specified shear force at pile head = 365.000 kN Specified bending moment at pile head = 83.550 m-kNSpecified axial load at pile head .000 kN

Non-zero moment for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment ) condition.

Depth	Deflect.	Moment	Shear	Slope	Total	Flx. Rig.	Soil Res
X	Y	M	V	S	Stress	EI	p
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
X m 0.000 .03103 .06207 .09310 .124 .155 .186 .217 .248 .279 .310 .341 .372 .403 .434 .466 .497 .528 .559 .590 .621 .652 .683 .714 .745 .776 .807 .838 .869 .900 .931 .962	y m018217 .017146 .016097 .015071 .014070 .013096 .012150 .011234 .0103350 .009499 .008685 .007906 .007165 .006463 .005801 .005179 .004598 .004057 .003554 .003090 .002661 .002661 .002661 .001910 .001584 .001289 .001023 7.8562-04 3.88E-04 2.27E-04	M kN- m	V kN 365.0 336.5 308.5 281.0 253.8 227.1 200.8 175.0 149.6 124.9 100.8 77.2742 54.2647 31.7662 9.7508 -11.6541 -32.3029 -52.2180 -71.4511 -90.0521 -108.1 -125.5 -142.4 -158.5 -173.9 -188.5 -202.1 -214.6 -226.1 -236.5 -245.0 -247.4 -242.0	S Rad	Stress kN/ m**2  7.4276 8.3950 9.2846 10.0974 10.8349 11.4980 12.0880 12.6061 13.0534 13.7428 13.9881 14.1692 14.3445 14.3445 14.3413 14.2802 14.1631 13.9920 13.7688 13.4951 13.1725 12.8024 12.3868 11.9278 11.4273 10.8877 10.3122 9.7033 9.0645 8.3984 7.7124 7.0330	EI kN- m**2	P kN/m924.626 -909.848 -895.361 -881.196 -867.377 -853.926 -840.867 -825.824 -805.638 -766.238 -767.642 -749.872 -732.961 -716.940 -701.832 -677.591 -653.111 -630.311 -630.311 -630.311 -630.311 -653.111 -554.288 -571.541 -554.288 -531.243 -574.240 -7420.874 -420.874 -420.874 -420.874 -4388.085 -350.722 -318.257 -232.174 -76.704 -276.556
1.055 1.086 1.117 1.148 1.179	-2.07E-04 -2.72E-04 -3.21E-04 -3.58E-04 -3.84E-04 -4.00E-04 -4.07E-04	71.7359 64.6627 57.9047 51.4715 45.3703 39.6060 34.1817	-180.3 -169.3	002328 001836 001393 001005 -6.68E-04 -3.72E-04 -1.16E-04	6.3773 5.7485 5.1477 4.5758 4.0334 3.5210 3.0388	4298.603 4296.661 4295.101 4457.318 4462.736 4467.843 4472.637	314.318 327.253 337.267 344.665 349.823 353.010 354.477
	-4.07E-04	29.0988	-158.3	1.03E-04	2.5869	4477.121	354.462
	-4.00E-04	24.3573	-147.3	2.89E-04	2.1654	4481.295	353.187

1.303 -3.89E-04	19.9560	-136.4	4.42E-04	1.7741	4485.163	350.857
1.334 -3.73E-04	15.8926	-125.5	5.66E-04	1.4129	4488.728	347.665
1.366 -3.54E-04	12.1641	-114.8	6.63E-04	1.0814	4491.994	343.786
1.397 -3.32E-04	8.7666	-104.2	7.35E-04	.7794	4494.966	339.382
1.428 -3.08E-04	5.6961	-93.7483	7.83E-04	.5064	4890.861	334.599
1.459 -2.83E-04	2.9478	-83.4419	8.11E-04	.2621	4896.454	329.591
1.490 -2.58E-04	.5169	-73.2928	8.22E-04	4.60E-02	4898.917	324.466
1.521 -2.32E-04	-1.6014	-63.3030	8.18E-04	.1424	4898.917	319.321
1.552 -2.07E-04	-3.4122	-53.4719	8.03E-04	.3033	4895.509	314.239
1.583 -1.82E-04	-4.9204	-43.8773	7.76E-04	.4374	4892.440	304.075
1.614 -1.59E-04	-6.1357	-34.6228	7.41E-04	.5455	4889.964	292.328
1.645 -1.36E-04	-7.0694	-25.7235	6.97E-04	.6285	4496.449	281.182
1.676 -1.16E-04	-7.7323	-17.1585	6.46E-04	.6874	4495.870	270.789
1.707 -9.63E-05	-8.1344	-9.0255	5.91E-04	.7231	4495.518	
						253.333
1.738 -7.88E-05	-8.2925	-1.8770	5.35E-04	.7372	4495.380	207.349
1.769 -6.31E-05	-8.2509	3.9169	4.78E-04	.7335	4495.416	166.039
1.800 -4.92E-05	-8.0494	8.5010	4.21E-04	.7156	4495.593	129.379
1.831 -3.70E-05	-7.7232	12.0177	3.67E-04	.6866	4495.878	97.255
1.862 -2.64E-05	-7.3034	14.6051	3.15E-04	.6493	4496.244	69.484
1.893 -1.74E-05	-6.8167	16.3944	2.66E-04	.6060	4496.670	45.829
1.924 -9.89E-06	-6.2859	17.5092	2.23E-04	.5588	4889.658	26.015
1.955 -3.60E-06	-5.7299	18.0596	1.85E-04	.5094	4890.791	9.457
1.986 1.57E-06	-5.1649	18.1423	1.50E-04	.4592	4891.942	-4.131
2.017 5.72E-06	-4.6039	17.8447	1.19E-04	.4093	4893.085	-15.045
2.048 8.96E-06	-4.0573	17.2454	9.16E-05	.3607	4894.197	-23.575
2.079 1.14E-05	-3.5335	16.4140	6.76E-05	.3141	4895.263	-30.005
2.110 1.32E-05	-3.0385	15.4115	4.67E-05	.2701	4896.269	-34.605
2.141 1.43E-05	-2.5769	14.2905	2.89E-05	.2291	4897.208	-37.633
2.172 1.50E-05	-2.1515	13.0963	1.39E-05	.1913	4898.072	-39.329
2.203 1.52E-05	-1.7640	11.8667	1.54E-06	.1568	4898.859	-39.911
2.234 1.50E-05	-1.4150	10 6332	-8.53E-06	.1258	4898.917	-39.580
2.266 1.46E-05	-1.1040		-1.65E-05	9.81E-02	4898.917	-38.518
2.297 1.40E-05	8302	8.2513	-2.26E-05	7.38E-02	4898.917	-36.885
2.328 1.32E-05	5919	7.1386	-2.71E-05	5.26E-02	4898.917	-34.823
2.359 1.23E-05	3871		-3.02E-05	3.44E-02	4898.917	-32.455
2.390 1.14E-05	2136		-3.21E-05	1.90E-02	4898.917	-29.886
2.421 1.03E-05	-6.89E-02	4.2413	-3.30E-05	6.12E-03	4898.917	-27.207
2.452 9.31E-06	4.97E-02	3.4391	-3.31E-05	4.41E-03	4898.917	-24.492
2.483 8.29E-06	.1446		-3.25E-05	1.29E-02	4898.917	-21.803
2.514 7.29E-06	.2185	2.0847	-3.13E-05	1.94E-02	4898.917	-19.188
2.545 6.34E-06	.2740	1.5280	-2.98E-05	2.44E-02	4898.917	-16.687
2.576 5.45E-06	.3134		-2.79E-05	2.79E-02	4898.917	-14.327
2.607 4.61E-06	.3390		-2.58E-05	3.01E-02	4898.917	-12.130
2.638 3.84E-06	.3529	.2911	-2.37E-05	3.14E-02	4898.917	-10.108
2.669 3.14E-06	.3570	5.98E-03	-2.14E-05	3.17E-02	4898.917	-8.268
2.700 2.51E-06	.3532		-1.92E-05	3.14E-02	4898.917	-6.613
2.731 1.95E-06	.3431		-1.69E-05	3.05E-02	4898.917	-5.140
2.762 1.46E-06	.3280	5467	-1.48E-05	2.92E-02	4898.917	-3.845
2.793 1.03E-06	.3091	6486	-1.28E-05	2.75E-02	4898.917	-2.720
2.824 6.67E-07	.2877		-1.09E-05	2.56E-02	4898.917	-1.755
2.855 3.57E-07	.2646		-9.17E-06	2.35E-02	4898.917	937989
2.886 9.81E-08	.2405	7784	-7.57E-06	2.14E-02	4898.917	258135
2.917 -1.13E-07	.2162	7778	-6.12E-06	1.92E-02	4898.917	.297320
2.948 -2.82E-07	.1923		-4.82E-06	1.71E-02	4898.917	.740935
2.979 -4.12E-07	.1690		-3.68E-06	1.50E-02	4898.917	1.085
3.010 -5.10E-07	.1467		-2.68E-06		4898.917	1.342
3.041 -5.79E-07	.1258	6512	-1.82E-06	1.12E-02	4898.917	1.523
3.072 -6.23E-07	.1063		-1.08E-06	9.45E-03	4898.917	1.639
3.103 -6.46E-07			-4.65E-07			1.700
	8.84E-02			7.86E-03	4898.917	
3.134 -6.52E-07	7.21E-02	4974	4.31E-08	6.41E-03	4898.917	1.715
3.166 -6.43E-07	5.75E-02	4445	4.54E-07	5.12E-03	4898.917	1.692
3.197 -6.24E-07	4.46E-02	3928	7.77E-07	3.96E-03	4898.917	1.641
3.228 -5.95E-07	3.32E-02	3431	1.02E-06	2.95E-03	4898.917	1.566
3.259 -5.60E-07	2.33E-02	2959	1.20E-06	2.07E-03	4898.917	1.473
3.290 -5.21E-07	1.48E-02	2518	1.32E-06	1.31E-03	4898.917	1.369
3.321 -4.78E-07	7.64E-03	2110	1.39E-06	6.79E-04	4898.917	1.257
3.352 -4.34E-07	1.69E-03	1738	1.42E-06	1.51E-04	4898.917	1.142
3.383 -3.90E-07	-3.15E-03	1402	1.42E-06	2.80E-04	4898.917	1.025
3.414 -3.46E-07	-7.01E-03	1101	1.39E-06	6.23E-04	4898.917	.910081
3.445 -3.04E-07			1.33E-06	8.88E-04	4898.917	.798699
				1.08E-03		
3.476 -2.63E-07			1.26E-06		4898.917	.692482
3.507 -2.25E-07			1.18E-06	1.22E-03	4898.917	.592574
3.538 -1.90E-07	-1.47E-02	-2.36E-02	1.09E-06	1.31E-03	4898.917	.499773
3.569 -1.58E-07			9.95E-07	1.35E-03	4898.917	.414584
3.600 -1.28E-07		2.25E-03	8.99E-07	1.36E-03	4898.917	.337260
3.631 -1.02E-07		1.16E-02	8.02E-07	1.34E-03	4898.917	.267849
3.662 -7.84E-08	-1.46E-02	1.90E-02	7.09E-07	1.30E-03	4898.917	.206231
3.693 -5.78E-08		2.46E-02	6.18E-07	1.23E-03	4898.917	.152152
3.724 -4.00E-08		2.86E-02	5.33E-07	1.16E-03	4898.917	.105257
3.755 -2.48E-08		3.12E-02	4.53E-07	1.08E-03	4898.917	.065112
3.786 -1.19E-08	-1.11E-02	3.27E-02	3.80E-07	9.88E-04	4898.917	.031234

```
3.817 -1.18E-09 -1.01E-02 3.32E-02 3.13E-07 8.97E-04 4898.917 -.003106
3.848 7.53E-09 -9.05E-03 3.30E-02 2.52E-07 8.05E-04 4898.917 -.019805
3.879 1.45E-08 -8.04E-03 3.21E-02 1.98E-07 7.15E-04 4898.917 -.038032
3.910 1.98E-08 -7.06E-03 3.07E-02 1.50E-07 6.28E-04 4898.917 -.052101
3.941 2.38E-08 -6.14E-03 2.89E-02 1.08E-07 5.46E-04 4898.917 -.062516
3.972 2.65E-08 -5.27E-03 2.68E-02 7.20E-08 4.69E-04 4898.917 -.062516
3.972 2.65E-08 -4.47E-03 2.46E-02 4.11E-08 3.98E-04 4898.917 -.06757
4.003 2.82E-08 -4.47E-03 2.23E-02 1.51E-08 3.98E-04 4898.917 -.074271
4.034 2.91E-08 -3.74E-03 2.23E-02 1.51E-08 3.33E-04 4898.917 -.076472
4.066 2.92E-08 -3.09E-03 1.99E-02 -6.55E-09 2.75E-04 4898.917 -.076737
4.097 2.87E-08 -2.51E-03 1.75E-02 -2.43E-08 2.23E-04 4898.917 -.075404
4.128 2.77E-08 -2.00E-03 1.52E-02 -3.86E-08 1.78E-04 4898.917 -.072772
4.159 2.63E-08 -1.57E-03 1.30E-02 -4.99E-08 1.39E-04 4898.917 -.069104

      4.128
      2.77E-08
      -2.00E-03
      1.52E-02
      -3.86E-08
      1.78E-04
      4898.917

      4.159
      2.63E-08
      -1.57E-03
      1.30E-02
      -4.99E-08
      1.39E-04
      4898.917

      4.190
      2.46E-08
      -1.19E-03
      1.09E-02
      -5.86E-08
      1.06E-04
      4898.917

      4.221
      2.26E-08
      -8.85E-04
      9.02E-03
      -6.52E-08
      7.87E-05
      4898.917

      4.252
      2.05E-08
      -6.34E-04
      7.26E-03
      -7.00E-08
      5.64E-05
      4898.917

      4.283
      1.83E-08
      -4.35E-04
      5.68E-03
      -7.34E-08
      3.86E-05
      4898.917

      4.314
      1.60E-08
      -2.82E-04
      4.28E-03
      -7.57E-08
      2.50E-05
      4898.917

                                                                                                                                                                                                                                                                                                                                                                                            -.069104
                                                                                                                                                                                                                                                                                                                                                                                            -.064628
                                                                                                                                                                                                                                                                                                                                                                                              -.059533
                                                                                                                                                                                                                                                                                                                                                                                              -.053981
                                                                                                                                                                                                                                                                                                                                                                                              -.048101
                                                                                                                                                                                                                                                                                                                                                                                             -.041996
 4.345 1.36E-08 -1.69E-04 3.07E-03 -7.71E-08 1.50E-05 4898.917

4.376 1.12E-08 -9.10E-05 2.06E-03 -7.79E-08 8.09E-06 4898.917

4.407 8.75E-09 -4.11E-05 1.25E-03 -7.83E-08 3.66E-06 4898.917

4.438 6.32E-09 -1.35E-05 6.33E-04 -7.85E-08 1.20E-06 4898.917
                                                                                                                                                                                                                                                                                                                                                                                            -.035745
                                                                                                                                                                                                                                                                                                                                                                                              -.029407
                                                                                                                                                                                                                                                                                                                                                                                             -.023022
                                                                                                                                                                                                                                                                                                                                                                                            -.016615
 4.469 3.88E-09 -1.82E-06 2.17E-04 -7.86E-08 1.62E-07 4898.917
4.500 1.44E-09 0.0 0.0 -7.86E-08 0.0 4898.917
                                                                                                                                                                                                                                                                                                                                                                                             -.010202
                                                                                                                                                                                                                                                                                                                                                                                            -.003788
```

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of total stress due to combined axial stress and bending may not be representative of actual conditions.

Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

```
Pile-head deflection
                                                .01821670 m
Computed slope at pile head =

Maximum bending moment =

Maximum shear force =

Depth of maximum bending moment =
                                                -.03479080
                                               161.355 kN- m
                                                    365.000 kN
                                                .43448276 m
Depth of maximum shear force =
                                                 0.000 m
Number of iterations
Number of zero deflection points =
```

Summary of Pile-head Response

Definition of symbols for pile-head boundary conditions:

```
v = pile-head displacment, m
M = pile-head moment, kN- m
V = pile-head shear force, kN
S = pile-head slope, radians
```

R = rotational stiffness of pile-head, m- kN/rad

BC Type	Boundary Condition 1	Boundary Condition 2	Axial Load kN	Pile Head Deflection m	Maximum Moment m- kN	Maximum Shear kN
1	V = 365.000	M = 83.550	0.0000	.018217	161.3551	365.0000

```
LPILE Plus for Windows, Version 4.0 (4.0.8)
               Analysis of Individual Piles and Drilled Shafts
               Subjected to Lateral Loading Using the p-y Method
                     (c) Copyright ENSOFT, Inc., 1985-2003
                              All Rights Reserved
Path to file locations:
                              L:\Programs\LPILE\Chapter 6\Ch. 6 Example with P=474.5\P=Pult\
Path to file locations: L:\Programs\LPII
Name of input data file: Up analysis.lpd
Name of output file: Up analysis.lpo
Name of plot output file: Up analysis.lpp
Name of runtime file:
                            Up analysis.lpr
Time and Date of Analysis
               Date: May 4, 2005 Time: 17: 5:12
______
                          Problem Title
Up Analysis for P=474.5 Case
______
                                 Program Options
Units Used in Computations - SI Units, meters, kilopascals
Basic Program Options:
Analysis Type 3:
 Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment
  Capacity with Pile Response Computed Using Nonlinear EI
Computation Options:
- User-specified p-y curves used in analysis
- Analysis uses p-y multiplers for group action
- Analysis assumes no shear resistance at pile tip
- Analysis for fixed-length pile or shaft only
- No computation of foundation stiffness matrix elements
- Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths
Solution Control Parameters:
- Maximum number of iterations allowed = 100
- Deflection tolerance for convergence = 2.5400E-07 m
- Maximum allowable deflection = 2.5400E+00 m
                                            2.5400E-07 m
Printing Options:
- Values of pile-head deflection, bending moment, shear force, and
  soil reaction are printed for full length of pile.
- Printing Increment (spacing of output points) =
Pile Structural Properties and Geometry
Pile Length
                                                  10.00 m
                                                  .00 m
Depth of ground surface below top of pile =
Slope angle of ground surface
Structural properties of pile defined using 2 points
                 Pile Moment of Pile Modulus of Diameter Inertia Area Elasticity m m**4 Sq. m kN/Sq. m
```

1	0.0000	.17780000	1.0000	.024800	200000000.000
2	10.0000	.17780000	1.0000	.024800	200000000.000

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of moment of inertia and modulus of are not used for any computations other than total stress due to combined axial loading and bending.

Soil and Rock Layering Information

The soil profile is modelled using 4 layers

Layer 1 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = .000 m 5.290 m Layer 2 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = 5.290 m 5.310 m

Layer 3 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = 5.310 m 8.000 m

Layer 4 is modelled using user-specied p-y curves Distance from top of pile to top of layer = Distance from top of pile to bottom of layer = 8.000 m 10.000 m

(Depth of lowest layer extends .00 m below pile tip)

______ Effective Unit Weight of Soil vs. Depth

Distribution of effective unit weight of soil with depth is defined using 8 points

Point No.	Depth X m	Eff. Unit Weight kN/ m**3
1	.00	11.40000
2	5.29	11.40000
3	5.29	11.40000
4	5.31	21.20000
5	5.31	21.20000
6	8.00	21.20000
7	8.00	21.20000
8	10.00	21.20000

Shear Strength of Soils

Distribution of shear strength parameters with depth defined using 0 points

No.	m	kN/ m**2	Deg.	k_rm	%
Point	Depth X	Cohesion c	Angle of Friction	E50 or	RQD

#### Notes:

- (1) Cohesion = uniaxial compressive strength for rock materials.
  (2) Values of E50 are reported for clay strata.
  (3) Default values will be generated for E50 when input values are 0.
- (4) RQD and k rm are reported only for weak rock strata.

p-y Modification Factors

Distribution of p-y multipliers with depth defined using 5 points

Point No.	Depth X m	p-mult	y-mult
1	.000	1.0000	1.0000
2	5.290	1.0000	1.0000
3	5.310	1.0000	1.0000
4	8.000	1.0000	1.0000
5	10.000	1.0000	1.0000

User-specified p-y Curves

User-specified p-y curves defined using 8 curves.

User-specified curve number 1 at depth = .000 m

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.248

User-specified curve number 2 at depth = 5.290 m

Point No.	y m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.248

User-specified curve number 3 at depth = 5.290 m

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0002	92.072
3	.0004	109.493
4	.0009	137.680
5	.0018	163.731
6	.0027	181.198
7	.0037	194.710
8	.0092	244.834
9	.0183	291.159
10	.0366	346.248
11	.0412	346.248
12	.0458	346.298

User-specified curve number 4 at depth = 5.310 m

No.	m	kN/ m		
Point y		p,		

1	.0000	.000
2	.0002	65.766
3	.0005	78.209
4	.0011	98.343
5	.0023	116.950
6	.0034	129.427
7	.0046	139.078
8	.0115	174.882
9	.0229	207.971
10	.0458	247.320
11	.0515	247.320
12	.0573	247.320

User-specified curve number 5 at depth = 5.310 m

У	p,
m	kN/ m
.0000	.000
.0002	65.766
.0005	78.209
.0011	98.343
.0023	116.950
.0034	129.427
.0046	139.078
.0115	174.882
.0229	207.971
.0458	247.320
.0515	247.320
.0573	247.320
	m

User-specified curve number 6 at depth = 8.000 m

Point No.	У m	p, kN/ m
1	.0000	.000
2	.0002	56.414
3	.0005	67.088
4	.0011	84.358
5	.0023	100.319
6	.0034	111.022
7	.0046	119.300
8	.0115	150.012
9	.0229	178.396
10	.0458	212.150
11	.0515	212.150
12	.0573	212.150

User-specified curve number 7 at depth = 8.000 m

Point No.	y m	p, kN/ m
1	.0000	.000
2	.0002	56.414
3	.0005	67.088
4	.0011	84.358
5	.0023	100.319
6	.0034	111.022
7	.0046	119.300
8	.0115	150.012
9	.0229	178.396
10	.0458	212.150
11	.0515	212.150
12	.0573	212.150

User-specified curve number 8 at depth = 10.000 m

Point No.	Y m	p, kN/ m
1	.0000	.000
2	.0005	26.070
3	.0011	32.781
4	.0020	21.922
5	.0023	38.983
6	.0034	43.142
7	.0046	46.359
8	.0115	58.294
9	.0151	82.440

10 11 12	.0229 .0458 .0573	69.324 82.440 82.440			
		Loadi	ng Type		
Static loading					
	Pile-head Load	ding and Pi	le-head Fixit	су Со	
Number of load	s specified =	1			
Load Case Numb	er 1				
Pile-head boun Shear force at Bending moment Axial load at	dary condition pile head at pile head pile head	ns are Shea = = =	r and Moment 330.000 kN -76.200 m- k 474.500 kN	(BC	Type 1)
	er the applied				es the pile-head not a free-head
Output of p-y Curves at Specified Depths					
No.	th Below Pile	Head	Depth Below 0 m	Groun	d Surface
1	.000		.00	0 0	
2 3	5.290 5.310		5.29 5.31		
4	8.000		8.00	0 0	
5	10.000		10.00		
Depth of groun	d surface belo	ow top of p	ile =	.00	m
Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness					
Pile Description:					
The sectional shape is a circular shaft with steel casing.					
Outside Diamet Wall thickness Cross-sectiona Moment of iner		ll ll shell	= .15 = .006 = 2.08692E-		m m**2 m**4
Material Properties:					
Compressive St Yield Stress o Steel shell or	f Reinforcemer	nt	=	0.	kN/ m**2 kN/ m**2 kN/ m**2
Modulus of Ela Cover Thicknes				00.	
Number of Rein Area of Single Number of Rows	Bar	ng Bars	= .000	10 000 5	m**2

Distribution and Area of Steel Reinforcement

Row Number	Area of Reinforcement m**2	Distance to Centroidal Axis m
1	.000000	.0736
2	.000000	.0455
3	.000000	.0000
4	.000000	0455
5	.000000	0736

Axial Thrust Force = 474.50 kN

Bending Moment	Bending Stiffness	Bending Curvature	Maximum Strain	Neutral Axis Position
kN-m	kN-m2	rad/m	m/m	m
 1.69826245	4792.874	.00035433	.00031727	.90691267
2.45303965	4792.862	.00051181	.00032949	.65527803
3.20781175	4792.848	.00066929	.00034172	.52206775
3.96257836	4792.833	.00082677	.00035395	.43960844
4.71733626	4792.814	.00098425	.00036619	.38354674
5.47208598	4792.792	.00114173	.00037843	.34295465
6.22682760	4792.770	.00129921	.00039068	.31220536
6.98155916 7.73628058	4792.746 4792.720	.00145669 .00161417	.00040293	.28810838 .26871577
8.49098340	4792.688	.00101417	.00041313	.25277953
9.24568013	4792.659	.00192913	.00043973	.23944236
10.000	4792.625	.00208661	.00045201	.22812367
10.755	4792.590	.00224409	.00046429	.21839481
11.510	4792.551	.00240157	.00047658	.20994649
12.264	4792.509	.00255906	.00048888	.20253996
13.019	4792.470	.00271654	.00050118	.19599075
13.774	4792.426	.00287402	.00051348	.19016320
14.528 15.283	4792.379 4792.326	.00303150 .00318898	.00052579 .00053812	.18494336
16.035	4791.716	.00316696	.00055042	.17597957
16.774	4787.090	.00350394	.00056260	.17206198
17.571	4799.091	.00366142	.00057505	.16855677
18.301	4792.220	.00381890	.00058745	.16532828
19.053	4791.556	.00397638	.00059979	.16233854
24.610	4771.704	.00515748	.00068957	.14520315
29.767	4696.101	.00633858	.00078032	.13460612
35.334 39.786	4698.840 4572.710	.00751969 .00870079	.00087092 .00095706	.12731897 .12149685
45.804	4635.195	.00988189	.00105014	.11776917
50.555	4569.762	.01106299	.00113526	.11411745
56.180	4588.341	.01224409	.00122769	.11176798
61.386	4572.465	.01342520	.00131523	.10946735
64.845	4439.494	.01460630	.00139171	.10678147
71.647	4538.208	.01578740	.00149414	.10614120
74.736	4404.370	.01696850 .01814961	.00156633	.10380800
81.890 85.716	4511.946 4434.167	.01814961	.00167053 .00175060	.10354213
92.018	4486.089	.02051181	.00173000	.10200002
97.124	4477.213	.02169291	.00193616	.10075315
102.139	4465.294	.02287402	.00202929	.10021598
105.295	4377.229	.02405512	.00210249	.09890288
109.026	4320.217	.02523622	.00218134	.09793705
113.742	4305.584	.02641732	.00227957	.09779054
118.611	4297.758	.02759843	.00238148	.09779054
127.233 131.954	4420.944 4404.252	.02877953 .02996063	.00247762 .00257166	.09758978 .09733476
136.319	4377.388	.03114173	.00257100	.09715027
140.277	4339.870	.03232283	.00276706	.09710686
143.850	4293.538	.03350394	.00287126	.09719911
147.136	4242.066	.03468504	.00297869	.09737816
150.123	4185.651	.03586614	.00308557	.09753009
152.748	4123.053	.03704724	.00319502	.09774171
152.748	3995.667	.03822835	.00329874	.09779054
152.748	3875.917	.03940945	.00340066	.09779054
154.387 155.966	3803.521 3733.787	.04059055 .04177165	.00350258	.09779054
157.340	3663.103	.04177165	.00370642	.09779054
158.551	3592.498	.04413386	.00380833	.09779054

p-y Curve Computed by Interpolation from User-input Curves

Soil Layer Number	=	1
Depth below ground surface	=	.000 m
Depth below pile head	=	.000 m
p-multiplier	=	1.00000
y-multiplier	=	1.00000

y, m	p, kN/ m
y, m .0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133	p, kN/m  .000 140.575 143.795 171.931 189.761 201.500 211.627 221.754 231.882 242.009 248.913 254.570 260.227 265.884 343.117
.0667	346.248 346.248

#### p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number
Soil Layer Number = 2
Depth below ground surface = 5.290 m
Depth below pile head = 5.290 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

y, m	p, kN/m
.0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356	.000 140.575 143.795 171.931 189.761 201.500 211.627 221.754 231.882 242.009 248.913 254.570 260.227 265.884 343.117 346.248
.0889	346.248

#### p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number
Depth below ground surface = 5.310 m
Depth below pile head = 5.310 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

y, m	p, kN/m
.0000	.000
.0010	94.987
. 0011	98.517

```
115.748
128.676
137.831
144.040
149.806
155.572
161.339
167.105
172.871
.0022
.0033
.0044
.0056
.0067
.0078
.0089
.0100
.0111
                     176.983
180.208
.0122
.0133
                     229.725
247.320
.0356
.0667
.0889
                     247.320
```

p-y Curve Computed by Interpolation from User-input Curves

Soil Layer Number = 4
Depth below ground surface = 8.000 m
Depth below pile head = 8.000 m
p-multiplier = 1.00000
y-multiplier = 1.00000

y, m	p, kN/ m
.0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356	.000 81.480 84.508 99.288 110.377 118.231 123.556 128.502 133.449 138.395 143.341 148.287 151.814 154.581 197.057 212.150
.0889	212.150

 $\ensuremath{\text{p-y}}$  Curve Computed by Interpolation from User-input Curves

 Soil Layer Number
 =
 4

 Depth below ground surface
 =
 10.000 m

 Depth below pile head
 =
 10.0000 m

 p-multiplier
 =
 1.00000 m

 y-multiplier
 =
 1.00000 m

y, m	p, kN/m
y, m .0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067 .0078 .0089 .0100 .0111 .0122 .0133 .0356 .0667	000 31.663 32.645 34.576 42.892 45.943 48.013 49.935 51.857 53.779 55.702 57.624 63.148 70.602 76.575 82.440
.0889	82.440

Computed Values of Load Distribution and Deflection

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Pile-head boundary conditions are Shear and Moment (BC Type 1) Specified shear force at pile head = 330.000 kN Specified bending moment at pile head = -76.200 m- kN Specified axial load at pile head = 474.500 kN

Non-zero moment for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment )condition.

Depth	Deflect.	Moment	Shear	Slope	Total	Flx. Rig.	Soil Res
X m	У m	M kN- m	V kN	S Rad.	Stress kN/ m**2	EI kN- m**2	p kN/ m
0.000 .06897	.039554	-76.2000 -53.2344	330.0 306.1	030915 031890	1.91E+04 1.91E+04	4578.630 4578.630	-346.250 -346.250
.138	.035155	-31.8893	282.4	032531	1.91E+04	4578.630	-341.900
.207	.032895	-12.1547	259.0	032858	1.91E+04	4792.515	-335.096
.276	.030623	5.9918	236.2	032903	1.91E+04	4792.777	-328.257
.345	.028357	22.5742	213.8	032697	1.91E+04	4778.996	-321.435
.414	.026113 .023908	37.6172 51.1451	191.8 170.4	032254 031588	1.91E+04 1.91E+04	4635.213 4571.717	-314.680 -308.042
.552	.021756	63.1827	149.3	031388	1.91E+04	4504.909	-301.564
.621	.019671	73.7543	128.8	029664	1.91E+04	4448.408	-295.287
.690	.017665	82.8840	108.6	028456	1.91E+04	4492.096	-287.925
.759	.015746	90.6026	89.1283	027121	1.91E+04	4474.516	-278.158
.828	.013924	96.9526	70.2648	025676	1.91E+04	4477.512	-268.882
.897 .966	.012204 .010594	102.0 105.7	52.0230 34.3658	024142 022521	1.91E+04 1.91E+04	4465.687 4371.015	-260.130 -251.930
1.034	.009098	108.2	17.2680	020826	1.91E+04	4333.193	-243.906
1.103	.007721	109.5	.8796	019091	1.91E+04	4318.897	-231.358
1.172	.006465	109.6	-14.6813	017343	1.91E+04	4318.567	-219.908
1.241	.005329	108.6	-29.4905	015603	1.91E+04	4327.408	-209.558
1.310	.004313	106.5	-43.6234	013895	1.91E+04	4358.842	-200.295
1.379 1.448	.003413	103.5 99.4374	-57.1104 -69.8877	012247 010675	1.91E+04 1.91E+04	4429.278 4471.724	-190.827 -179.714
1.517	.001940	94.5144	-81.8245	009181	1.91E+04	4481.754	-166.453
1.586	.001357	88.7521	-92.7682	007767	1.91E+04	4459.308	-150.915
1.655	8.69E-04	82.2272	-102.7	006452	1.91E+04	4505.249	-135.925
1.724	4.67E-04	75.0145	-111.3	005235	1.91E+04	4408.633	-113.290
1.793	1.47E-04	67.2246	-117.5	004131	1.91E+04	4474.417	-67.540
	-1.02E-04 -2.90E-04	59.0795 51.1296	-118.2 -113.1	003168 002337	1.91E+04 1.91E+04	4579.515 4571.665	47.154 99.928
	-4.25E-04	43.6298	-105.8	001625	1.91E+04	4612.790	110.890
	-5.14E-04	36.6360	-98.0281	001028	1.91E+04	4662.822	115.942
2.138	-5.67E-04	30.1760	-89.9306	-5.36E-04	1.91E+04	4696.303	118.887
	-5.88E-04	24.2669	-81.6894	-1.39E-04	1.91E+04	4772.936	120.108
	-5.86E-04	18.9176	-73.4109	1.73E-04	1.91E+04	4791.676	119.967
	-5.64E-04 -5.29E-04	14.1299 9.9005	-65.1787 -57.0566	4.10E-04 5.83E-04	1.91E+04 1.91E+04	4792.404 4792.629	118.767 116.776
	-4.84E-04	6.2219	-49.0908	6.99E-04	1.91E+04	4792.770	114.232
	-4.33E-04	3.0836	-41.3125	7.66E-04	1.91E+04	4792.850	111.339
	-3.78E-04	.4735	-33.7626	7.92E-04	1.91E+04	4792.874	107.609
	-3.24E-04	-1.6251	-26.5060	7.84E-04	1.91E+04	4792.874	102.832
	-2.70E-04	-3.2338	-19.5740	7.49E-04	1.91E+04	4792.848	98.195
	-2.20E-04 -1.75E-04	-4.3740 -5.0657	-12.9522 -6.9450	6.94E-04 6.26E-04	1.91E+04 1.91E+04	4792.822 4792.804	93.838 80.372
	-1.34E-04	-5.3729	-2.0475	5.51E-04	1.91E+04	4792.795	61.656
	-9.86E-05	-5.3842	1.6440	4.73E-04	1.91E+04	4792.795	45.396
	-6.86E-05	-5.1771	4.2988	3.97E-04	1.91E+04	4792.801	31.595
	-4.38E-05	-4.8173	6.0834	3.26E-04	1.91E+04	4792.811	20.159
	-2.37E-05 -7.99E-06	-4.3593 -3.8473	7.1552 7.6588	2.60E-04 2.00E-04	1.91E+04 1.91E+04	4792.823 4792.835	10.924 3.680
3.379	3.92E-06	-3.3160	7.7235	1.49E-04	1.91E+04	4792.846	-1.806
3.448	1.25E-05	-2.7918	7.4620	1.05E-04	1.91E+04	4792.856	-5.777
3.517	1.84E-05	-2.2936	6.9707	6.84E-05	1.91E+04	4792.865	-8.472
3.586	2.20E-05	-1.8348	6.3296	3.87E-05	1.91E+04	4792.872	-10.120
3.655	2.37E-05	-1.4231	5.6038	1.53E-05	1.91E+04	4792.874	-10.929
3.724 3.793	2.41E-05 2.34E-05	-1.0628 7548		-2.63E-06 -1.57E-05	1.91E+04 1.91E+04	4792.874 4792.874	-11.089 -10.763
3.862	2.19E-05	4975		-2.47E-05	1.91E+04	4792.874	-10.092
3.931	2.00E-05	2880		-3.04E-05	1.91E+04	4792.874	-9.193
4.000	1.77E-05	1222		-3.33E-05	1.91E+04	4792.874	-8.164
4.069	1.54E-05	4.94E-03		-3.42E-05	1.91E+04	4792.874	-7.078
4.138	1.30E-05 1.08E-05	9.84E-02 .1633		-3.34E-05 -3.15E-05	1.91E+04 1.91E+04	4792.874 4792.874	-5.995 -4.956
4.207 4.276	8.67E-06	.1633		-3.15E-05	1.91E+04 1.91E+04	4792.874	-4.956 -3.992
4.345	6.78E-06	.2266		-2.58E-05	1.91E+04	4792.874	-3.122
4.414	5.12E-06	.2338		-2.25E-05	1.91E+04	4792.874	-2.355
4.483	3.68E-06	.2297		-1.91E-05	1.91E+04	4792.874	-1.695
4.552	2.48E-06	.2174	2258	-1.59E-05	1.91E+04	4792.874	-1.140

4.621	1.49E-06	.1996	2887	-1.29E-05	1.91E+04	4792.874	684197
							319626
4.690	6.94E-07	.1785		-1.02E-05	1.91E+04	4792.874	319626
4.759	7.95E-08	.1557	3356	-7.79E-06	1.91E+04	4792.874	036584
4.828	-3.81E-07	.1327		-5.72E-06	1.91E+04	4792.874	.175332
4.897	-7.10E-07	.1104	3135	-3.97E-06	1.91E+04	4792.874	.326633
4.966	-9.29E-07	8.97E-02		-2.53E-06	1.91E+04	4792.874	.427481
5.034	-1.06E-06	7.09E-02	2560	-1.38E-06	1.91E+04	4792.874	.487352
5.103	-1.12E-06	5.45E-02	2214	-4.73E-07	1.91E+04	4792.874	.514809
5 172	-1.12E-06	4.04E-02	1858	2.10E-07	1.91E+04	4792.874	.517375
5.241	-1.09E-06	2.88E-02	1507	7.09E-07	1.91E+04	4792.874	.501465
5 310	-1.03E-06	1.96E-02	1217	1.06E-06	1.91E+04	4792.874	.337408
5.379	-9.43E-07	1.20E-02	-9.94E-02	1.28E-06	1.91E+04	4792.874	.309101
5 118	-8.49E-07	5 Q1F_03	-7.92E-02	1.41E-06	1.91E+04	4792.874	.277110
5.517	-7.49E-07	9.61E-04	-6.13E-02	1.46E-06	1.91E+04	4792.874	.243469
5 586	-6.47E-07	-2 7/F-03	_4 575-02	1.45E-06	1.91E+04	4792.874	.209761
5.655	-5.49E-07	-5.43E-03	-3.23E-02	1.39E-06	1.91E+04	4792.874	.177171
5 724	-4.56E-07	-7 28E-03	-2 12F-02	1.30E-06	1.91E+04	4792.874	.146551
5.793	-3.70E-07	-8.43E-03	-1.20E-02	1.19E-06	1.91E+04	4792.874	.118470
5 862	-2.92E-07	-0 02E-03	_/ 715_03	1.06E-06	1.91E+04	4792.874	.093267
5.931	-2.24E-07	-9.15E-03	9.57E-04	9.29E-07	1.91E+04	4792.874	.071096
6 000	-1.64E-07	_8 95E_03	5.20E-03	7.99E-07	1.91E+04	4792.874	.051968
6.069	-1.13E-07	-8.49E-03	8.23E-03	6.73E-07	1.91E+04	4792.874	.035784
6 138	-7.11E-08	-7 86E-03	1.02E-02	5.56E-07	1.91E+04	4792.874	.022370
6.207	-3.67E-08	-7.11E-03	1.14E-02	4.48E-07	1.91E+04	4792.874	.011500
	-9.34E-09		1.19E-02	3.51E-07	1.91E+04	4792.874	.002915
6.345	1.18E-08	-5.50E-03	1.19E-02	2.67E-07	1.91E+04	4792.874	003658
6.414		-4.69E-03	1.15E-02	1.93E-07	1.91E+04	4792.874	008491
6.483	3.84E-08	-3.93E-03	1.08E-02	1.31E-07	1.91E+04	4792.874	011850
6.552	4 558-08	-3.22E-03	9.86E-03	7.98E-08	1.91E+04	4792.874	013985
6.621	4.94E-08	-2.57E-03	8.86E-03	3.81E-08	1.91E+04	4792.874	015126
6.690	5 088-08	-2.00E-03	7.80E-03	5.21E-09	1.91E+04	4792.874	015479
6.759	5.01E-08	-1.50E-03	6.74E-03	-2.00E-08	1.91E+04	4792.874	015226
6.828	4 80E-08	-1.07E-03	5 725-03	-3.84E-08	1.91E+04	4792.874	014524
6.897	4.48E-08	-7.07E-04	4.75E-03	-5.12E-08	1.91E+04	4792.874	013509
6.966	4 105-08	-4.10E-04	3 868-03	-5.92E-08	1.91E+04	4792.874	012291
7.034	3.67E-08	-1.71E-04	3.06E-03	-6.34E-08	1.91E+04	4792.874	010960
7.103	3.22E-08	1.61E-05	2 358-03	-6.45E-08	1.91E+04	4792.874	009589
7.172	2.78E-08	1.57E-04	1.73E-03	-6.33E-08	1.91E+04	4792.874	008234
7.241	2.35E-08	2.59E-04	1 21 - 03	-6.03E-08	1.91E+04	4792.874	006935
7.310	1.95E-08	3.28E-04	7.75E-04	-5.60E-08	1.91E+04	4792.874	005723
7.379	1.58E-08	3.70E-04	4 198-04	-5.10E-08	1.91E+04	4792.874	004615
7.448	1.24E-08	3.90E-04	1.34E-04	-4.55E-08	1.91E+04	4792.874	003624
7.517	9.48E-09	3 92E-04	-8.54E-05	-3 99E-08	1.91E+04	4792.874	002753
7.586	6.92E-09	3.80E-04	-2.49E-04	-3.44E-08	1.91E+04	4792.874	002001
7.655	4.74E-09	3 59F-04	-3.65E-04	-2 91F-08	1.91E+04	4792.874	001364
7.724	2.91E-09	3.32E-04	-4.41E-04	-2.41E-08	1.91E+04	4792.874	-8.35E-04
7.793	1.41E-09	3.00E-04	-4.84E-04	-1.95E-08	1.91E+04	4792.874	-4.04E-04
7.862	2.17E-10	2.66E-04	-5.00E-04	-1.55E-08	1.91E+04	4792.874	-6.16E-05
7 931	-7.17E-10	2 32E-04	-4.95E-04	-1 19E-08	1.91E+04	4792.874	2.03E-04
8.000	-1.42E-09		-4.74E-04		1.91E+04	4792.874	4.01E-04
8.069	-1.93E-09	1.67E-04	-4.42E-04	-6.13E-09	1.91E+04	4792.874	5.28E-04
					1.91E+04		
	-2.27E-09		-4.03E-04			4792.874	6.03E-04
8.207	-2.47E-09	1.12E-04	-3.60E-04	-2.13E-09	1.91E+04	4792.874	6.38E-04
	-2.56E-09		-3.16E-04				
					1.91E+04	4792.874	6.41E-04
8.345	-2.56E-09	6.84E-05	-2.73E-04	4.43E-10	1.91E+04	4792.874	6.21E-04
	-2.50E-09		-2.31E-04		1.91E+04		
8.483	-2.38E-09	3.64E-05	-1.92E-04	1.93E-09	1.91E+04	4792.874	5.40E-04
	-2.23E-09	2.44E-05	-1.57E-04	2.37E-09	1.91E+04	4792.874	4.88E-04
8.621	-2.06E-09	1.46E-05	-1.25E-04	2.65E-09	1.91E+04	4792.874	4.33E-04
8,690	-1.87E-09	6.94E-06	-9.72E-05	2.81E-09	1.91E+04	4792.874	3.79E-04
8.759	-1.67E-09	1.04E-06	-7.29E-05	2.86E-09	1.91E+04	4792.874	3.25E-04
8,828	-1.47E-09	-3.30E-06	-5.22E-05	2.85E-09	1.91E+04	4792.874	2.75E-04
	-1.28E-09			2.78E-09	1.91E+04	4792.874	2.29E-04
8.966	-1.09E-09	-8.29E-06	-2.05E-05	2.67E-09	1.91E+04	4792.874	1.86E-04
9.034	-9.09E-10	-9.34E-06	-8.9/E-U6	2.54E-09	1.91E+04	4792.874	1.48E-04
9.103	-7.38E-10	-9.69E-06	8.98E-08	2.41E-09	1.91E+04	4792.874	1.15E-04
	-5.77E-10		6.97E-06	2.27E-09	1.91E+04	4792.874	8.49E-05
9,241	-4.25E-10	-8.88E-06	1.19E-05	2.14E-09	1.91E+04	4792.874	5.92E-05
	-2.82E-10		1.53E-05	2.02E-09	1.91E+04	4792.874	3.70E-05
9.379	-1.47E-10	-6.91E-06	1.72E-05	1.91E-09	1.91E+04	4792.874	1.81E-05
	-1.84E-11		1.79E-05	1.82E-09	1.91E+04	4792.874	2.12E-06
9.517	1.04E-10	-4.56E-06	1.75E-05	1.74E-09	1.91E+04	4792.874	-1.12E-05
9.586		-3.44E-06	1.64E-05	1.69E-09	1.91E+04		-2.22E-05
9.655	3.37E-10	-2.41E-06	1.46E-05	1.64E-09	1.91E+04	4792.874	-3.09E-05
9.724		-1.54E-06	1.22E-05	1.62E-09	1.91E+04		-3.77E-05
9.793	5.60E-10	-8.36E-07	9.43E-06	1.60E-09	1.91E+04	4792.874	-4.25E-05
9.862		-3.39E-07	6.40E-06	1.59E-09	1.91E+04		-4.55E-05
9.931	7.79E-10	-5.82E-08	3.21E-06	1.59E-09	1.91E+04	4792.874	-4.68E-05
10.000	8.89E-10	0.0	0.0	1.59E-09	1.91E+04		-4.63E-05
_5.500	J.UJL 10	0.0	0.0	2.370 07	>IU-T	1.72.074	1.000 00

Please note that because this analysis makes computations of ultimate moment

capacity and pile response using nonlinear bending stiffness that the above values of total stress due to combined axial stress and bending may not be representative of actual conditions.

#### Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

```
Pile-head deflection = .03955380 m

Computed slope at pile head = -.03091492

Maximum bending moment = 109.560 kN- m

Maximum shear force = 330.000 kN

Depth of maximum bending moment = 1.17241379 m

Depth of maximum shear force = 0.000 m

Number of iterations = 34

Number of zero deflection points = 6
```

Summary of Pile-head Response

Definition of symbols for pile-head boundary conditions:

```
y = pile-head displacment, m
M = pile-head moment, kN- m
V = pile-head shear force, kN
S = pile-head slope, radians
```

R = rotational stiffness of pile-head, m- kN/rad

BC Type	Boundary Condition 1	Boundary Condition 2	Axial Load kN	Pile Head Deflection m	Maximum Moment m- kN	Maximum Shear kN
1	V = 330.000	M = -76.200	474.5000	.039554	109.5597	330.0000

```
LPILE Plus for Windows, Version 4.0 (4.0.8)
                 Analysis of Individual Piles and Drilled Shafts
                Subjected to Lateral Loading Using the p-y Method
                        (c) Copyright ENSOFT, Inc., 1985-2003
                                 All Rights Reserved
Path to file locations: L:\Programs\LPILE\Chapter 6\Ch. 6 Example with P=474.5\P=Pult\
Name of input data file: Down analysis.lpd
Name of output file: Down analysis.lpo
Name of plot output file: Down analysis.lpp
Name of runtime file: Down analysis.lpr
                            Time and Date of Analysis
                 Date: May 4, 2005 Time: 17: 4:52
                            Problem Title
Down Analysis for P=474.5 Case
                                    Program Options
Units Used in Computations - SI Units, meters, kilopascals
Basic Program Options:
Analysis Type 3:
- Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment
  Capacity with Pile Response Computed Using Nonlinear EI
Computation Options:
- User-specified p-y curves used in analysis
- Analysis uses p-y multiplers for group action

- Analysis assumes no shear resistance at pile tip

- Analysis for fixed-length pile or shaft only
- No computation of foundation stiffness matrix elements
- Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths
Solution Control Parameters:
- Number of pile increments
- Maximum number of iterations allowed = 2.5400E-07 m

Maximum allowable deflection = 2.5400E+00 m
- Maximum number of iterations allowed =
                                                           100
Printing Options:

    Values of pile-head deflection, bending moment, shear force, and soil reaction are printed for full length of pile.
    Printing Increment (spacing of output points) = 1

_____
                                         _____
                    Pile Structural Properties and Geometry
______
Pile Length
                                                         4.50 m
                                                         .00 m
Depth of ground surface below top of pile =
Slope angle of ground surface
Structural properties of pile defined using 2 points
                   Pile Moment of Pile Modulus of Diameter Inertia Area Elasticity m m**4 Sq. m kN/Sq. m
```

		.17780000				
moment cap that the a for any co	pacity and pabove values	nuse this analyile response of moment of other than to	using non inertia a	linear bendin and modulus o	g stiffness f are not us	
		Soil and Roc				
The soil p	profile is m	nodelled using	1 layers	3		
Distance f	from top of	using user-sp pile to top o pile to bottom	f laver	= .	000 m 000 m	
(Depth of	lowest laye	er extends	1.50 m be	elow pile tip	)	
	Ef	fective Unit	 Weight of	Soil vs. Dep	 th	
	ion of effect dusing 2 p	tive unit weigoints	ght of so:	il with depth		
Point No.	Depth X m	Eff. Unit   kN/ m*	Weight *3			
1 2		12.2000				
		Shear S		 F Soils		
	ion of shear sing 0 poir	strength para	ameters w	ith depth		
Point I	Depth X m	Cohesion c kN/ m**2	Angle of	Friction Deg.	E50 or k_rm	RQD % 
Notes:						
(2) Value (3) Defau	es of E50 an ult values w	rial compressine reported for ill be general reported only	r clay str ted for E!	rata. 50 when input	values are	0.
		р-у Mod	ification	Factors		
		nultipliers wi				
Point No.	Depth X			-mult	-	
1 2	.000	1.000	0	1.0000		
		 User-sp	ecified p			

User-specified p-y curves defined using 2 curves.

User-specified curve number 1 at depth = .000 m

Point	У	p,
No.	m	kN/ m
1	.0000	.000
2	.0001	263.064
3	.0002	312.838
4	.0006	393.373
5	.0011	467.802
6	.0017	517.708
7	.0023	556.313
8	.0057	699.527
9	.0115	831.882
10	.0229	989.280
11	.0258	989.280
12	.0286	989.280

User-specified curve number 2 at depth = 6.000 m

Point No.	Y m	p, kN/ m
1	.0000	.000
2	.0001	263.064
3	.0002	312.838
4	.0006	393.373
5	.0011	467.802
6	.0017	517.708
7	.0023	556.313
8	.0057	699.527
9	.0115	831.882
10	.0229	989.280
11	.0258	989.280
12	.0286	989.280

Loading Type

Static loading criteria was used for computation of p-y curves

Pile-head Loading and Pile-head Fixity Conditions

Number of loads specified = 1

Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1)

Shear force at pile head = 330.000 kNBending moment at pile head = 76.200 m- kNAxial load at pile head = 474.500 kN

Non-zero moment at pile head for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment) condition.

Output of p-y Curves at Specified Depths

p-y curves are generated and printed for verification at 2 depths.

Depth Depth Below Pile Head Depth Below Ground Surface No. m m

Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness

#### Pile Description:

The sectional shape is a circular shaft with steel casing.

Outside Diameter	=	.1778	m
Wall thickness of steel shell	=	.0115	m
Cross-sectional area of shell	=	.00601	m**2
Moment of inertia of steel shell	=	2.08692E-05	m**4

#### Material Properties:

Compressive Strength of Concrete Yield Stress of Reinforcement Steel shell or core yield stress	= = =	27600.000 0. 552000.	kN/ m**2 kN/ m**2 kN/ m**2
Modulus of Elasticity of Reinforcement Cover Thickness (edge to bar center)		200000000.	kN/ m**2 m
Number of Reinforcing Bars Area of Single Bar Number of Rows of Reinforcing Bars Ultimate Axial Squash Load Capacity	= = =	10 .00000 5 3758.02	m**2

Distribution and Area of Steel Reinforcement

Row Number	Area of Reinforcement m**2	Distance to Centroidal Axis m
1	.000000	.0736
2	.000000	.0455
3	.000000	.0000
4	.000000	0455
5	.000000	0736

Axial Thrust Force = 474.50 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
1.69826245	4792.874	.00035433	.00031727	.90691267
2.45303965	4792.862	.00051181	.00032949	.65527803
3.20781175	4792.848	.00066929	.00034172	.52206775
3.96257836	4792.833	.00082677	.00035395	.43960844
4.71733626	4792.814	.00098425	.00036619	.38354674
5.47208598	4792.792	.00114173	.00037843	.34295465
6.22682760	4792.770	.00129921	.00039068	.31220536
6.98155916	4792.746	.00145669	.00040293	.28810838
7.73628058	4792.720	.00161417	.00041519	.26871577
8.49098340	4792.688	.00177165	.00042746	.25277953
9.24568013	4792.659	.00192913	.00043973	.23944236
10.000	4792.625	.00208661	.00045201	.22812367
10.755	4792.590	.00224409	.00046429	.21839481
11.510	4792.551	.00240157	.00047658	.20994649
12.264	4792.509	.00255906	.00048888	.20253996
13.019	4792.470	.00271654	.00050118	.19599075
13.774	4792.426	.00287402	.00051348	.19016320
14.528	4792.379	.00303150	.00052579	.18494336
15.283	4792.326	.00318898	.00053812	.18024442
16.035	4791.716	.00334646	.00055042	.17597957
16.774	4787.090	.00350394	.00056260	.17206198
17.571	4799.091	.00366142	.00057505	.16855677
18.301	4792.220	.00381890	.00058745	.16532828
19.053	4791.556	.00397638	.00059979	.16233854
24.610	4771.704	.00515748	.00068957	.14520315
29.767	4696.101	.00633858	.00078032	.13460612
35.334	4698.840	.00751969	.00087092	.12731897
39.786	4572.710	.00870079	.00095706	.12149685
45.804	4635.195	.00988189	.00105014	.11776917
50.555	4569.762	.01106299	.00113526	.11411745

```
.01224409
                                        .00122769
                                                      .11176798
 56.180
             4588.341
 61.386
             4572.465
                          .01342520
                                        .00131523
                                                      .10946735
                         .01460630
 64.845
            4439.494
                                       .00139171
                                                      .10678147
 71.647
            4538.208
                         .01578740
                                        .00149414
                                                      .10614120
                                                      .10380800
 74.736
            4404.370
                         .01696850
                                       .00156633
 81.890
            4511.946
                          .01814961
                                        .00167053
                                                      .10354213
            4434.167
                                                      .10206082
 85.716
                         .01933071
                                       .00175060
 92.018
            4486.089
                         .02051181
                                        .00183074
                                                      .10075315
            4477.213
 97.124
                         .02169291
                                       .00193616
                                                      .10075315
102.139
            4465.294
                          .02287402
                                        .00202929
                                                      .10021598
            4377.229
105.295
                         .02405512
                                       .00210249
                                                      .09890288
109.026
            4320.217
                         .02523622
                                        .00218134
                                                      .09793705
113.742
            4305.584
                         .02641732
                                        .00227957
                                                      .09779054
118.611
            4297.758
                          .02759843
                                        .00238148
                                                      .09779054
                          .02877953
127.233
            4420.944
                                        .00247762
                                                      .09758978
                          .02996063
131.954
            4404.252
                                        .00257166
                                                      .09733476
            4377.388
                          .03114173
                                                      .09715027
136.319
                                        .00266730
            4339.870
                          .03232283
140.277
                                        .00276706
                                                      .09710686
                          .03350394
                                                      .09719911
143.850
            4293.538
                                        .00287126
                          .03468504
                                                      .09737816
147.136
            4242.066
                                        .00297869
                          .03586614
                                        .00308557
                                                      .09753009
150.123
            4185.651
                         .03704724
                                        .00319502
                                                      .09774171
152.748
            4123.053
                          .03822835
                                        .00329874
                                                      .09779054
152.748
            3995.667
                          .03940945
                                                      .09779054
152.748
            3875.917
                                        .00340066
                                                      .09779054
154.387
             3803.521
                          .04059055
                                        .00350258
                                                      .09779054
             3733.787
                          .04177165
155.966
                                       .00360450
                                                      .09779054
157.340
             3663.103
                          .04295276
                                        .00370642
158.551
             3592.498
                          .04413386
                                        .00380833
                                                      .09779054
```

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 147.732 m- kN

p-y Curve Computed by Interpolation from User-input Curves

```
Soil Layer Number = 1
Depth below ground surface = .000 m
Depth below pile head = .000 m
p-multiplier = 1.00000
y-multiplier = 1.00000
```

y, m	p, kN/m
y, m .0000 .0010 .0011 .0022 .0033 .0044 .0056 .0067	p, kN/ m  .000 452.916 468.738 551.327 599.856 646.664 693.472 721.605 746.964
.0089 .0100 .0111 .0122 .0133 .0356 .0667	772.322 797.681 823.039 841.875 857.218 989.280 989.280 989.280

p-y Curve Computed by Interpolation from User-input Curves

Soil Layer Number = 1
Depth below ground surface = 4.500 m
Depth below pile head = 4.500 m
p-multiplier = 1.00000
y-multiplier = 1.00000

y, m	p, kN/m
.0000	.000
.0010	452.916
.0011	468.738
.0022	551.327
.0033	599.856
.0044	646.664
.0056	693.472
.0067	721.605

```
746.964
772.322
.0078
.0089
.0100
               797.681
.0111
               823.039
.0122
              841.875
.0133
               857.218
.0356
               989.280
.0667
               989.280
.0889
              989.280
```

Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 1

Pile-head boundary conditions are Shear and Moment (BC Type 1) Specified shear force at pile head = 330.000 kN Specified bending moment at pile head = 76.200 m- kN Specified axial load at pile head = 474.500 kN

Non-zero moment for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment ) condition.

the appri	red bire-ne	ad Ioading	, Dut IS I	iot a liee-	neau (Zer	J MOMETIC / C	ondiction.
Depth X	Deflect. Y	Moment M	Shear V	Slope S	Total Stress	Flx. Rig. EI	Soil Res p
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
0.000	.014998	76.2000	330.0	029550	1.91E+04	4440.259	-880.191
.03103	.014089	86.4487	302.9	028982	1.91E+04	4440.259	-867.643
.06207	.013199	95.8529	276.1	028344	1.91E+04	4440.259	-855.355
.09310	.012330	104.4	249.8	027641	1.91E+04	4402.137	-843.353
.124	.011484	112.2	223.8	026869 026036	1.91E+04	4310.471	-831.519
.155	.010662 .009868	119.1 125.2	198.3 173.3	025165	1.91E+04 1.91E+04	4304.934 4392.860	-812.777 -794.642
.217	.009100	130.6	148.9	024263	1.91E+04	4409.035	-777.134
.248	.008362	135.2	125.1	023324	1.91E+04	4384.290	-760.277
.279	.007653	139.1	101.7	022350	1.91E+04	4351.532	-744.098
.310	.006975	142.2	78.8937	021343	1.91E+04	4315.407	-728.621
.341	.006328	144.6	56.5102	020308	1.91E+04	4282.247	-713.869
.372	.005714	146.3	34.5731	019250	1.91E+04	4255.618	-699.859
.403	.005133	147.3	13.2288	018178	1.91E+04	4239.142	-675.661
.434	.004586	147.6	-7.3822	017097	1.91E+04	4232.741	-652.603
.466	.004072	147.3	-27.2996	016017	1.91E+04	4238.305	-630.961
.497	.003592	146.4	-46.5672	014943	1.91E+04	4253.508	-610.730
.528	.003144	144.9	-65.2286	013883	1.91E+04	4277.471	-591.895
.559	.002730	142.8	-83.3268	012843	1.91E+04	4307.612	-574.434
.590 .621	.002347 .001996	140.1 136.9	-100.9 -117.9	011828 010842	1.91E+04 1.91E+04	4341.609 4372.296	-558.318 -536.749
.652	.001556	133.1	-134.2	009887	1.91E+04	4397.257	-515.586
.683	.001374	128.8	-149.8	008964	1.91E+04	4415.342	-491.280
.714	.001118	124.1	-164.8	008072	1.91E+04	4376.125	-469.311
.745	8.81E-04	118.8	-178.8	007203	1.91E+04	4300.982	-435.230
.776	6.71E-04	113.2	-191.8	006366	1.91E+04	4307.350	-403.939
.807	4.86E-04	107.1	-203.8	005577	1.91E+04	4349.681	-370.427
.838	3.25E-04	100.7	-214.8	004845	1.91E+04	4468.752	-337.979
.869	1.85E-04	93.9248	-224.8	004170	1.91E+04	4482.780	-305.510
.900	6.59E-05	86.8575	-232.2	003542	1.91E+04	4443.643	-173.263
.931	-3.46E-05	79.6145	-233.5	002963	1.91E+04	4478.130	91.121
.962	-1.18E-04 -1.86E-04	72.4510 65.5422	-227.9 -218.9	002437 001959	1.91E+04 1.91E+04	4504.740 4449.767	271.981 305.793
.993	-2.40E-04	58.9212	-218.9	001531	1.91E+04 1.91E+04	4579.999	320.786
	-2.81E-04	52.6032	-199.1	001331	1.91E+04	4576.541	329.109
	-3.11E-04	46.5970	-188.8	-8.18E-04	1.91E+04	4624.438	335.201
	-3.32E-04	40.9090	-178.3	-5.23E-04	1.91E+04	4584.479	339.339
1.148	-3.44E-04	35.5438	-167.8	-2.67E-04	1.91E+04	4693.099	341.745
1.179	-3.48E-04	30.5042	-157.1	-4.89E-05	1.91E+04	4696.464	342.682
1.210	-3.47E-04	25.7917	-146.5	1.36E-04	1.91E+04	4754.616	342.359
	-3.40E-04	21.4065	-135.9	2.90E-04	1.91E+04	4783.170	340.984
	-3.29E-04	17.3477	-125.4	4.15E-04	1.91E+04	4795.724	338.741
	-3.14E-04	13.6134	-114.9	5.15E-04	1.91E+04	4792.435	335.796
	-2.97E-04 -2.77E-04	10.2013	-104.5	5.93E-04	1.91E+04	4792.615	332.301
	-2.7/E-04 -2.56E-04	7.1083 4.3309	-94.2721 -84.1457	6.49E-04 6.86E-04	1.91E+04 1.91E+04	4792.742 4792.823	328.392 324.196
	-2.35E-04	1.8653	-74.1523	7.06E-04	1.91E+04	4792.823	319.825
	-2.13E-04	2925	-64.2957	7.11E-04	1.91E+04	4792.874	315.378
	-1.91E-04	-2.1464	-54.6200	7.03E-04	1.91E+04	4792.867	308.163
	-1.69E-04	-3.7034	-45.2231	6.84E-04	1.91E+04	4792.838	297.413

1.552	-1.48E-04	-4.9735	-36.1541	6.56E-04	1.91E+04	4792.806	287.034
1.583	-1.28E-04	-5.9668	-27.3995	6.20E-04	1.91E+04	4792.778	277.152
1 614	-1.10E-04	-6.6925	-18.9423	5.79E-04	1.91E+04	4792.755	267.867
		-7.1596					
	-9.23E-05		-11.0162	5.35E-04	1.91E+04	4792.740	242.930
1.676	-7.65E-05	-7.3920	-4.1248	4.87E-04	1.91E+04	4792.732	201.179
1.707	-6.21E-05	-7.4299	1.5314	4.39E-04	1.91E+04	4792.731	163.335
	-4.92E-05	-7.3099	6.0742	3.92E-04	1.91E+04	4792.735	129.420
1.769	-3.78E-05	-7.0645	9.6244	3.45E-04	1.91E+04	4792.743	99.369
1.800	-2.78E-05	-6.7227	12.2999	3.01E-04	1.91E+04	4792.754	73.052
	-1.91E-05	-6.3099	14.2138	2.58E-04	1.91E+04	4792.768	50.289
1.862	-1.17E-05	-5.8480	15.4730	2.19E-04	1.91E+04	4792.781	30.862
1.893	-5.52E-06	-5.3559	16.1773	1.83E-04	1.91E+04	4792.796	14.526
1 924	-3.89E-07	-4.8493	16.4186	1.50E-04	1.91E+04	4792.810	1.022
1.955	3.77E-06	-4.3412	16.2805	1.20E-04	1.91E+04	4792.823	-9.919
1.986	7.06E-06	-3.8423	15.8386	9.35E-05	1.91E+04	4792.835	-18.564
2.017	9.57E-06	-3.3609	15.1598	7.01E-05	1.91E+04	4792.845	-25.179
2.048	1.14E-05	-2.9034	14.3033	4.99E-05	1.91E+04	4792.854	-30.017
2.079	1.27E-05	-2.4746	13.3205	3.24E-05	1.91E+04	4792.862	-33.320
2.110	1.34E-05	-2.0776	12.2555	1.77E-05	1.91E+04	4792.868	-35.314
2.141	1.38E-05	-1.7144	11.1456	5.43E-06	1.91E+04	4792.874	-36.211
2.172	1.38E-05	-1.3860		-4.61E-06	1.91E+04	4792.874	-36.201
2.203	1.35E-05	-1.0922	8.9100	-1.26E-05	1.91E+04	4792.874	-35.459
2.234	1.30E-05	8326	7.8301	-1.89E-05	1.91E+04	4792.874	-34.139
2.266	1.23E-05	6057		-2.35E-05	1.91E+04	4792.874	-32.379
2.297	1.15E-05	4099		-2.68E-05	1.91E+04	4792.874	-30.299
2.328	1.06E-05	2433	4.9207	-2.89E-05	1.91E+04	4792.874	-28.002
2.359	9.72E-06	1037	4 0893	-3.00E-05	1.91E+04	4792.874	-25.576
2.390	8.78E-06	1.14E-02		-3.03E-05	1.91E+04	4792.874	-23.096
2.421	7.84E-06	.1042	2.6556	-3.00E-05	1.91E+04	4792.874	-20.622
2.452	6.92E-06	.1771	2.0532	-2.91E-05	1.91E+04	4792.874	-18.202
		.2325					
2.483	6.04E-06			-2.77E-05	1.91E+04	4792.874	-15.877
2.514	5.20E-06	.2725	1.0658	-2.61E-05	1.91E+04	4792.874	-13.674
2.545	4.42E-06	.2994	.6734	-2.42E-05	1.91E+04	4792.874	-11.615
2.576	3.69E-06	.3150		-2.23E-05	1.91E+04	4792.874	-9.715
2.607	3.03E-06	.3213		-2.02E-05	1.91E+04	4792.874	-7.981
2.638	2.44E-06	.3198	1556	-1.81E-05	1.91E+04	4792.874	-6.417
2.669	1.91E-06	.3122	3331	-1.61E-05	1.91E+04	4792.874	-5.022
2.700	1.44E-06	.2996		-1.41E-05	1.91E+04	4792.874	-3.792
2.731	1.03E-06	.2834	5710	-1.22E-05	1.91E+04	4792.874	-2.721
2.762	6.84E-07	.2646	6411	-1.04E-05	1.91E+04	4792.874	-1.799
2.793	3.87E-07	.2439		-8.79E-06	1.91E+04	4792.874	-1.018
2.824	1.39E-07	.2223	7063	-7.28E-06	1.91E+04	4792.874	364770
2.855	-6.48E-08	.2003	7093	-5.91E-06	1.91E+04	4792.874	.170530
2.886	-2.28E-07	.1785	6973	-4.68E-06	1.91E+04	4792.874	.599935
	-3.55E-07	.1572		-3.60E-06	1.91E+04	4792.874	.934996
2.948	-4.51E-07	.1368	6406	-2.64E-06	1.91E+04	4792.874	1.187
2.979	-5.20E-07	.1175	6010	-1.82E-06	1.91E+04	4792.874	1.367
	-5.64E-07	9.95E-02		-1.12E-06	1.91E+04	4792.874	1.484
	-5.89E-07	8.30E-02		-5.27E-07	1.91E+04	4792.874	1.549
3.072	-5.97E-07	6.79E-02	4612	-3.85E-08	1.91E+04	4792.874	1.570
3.103	-5.91E-07	5.43E-02	4127	3.57E-07	1.91E+04	4792.874	1.555
	-5.75E-07	4.23E-02	3651	6.70E-07	1.91E+04	4792.874	1.512
	-5.50E-07	3.17E-02	3192	9.09E-07	1.91E+04	4792.874	1.446
3.197	-5.18E-07	2.24E-02	2757	1.08E-06	1.91E+04	4792.874	1.363
3.228	-4.82E-07	1.45E-02	2348	1.20E-06	1.91E+04	4792.874	1.269
	-4.44E-07			1.28E-06	1.91E+04		
	-4.03E-07	2.25E-03	1625	1.31E-06	1.91E+04	4792.874	1.060
	-3.62E-07		1312	1.31E-06	1.91E+04	4792.874	.952991
3.352	-3.22E-07	-5.93E-03	1033	1.28E-06	1.91E+04	4792.874	.846726
	-2.83E-07			1.23E-06	1.91E+04	4792.874	.743596
	-2.45E-07			1.17E-06	1.91E+04	4792.874	.645089
	-2.10E-07	-1.23E-02		1.10E-06	1.91E+04	4792.874	.552316
3.476				1 010 00		4792.874	.466057
	-1.77E-07	-1.33E-02	-2.27E-02	I.UIE-06	1.91E+04		
3 507	-1.77E-07			1.01E-06	1.91E+04		
	-1.47E-07	-1.38E-02	-9.44E-03	9.26E-07	1.91E+04	4792.874	.386811
3.538	-1.47E-07 -1.20E-07	-1.38E-02 -1.39E-02	-9.44E-03 1.45E-03	9.26E-07 8.37E-07	1.91E+04 1.91E+04	4792.874 4792.874	.386811 .314838
3.538	-1.47E-07	-1.38E-02 -1.39E-02	-9.44E-03	9.26E-07	1.91E+04	4792.874	.386811
3.538 3.569	-1.47E-07 -1.20E-07 -9.51E-08	-1.38E-02 -1.39E-02 -1.37E-02	-9.44E-03 1.45E-03 1.02E-02	9.26E-07 8.37E-07 7.47E-07	1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874	.386811 .314838 .250203
3.538 3.569 3.600	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806
3.538 3.569 3.600 3.631	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423
3.538 3.569 3.600 3.631 3.662	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729
3.538 3.569 3.600 3.631 3.662	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423
3.538 3.569 3.600 3.631 3.662 3.693	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326
3.538 3.569 3.600 3.631 3.662 3.693 3.724	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08 -1.13E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765
3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08 -1.13E-08 -1.36E-09	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02 3.04E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07 2.91E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765
3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755 3.786	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09	-1.38E-02 -1.39E-02 -1.37E-02 -1.37E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03 -8.26E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02 3.04E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07 2.91E-07 2.35E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 017769
3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02 3.04E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07 2.91E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765
3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755 3.786 3.817	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09 1.32E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03 -8.26E-03 -7.33E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02 3.04E-02 3.02E-02 2.94E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07 2.91E-07 2.35E-07 1.84E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 -017769 034735
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3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755 3.786 3.817 3.848 3.879	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -3.75E-08 -1.13E-08 -1.13E-09 6.75E-09 1.32E-08 1.82E-08 2.44E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.11E-02 -1.01E-02 -9.20E-03 -8.26E-03 -7.33E-03 -5.59E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 2.99E-02 3.04E-02 3.02E-02 2.94E-02 2.81E-02 2.65E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 3.54E-07 2.91E-07 2.35E-07 1.39E-07 1.01E-07	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 -017769 -034735 -047825 -057509
3.538 3.569 3.600 3.631 3.662 3.724 3.755 3.786 3.817 3.848 3.879 3.9910 3.941	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09 1.32E-08 1.82E-08 2.19E-08 2.44E-08 2.60E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.37E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03 -8.26E-03 -7.33E-03 -6.44E-03 -5.59E-03 -4.80E-03 -4.07E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.99E-02 3.04E-02 3.02E-02 2.94E-02 2.81E-02 2.65E-02 2.46E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 3.54E-07 2.91E-07 2.35E-07 1.84E-07 1.39E-07 6.69E-08 3.82E-08	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 -017769 -034735 -047825 -057509 -064237 -068428
3.538 3.569 3.600 3.631 3.662 3.693 3.724 3.755 3.786 3.817 3.848 3.879 3.910	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -3.75E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09 1.32E-08 1.82E-08 2.19E-08 2.44E-08 2.60E-08 2.68E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.33E-02 -1.27E-02 -1.19E-02 -1.11E-02 -9.20E-03 -8.26E-03 -7.33E-03 -6.44E-03 -5.59E-03 -4.80E-03 -4.07E-03 -3.40E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.99E-02 3.04E-02 3.02E-02 2.94E-02 2.81E-02 2.66E-02 2.26E-02 2.04E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 4.22E-07 3.54E-07 2.35E-07 1.84E-07 1.39E-07 1.01E-07 6.69E-08 3.82E-08 1.40E-08	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 -017769 -034735 -047825 -057509 -064237 -068428 -070469
3.538 3.569 3.600 3.631 3.662 3.724 3.755 3.786 3.817 3.848 3.879 3.9910 3.941	-1.47E-07 -1.20E-07 -9.51E-08 -7.33E-08 -5.41E-08 -2.33E-08 -1.13E-08 -1.36E-09 6.75E-09 1.32E-08 1.82E-08 2.19E-08 2.44E-08 2.66E-08 2.68E-08 2.69E-08	-1.38E-02 -1.39E-02 -1.37E-02 -1.37E-02 -1.27E-02 -1.19E-02 -1.11E-02 -1.01E-02 -9.20E-03 -8.26E-03 -7.33E-03 -6.44E-03 -5.59E-03 -4.80E-03 -4.07E-03	-9.44E-03 1.45E-03 1.02E-02 1.71E-02 2.23E-02 2.60E-02 2.85E-02 3.04E-02 3.02E-02 2.94E-02 2.65E-02 2.46E-02 2.26E-02 2.04E-02 1.82E-02	9.26E-07 8.37E-07 7.47E-07 6.60E-07 5.76E-07 4.97E-07 3.54E-07 2.91E-07 2.35E-07 1.84E-07 1.39E-07 6.69E-08 3.82E-08	1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04 1.91E+04	4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874 4792.874	.386811 .314838 .250203 .192806 .142423 .098729 .061326 .029765 .003565 -017769 -034735 -047825 -057509 -064237 -068428

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4.066 2.55E-08 -1.81E-03 1.39E-02 -3.57E-08 1.91E+04 4792.874 -.067036
4.097 2.42E-08 -1.41E-03 1.19E-02 -4.61E-08 1.91E+04 4792.874 -.063644
4.128 2.26E-08 -1.07E-03 9.97E-03 -5.41E-08 1.91E+04 4792.874 -.059508
4.159 2.08E-08 -7.85E-04 8.20E-03 -6.01E-08 1.91E+04 4792.874 -.059508
4.190 1.89E-08 -5.56E-04 6.58E-03 -6.45E-08 1.91E+04 4792.874 -.049693
4.221 1.68E-08 -3.75E-04 5.12E-03 -6.75E-08 1.91E+04 4792.874 -.049693
4.221 1.68E-08 -2.37E-04 5.12E-03 -6.75E-08 1.91E+04 4792.874 -.04283
4.252 1.47E-08 -2.37E-04 3.83E-03 -6.95E-08 1.91E+04 4792.874 -.038676
4.283 1.25E-08 -1.35E-04 2.72E-03 -7.07E-08 1.91E+04 4792.874 -.032943
4.314 1.03E-08 -6.58E-05 1.79E-03 -7.13E-08 1.91E+04 4792.874 -.027138
4.345 8.10E-09 -2.23E-05 1.04E-03 -7.16E-08 1.91E+04 4792.874 -.021299
4.376 5.87E-09 6.32E-07 4.66E-04 -7.17E-08 1.91E+04 4792.874 -.015448
4.407 3.65E-09 8.71E-06 7.74E-05 -7.16E-08 1.91E+04 4792.874 -.009597
4.438 1.43E-09 7.55E-06 -1.30E-04 -7.15E-08 1.91E+04 4792.874 -.009597
4.438 1.43E-09 7.55E-06 -1.30E-04 -7.15E-08 1.91E+04 4792.874 -.009791
4.500 -3.01E-09 0.0 0.0 -7.15E-08 1.91E+04 4792.874 .002091
```

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of total stress due to combined axial stress and bending may not be representative of actual conditions.

Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

```
Summary of Pile-head Response
```

Definition of symbols for pile-head boundary conditions:

```
y = pile-head displacment, m
M = pile-head moment, kN- m
V = pile-head shear force, kN
S = pile-head slope, radians
R = rotational stiffness of pile-head, m- kN/rad
```

BC	Boundary	Boundary	Axial	Pile Head	Maximum	Maximum
Type	Condition	Condition	Load	Deflection	Moment	Shear
	1	2	kN	m	m- kN	kN
1	V = 330.000	M = 76.200	474.5000	.014998	147.6397	330.0000

# **APPENDIX C**

# **Micropile Guide Construction Specification**

[Foundation Support Projects]
Contractor Design/Build of Micropiles
Metric (SI) Units
(With Commentary)

(Commentary: Owner-Controlled design specifications can vary in the amount of the design to be performed by the Owner's design engineer and the amount performed by the micropile specialty Contractor. This guide specification is set up for the Owner-controlled design (Standard Design) method wherein the Owner provides preliminary plans showing the pile design loadings, footing design, and pile layout for each footing location. The Owner also provides related design criteria and requirements, subsurface data, rights-of-way limits, utility locations, site limitations, construction material and testing specifications, and required Contractor working drawing/design and construction submittals and review requirements. The micropile Contractor designs the individual micropile elements and pile top footing connections and selects the micropile construction process and equipment. This approach is very similar to that commonly used by many highway agencies for Owner design of permanent tieback and permanent soil nail walls. During the bidding process, the micropile contractors prepare a preliminary micropile design and a firm cost proposal based on the Owner's preliminary plans and specifications. If the micropile portion of the project is to be subcontracted, general contractors will receive bids from the micropile contractors and include the best offer and name of the selected micropile contractor in their bid submittal. Once the contract is awarded, the selected micropile Contractor prepares detailed micropile design calculations and working drawings and submits them to the Engineer for review. After acceptance of the design, construction begins.)

### 1.0 DESCRIPTION

This work shall consist of constructing micropiles as shown on the contract plans and approved working drawings and as specified herein. The micropile specialty Contractor is responsible for furnishing of all design, materials, products, accessories, tools, equipment, services, transportation, labor and supervision, and manufacturing techniques required for design, installation and testing of micropiles and pile top attachments for this project.

The selected micropile Contractor shall select the micropile type, size, pile top attachment, installation means and methods, estimate the ground-grout bond value and determine the required bond length and final micropile diameter. The micropile Contractor shall design and install micropiles that will develop the load capacities indicated on the contract plans. The micropile load capacities shall be verified by verification and proof load testing as required and must meet the test acceptance criteria specified herein.

Where the imperative mood is used within this specification, "The Contractor shall" is implied.

(Commentary: Successful design and installation of high-quality micropiles require experienced Contractors having the necessary specialty drilling and grouting equipment and expertise and experienced work crews. The most important section of the specifications to be enforced by the Owner deals with the experience qualifications of the micropile Contractor. Failure to enforce the specified experience qualifications opens the door for inexperienced Contractors trying to cut costs. The results often are inferior workmanship, project delays, and project claims that, more often than not, substantially increase project costs. Results like these often discourage project Owners from implementing new technology, and draws them back to more traditional methods at any cost. This can be avoided with the proper specification implementation and, as importantly, enforcement to ensure a mutually successful project.)

### 1.1 Micropile Contractor's Experience Requirements And Submittal.

The micropile Contractor shall be experienced in the construction and load testing of micropiles and have successfully constructed at least 5 projects in the last 5 years involving construction totaling at least 100 micropiles of similar capacity to those required in these plans and specifications.

The Contractor shall have previous micropile drilling and grouting experience in soil/rock similar to project conditions. The Contractor shall submit construction details, structural details and load test results for at least three previous successful micropile load tests from different projects of similar scope to this project.

The Contractor shall assign an Engineer to supervise the work with experience on at least 3 projects of similar scope to this project completed over the past 5 years. The Contractor shall not use consultants or manufacturers' representatives to satisfy the supervising Engineer requirements of this section. The on-site foremen and drill rig operators shall also have

experience on at least 3 projects over the past 5 years installing micropiles of equal or greater capacity than required in these plans and specifications.

The micropiles shall be designed by a Registered Professional Engineer with experience in the design of at least 3 successfully completed micropile projects over the past 5 years, with micropiles of similar capacity to those required in these plans and specifications. The micropile design engineer may be either an employee of the Contractor or a separate Consultant design engineer meeting the stated experience requirements. (*Commentary: If the Owner prepares a fully detailed design, this paragraph can be deleted*).

At least 45 calendar days before the planned start of micropile construction, the Contractor shall submit 5 copies of the completed project reference list and a personnel list. The project reference list shall include a brief project description with the owner's name and current phone number and load test reports. The personnel list shall identify the micropile system design engineer (if applicable), supervising project Engineer, drill rig operators, and on-site foremen to be assigned to the project. The personnel list shall contain a summary of each individual's experience and be complete enough for the Engineer to determine whether each individual satisfies the required qualifications. The Engineer will approve or reject the Contractor's qualifications within 15 calendar days after receipt of a complete submission. Additional time required due to incomplete or unacceptable submittals will not be cause for time extension or impact or delay claims. All costs associated with incomplete or unacceptable submittals shall be borne by the Contractor.

Work shall not be started, nor materials ordered, until the Engineer's written approval of the Contractor's experience qualifications is given. The Engineer may suspend the Work if the Contractor uses non-approved personnel. If work is suspended, the Contractor shall be fully liable for all resulting costs and no adjustment in contract time will result from the suspension.

## 1.2 Related Specifications

(Commentary: Engineer to specify all related specifications.)

### 1.3 Definitions

(Commentary: Engineer to specify any additional definitions.)

**Admixture:** Substance added to the grout to control bleed and/or shrinkage, improve flowability, reduce water content, or retard setting time.

- **Alignment Load (AL):** A minimum initial load (no greater than 10 percent of the Design Load) applied to micropile during testing to keep the testing equipment correctly positioned.
- **Bond Length:** The length of the micropile that is bonded to the ground and used to transfer the applied axial loads to the surrounding soil or rock.
- **Bond-breaker:** A sleeve placed over the steel reinforcement to prevent load transfer.
- **Casing:** Steel tube introduced during the drilling process in overburden soil to temporarily stabilize the drill hole. This is usually withdrawn as the pile is grouted, although in certain types of micropiles, some casing is permanently left in place to provide added pile reinforcement.
- **Centralizer:** A device to support and position the reinforcing steel in the drill hole and/or casing so that a minimum grout cover is provided.
- **Contractor:** The person/firm responsible for performing the micropile work.
- **Coupler:** The means by which load capacity can be transmitted from one partial length of reinforcement to another.
- **Creep Movement:** The movement that occurs during the creep test of a micropile under a constant load.
- **Design Load (DL):** The maximum load expected to be applied to the micropile during its service life.
- **Encapsulation:** A corrugated or deformed tube protecting the reinforcing steel against corrosion.
- **Engineer:** The Owner or Owner's authorized agent.
- **Free (unbonded) length:** The designed length of the micropile that is not bonded to the surrounding ground or grout.
- **Micropile:** A small-diameter, bored, cast-in-place composite pile, in which the applied load is resisted by steel reinforcement, cement grout and frictional grout/ground bond.
- **Maximum Test Load:** The maximum load to which the micropile is subjected during testing.
- **Ultimate Grout-to-Ground Bond Values:** The estimated ultimate geotechnical unit grout-to-ground bond strength selected for use in design.
- **Overburden:** Material, natural or placed, that may require cased drilling methods to provide an open borehole to underlying strata.
- **Post-grouting:** The injection of additional grout into the load transfer length of a micropile after the primary grout has set. Also known as regrouting or secondary grouting.
- **Primary Grout:** Portland-cement-based grout injected into the micropile hole prior to or after the installation of the reinforcement to direct the load transfer to the surrounding ground along the micropile.

**Proof Load Test:** Incremental loading of a production micropile, recording the total movement at each increment.

**Reinforcement:** The steel component of the micropile that accepts and/or resists applied loadings.

**Sheathing:** Smooth or corrugated piping or tubing that protects the reinforcing steel against corrosion.

**Spacer:** A device to separate elements of a multiple-element reinforcement.

**Verification Load Test:** Pile load test performed to verify the design of the pile system and the construction methods proposed, prior to installation of production piles.

### 1.4 Referenced Codes and Standards.

The following publications form a part of this specification to the extent indicated by the references. The latest publication as of the issue date of this specification shall govern, unless indicated otherwise.

1.4.1 American Society for Testing and Materials (ASTM)

American Association of State Highway and Transportation Officials (AASHTO)

ASTM	AASHTO	SPECIFICATION / TEST
A36, A572	M183, M223	Structural Steel
A82	M55	Cold-Drawn Steel Wire for Concrete Reinforcement
A252	_	Welded and Seamless Steel Pipe Piles
A615	M31	Deformed and Plain Billet Steel Bars for Concrete Reinforcement
A722	M275	Uncoated High-Strength Steel Bar for Prestressing Concrete
A775	_	Epoxy -Coated Reinforcing Steel Bars
A934	_	Epoxy-Coated Prefabricated Steel Reinforcing Bars
	I	
C 33	M80	Concrete Aggregates
C 109	T106	Compressive Strength of Hydraulic Cement Mortar
C 188	T133	Density of Hydraulic Cement
C 144	M45	Aggregate for Masonry Mortar
C 150	M 85	Portland Cement
C 494	M194	Chemical Admixtures for Concrete
	I	
D 1143	_	Method of Testing Piles Under Static Axial Compressive Load
D 1784	_	Polyvinyl Chloride (PVC) Pipe (Class 13464-B)
D 3350	M 252	Polyethylene Corrugated Tubing
D 3689	_	Method of Testing Individual Piles Under Static Axial Tensile Load
D 3966		Standard Test Method for Piles Under Lateral Load
_	T 26	Quality of Water to be Used in Concrete

- 1.4.2 American Welding Society (AWS)
  - D1.1 Structural Welding Code-Steel
  - D1.2 Structural Welding Code-Reinforcing Steel
- 1.4.3 American Petroleum Institute (API)

5CT (N-80) Specification for casing and tubing

RP 13B-1 Recommended Practice – Standard Procedure for Field Testing Water Based Drilling Fluids

### 1.5 Available Information.

Available information developed by the Owner, or	or by the Owner's duly	authorized
representative include the following items:		

1.	Plans prepared by	, dated	_·	
2.	Geotechnical Report No.(s)	titled	dated	

(Commentary: The subsurface conditions expected can significantly impact the contractor's choice of procedures, methods, or equipment, the bidding process, and contract administration. Experience has proven that use of a geotechnical summary is advantageous toward achieving a successful contract. It is recommended that advisory wording be inserted into the contract special provisions to "red flag" the conditions to bidders. Such a summary may become part of the contract special provisions, making it a legal part of the contract documents. The purpose is to alert and be fair to bidders, and thus prevent/minimize differing site condition construction claims and dispute.)

## 1.6 Construction Site Survey

Before bidding the Work, the Contractor shall review the available subsurface information and visit the site to assess the site geometry, equipment access conditions, and location of existing structures and above ground facilities.

The Contractor is responsible for field locating and verifying the location of all utilities shown on the plans prior to starting the Work. Maintain uninterrupted service for those utilities designated to remain in service throughout the Work. Notify the Engineer of any utility locations different from shown on the plans that may require micropile relocations or structure design modification. Subject to the Engineer's approval, additional cost to the Contractor due to micropile relocations and/or structure design modification resulting from utility locations different from shown on the plans, will be paid as Extra Work.

(Commentary: The location of both active and abandoned buried utilities within the ground mass to receive micropiles can have a profound impact on the design and construction of the

micropiles. Careful consideration of the presence and location of all utilities is required for successful design and installation of micropiles.)

Prior to start of any micropile construction activity, the Contractor and Engineer shall jointly inspect the site to observe and document the pre-construction condition of the site, existing structures and facilities.

# 1.7 Micropile Design Requirements.

The micropiles shall be designed to meet the specified loading conditions, as shown on the contract plans and approved working drawings. Design the micropiles and pile top to footing connections using the procedures contained in the FHWA "Micropile Design and Construction", Report No. FHWA NHI-05-039.

The required geotechnical factors of safety shall be in accord with the FHWA manual, unless specified otherwise. Estimated soil/rock design shear strength parameters, unit weights, applied foundation loadings, slope and external surcharge loads, corrosion protection requirements, known utility locations, easements, right-of-ways and other applicable design criteria will be as shown on the plans or specified herein.

Structural design of any individual micropile structure elements not covered in the FHWA manual shall be by the service load design method in conformance with appropriate articles of the most current Edition of the AASHTO Standard Specifications for Highway Bridges, including current interim specifications.

Where required as shown on the contract plans, corrosion protection of the internal steel reinforcing bars, consisting of either encapsulation, epoxy coating, or grout, shall be provided in accordance with Materials Section 2.0. Where permanent casing is used for a portion of the micropile, encapsulation shall extend at least 1.5 m into the casing.

(Commentary: The previous paragraph is not comprehensive. Corrosion protection requirements need to be evaluated on a project-specific basis and detailed specifications and drawings depicting the corrosion protection requirements should be provided.)

(**Commentary:** When installation of micropiles provides additional support for existing structures, such as for seismic retrofit or underpinning applications, the structural designer should add appropriate specification verbiage and design criteria into this specification to cover the penetration of the existing structural elements and the top of pile anchorage to the existing structure.)

# 1.7.1 Micropile Design Submittals.

At least 21 calendar days before the planned start of micropile structure construction, submit complete design calculations and working drawings to the Engineer for review and approval. Include all details, dimensions, quantities, ground profiles, and cross-sections necessary to construct the micropile structure. Verify the limits of the micropile structure and ground survey data before preparing the detailed working drawings.

The drawings and calculations shall be signed and sealed by the contractor's Professional Engineer or by the Consultant designer's Professional Engineer (if applicable), previously approved by the owner's Engineer. If the micropile contractor uses a consultant design engineer to prepare the design, the micropile contractor shall still have overall contract responsibility for both the design and the construction.

### 1.7.2 Design Calculations.

Design calculations shall include, but not be limited to, the following items:

- 1. A written summary report which describes the overall micropile design.
- 2. Applicable code requirements and design references.
- 3. Micropile structure critical design cross-section(s) geometry including soil/rock strata and piezometric levels and location, magnitude and direction of design applied loadings, including slope or external surcharge loads.
- 4. Design criteria including, soil/rock shear strengths (friction angle and cohesion), unit weights, and ground-grout bond values and micropile drillhole diameter assumptions for each soil/rock strata.
- 5. Factors of safety and allowable stresses used in the design on the ground-grout bond values, surcharges, soil/rock and material unit weights, steel, grout, and concrete materials.
- 6. Seismic design earthquake acceleration coefficient.
- 7. Design calculation sheets (both static and seismic) with the project number, micropile structure location, designation, date of preparation, initials of designer and checker, and page number at the top of each page. Provide an index page with the design calculations.
- 8. Design notes including an explanation of any symbols and computer programs used in the design.
- 9. Pile to footing connection calculations.

(Commentary: If the contract allows the Contractor to provide alternative number of micropiles (e.g., provide fewer high capacity micropiles as compared to what is provided in plans, then the Contractor should also provide calculations for footing reinforcement (if different than that provided in the plans))).

# 1.7.3 Working Drawings.

The working drawings shall include all information required for the construction and quality control of the piling. Working drawings shall include, but not be limited to, the following items unless provided in the contract plans:

- 1. A plan view of the micropile structure(s) identifying:
  - (a) A reference baseline and elevation datum.
  - (b) The offset from the construction centerline or baseline to the face of the micropile structure at all changes in horizontal alignment.
  - (c) Beginning and end of micropile structure stations.
  - (d) Right-of-way and permanent or temporary construction easement limits, location of all known active and abandoned existing utilities, adjacent structures or other potential interferences. The centerline of any drainage structure or drainage pipe behind, passing through, or passing under the micropile structure.
  - (e) Subsurface exploration locations shown on a plan view of the proposed micropile structure alignment with appropriate reference base lines to fix the locations of the explorations relative to the micropile structure.
- 2. An elevation view of the micropile structure(s) identifying:
  - (a) Elevation view showing micropile locations and elevations; vertical and horizontal spacing; batter and alignment and the location of drainage elements (if applicable).
  - (b) Existing and finish grade profiles both behind and in front of the micropile structure.
- 3. Design parameters and applicable codes.
- 4. General notes for constructing the micropile structure including construction sequencing or other special construction requirements.
- 5. Horizontal and vertical curve data affecting the micropile structure and micropile structure control points. Match lines or other details to relate micropile structure stationing to centerline stationing.
- 6. A listing of the summary of quantities on the elevation drawing of each micropile structure showing pay item estimated quantities.
- 7. Micropile typical sections including micropile spacing and inclination; minimum drillhole diameter; pipe casing and reinforcing bar sizes and details; splice types and locations; centralizers and spacers; grout bond zone and casing plunge lengths (if used); corrosion protection details; and connection details to the substructure footing, anchorage, plates, etc.
- 8. A typical detail of verification and production proof test micropiles defining the micropile length, minimum drillhole diameter, inclination, and load test bonded and unbonded test lengths.

- 9. Details, dimensions, and schedules for all micropiles, casing and reinforcing steel, including reinforcing bar bending details.
- 10. Details for constructing micropile structures around drainage facilities (if applicable).

The working drawings and design calculations shall be signed and sealed by the Contractor's Professional Engineer or by the Consultant designer's Professional Engineer (if applicable), by the Owner. If the micropile Contractor uses a Consultant design engineer to prepare the design, the micropile Contractor shall still have overall contract responsibility for both the design and the construction.

Submit 5 sets of the working drawings with the initial submission. Drawing sheet size shall be 550 by 850 mm. One set will be returned with any indicated corrections. The Engineer will approve or reject the Contractor's submittal within 15 calendar days after receipt of a complete submission. If revisions are necessary, make the necessary corrections and resubmit 5 revised sets. When the drawings are approved, furnish 5 sets and a Mylar sepia set of the approved drawings. The Contractor will not be allowed to begin micropile structure construction or incorporate materials into the work until the submittal requirements are satisfied and found acceptable to the Engineer. Changes or deviations from the approved submittals must be re-submitted for approval. No adjustments in contract time or delay or impact claims will be allowed due to incomplete submittals. (*Commentary: Submittals procedures shall be coordinated with Owner/Agency procedures*).

Revise the drawings when plan dimensions are changed due to field conditions or for other reasons. Within 30 days after completion of the work, submit as-built drawings to the Engineer. Provide revised design calculations signed by the approved Registered Professional Engineer for all design changes made during the construction of the micropile structure.

#### 1.8 Construction Submittals.

The Contractor shall prepare and submit to the Engineer, for review of completeness, 5 copies of the following for the micropile system or systems to be constructed:

- 1. Detailed step-by-step description of the proposed micropile construction procedure, including personnel, testing and equipment to assure quality control. This step-by-step procedure shall be shown on the working drawings in sufficient detail to allow the Engineer to monitor the construction and quality of the micropiles.
- 2. Proposed start date and time schedule and micropile installation schedule providing the following:

Micropile number Micropile design load Type and size of reinforcing steel Minimum bond length Total micropile length Micropile top footing attachment

- 3. If welding of casing is proposed, submit the proposed welding procedure, certified by a qualified welding specialist.
- 4. Information on headroom and space requirements for installation equipment that verify the proposed equipment can perform at the site.
- 5. Plan describing how surface water, drill flush, and excess waste grout will be controlled and disposed.
- 6. Certified mill test reports for the reinforcing steel or coupon test results for permanent casing without mill certification. The ultimate strength, yield strength, elongation, and material properties composition shall be included. For API N-80 pipe casing, coupon test results may be submitted in lieu of mill certification.
- 7. Proposed Grouting Plan. The grouting plan shall include complete descriptions, details, and supporting calculations for the following:
  - (a) Grout mix design and type of materials to be used in the grout including certified test data and trial batch reports.
  - (b) Methods and equipment for accurately monitoring and recording the grout depth, grout volume and grout pressure as the grout is being placed.
  - (c) Grouting rate calculations, when requested by the Engineer. The calculations shall be based on the initial pump pressures or static head on the grout and losses throughout the placing system, including anticipated head of drilling fluid (if applicable) to be displaced.
  - (d) Estimated curing time for grout to achieve specified strength. Previous test results for the proposed grout mix completed within one year of the start of grouting may be submitted for initial verification and acceptance and start of production work. During production, grout shall be tested in accord with Section 3.4.5.
  - (e) Procedure and equipment for Contractor monitoring of grout quality.
- 8. Detailed plans for the proposed micropile load testing method. This shall include all drawings, details, and structural design calculations necessary to clearly describe the proposed test method, reaction load system capacity and equipment setup, types and accuracy of apparatus to be used for applying and measuring the test loads and pile top movements in accordance with Section 3.6, Pile Load Tests.
- 9. Calibration reports and data for each test jack, pressure gauge and master pressure gauge and electronic load cell to be used. The calibration tests shall have been

performed by an independent testing laboratory, and tests shall have been performed within 90 calendar days of the date submitted. Testing shall not commence until the Engineer has reviewed and accepted the jack, pressure gauge, master pressure gauge and electronic load cell calibration data.

Work other than test pile installation shall not begin until the construction submittals have been received, reviewed, and accepted in writing by the Engineer. Provide submittal items 1 through 5 at least 21 calendar days prior to initiating micropile construction, item 7 as the work progresses for each delivery and submittal items 6, 8 and 9 at least 7 days prior to start of micropile load testing or incorporation of the respective materials into the work. The Contractor shall allow the Engineer 7 calendar days to review the construction submittals after a complete set has been received. Additional time required due to incomplete or unacceptable submittals shall not be cause for delay or impact claims. All costs associated with incomplete or unacceptable Contractor submittals shall be the responsibility of the Contractor.

# 1.9 Pre-construction Meeting.

A pre-construction meeting will be scheduled by the Engineer and held prior to the start of micropile construction. The Engineer, prime Contractor, micropile specialty Contractor, micropile design engineer, excavation Contractor and geotechnical instrumentation specialist (if applicable) shall attend the meeting. Attendance is mandatory. The pre-construction meeting will be conducted to clarify the construction requirements for the work, to coordinate the construction schedule and activities, and to identify contractual relationships and delineation of responsibilities amongst the prime Contractor and the various Subcontractors - specifically those pertaining to excavation for micropile structures, anticipated subsurface conditions, micropile installation and testing, micropile structure survey control and site drainage control.

#### 2.0 MATERIALS.

Furnish materials new and without defects. Remove defective materials from the jobsite at no additional cost. Materials for micropiles shall consist of the following:

**Admixtures for Grout:** Admixtures shall conform to the requirements of ASTM C 494/AASHTO M194. Admixtures that control bleed, improve flowability, reduce water content, and retard set may be used in the grout, subject to the review and acceptance of the Engineer. Admixtures shall be compatible with the grout and mixed in accordance with the manufacturer's recommendations. Expansive admixtures shall only be added to the grout

used for filling sealed encapsulations and anchorage covers. Accelerators are not permitted. Admixtures containing chlorides are not permitted.

**Cement**: All cement shall be Portland cement conforming to ASTM C 150/AASHTO M85, Types I, II, III or V.

**Centralizers and Spacers:** Centralizers and spacers shall be fabricated from schedule 40 PVC pipe or tube, steel, or material non-detrimental to the reinforcing steel. Wood shall not be used.

**Encapsulation:** Encapsulation (double corrosion protection) shall be shop fabricated using high-density, corrugated polyethylene tubing conforming to the requirements of ASTM D3350/AASHTO M252 with a nominal wall thickness of 0.8 mm. The inside annulus between the reinforcing bars and the encapsulating tube shall be a minimum of 5mm and be fully grouted with non-shrink grout conforming to Materials Section 2.0.

**Epoxy Coating:** The minimum thickness of coating applied electrostatically to the reinforcing steel shall be 0.3 mm. Epoxy coating shall be in accordance with ASTM A775 or ASTM A934. Bend test requirements are waived. Bearing plates and nuts encased in the pile concrete footing need not be epoxy coated unless the footing reinforcement is epoxy coated.

**Fine Aggregate**: If sand - cement grout is used, sand shall conform to ASTM C 144/AASHTO M45.

**Galvanization**: If used, galvanization shall meet the requirements of ASTM A-153.

**Grout**: Neat cement or sand/cement mixture with a minimum 3-day compressive strength of 14 MPa and a 28-day compressive strength of 28 MPa per AASHTO T106/ASTM C109. (Commentary: Note to designers/specifiers. A 28-day grout strength of 28 MPa is common for micropiles. If the micropile design calls for higher grout strength, revise the specification accordingly.)

**Permanent Casing Pipe:** Permanent steel casing/pipe shall have the diameter and at least minimum wall thickness shown on the approved Working Drawings. The permanent steel casing/pipe:

1. shall meet the Tensile Requirements of ASTM A252, Grade 3, except the yield strength shall be a minimum of 345 MPa to 552 MPa as used in the design submittal.

2. may be new "Structural Grade" (a.k.a. "Mill Secondary") steel pipe meeting above but without Mill Certification, free from defects (dents, cracks, tears) and with two coupon tests per truckload delivered to the fabricator.

For permanent casing/pipe that will be welded for structural purposes, the following material conditions apply:

- 1. the carbon equivalency (CE) as defined in AWS D1.l, Section XI5.1, shall not exceed 0.45, as demonstrated by mill certifications
- 2. the sulfur content shall not exceed 0.05%, as demonstrated by mill certifications

For permanent casing/pipe that will be shop or field welded, the following fabrication or construction conditions apply:

- 1. the steel pipe shall not be joined by welded lap splicing
- 2. welded seams and splices shall be complete penetration welds
- 3. partial penetration welds may be restored in conformance with AWS D1.1
- 4. the proposed welding procedure certified by a welding specialist shall be submitted for approval

Threaded casing joints shall develop at least the required compressive, tensile, and/or bending strength used in the design of the micropile.

(Commentary: From a practical standpoint, the adequacy of pipe and reinforcing bar splices and threaded joint connections will be verified by the verification and proof load testing).

**Plates and Shapes:** Structural steel plates and shapes for pile top attachments shall conform to ASTM A 36/AASHTO M183, or ASTM A 572/AASHTO M223, Grade 350.

**Reinforcing Bars:** Reinforcing steel shall be deformed bars in accordance with ASTM A 615/AASHTO M31, Grade 420 or Grade 520 or ASTM A 722/AASHTO M275, Grade 1035. When a bearing plate and nut are required to be threaded onto the top end of reinforcing bars for the pile top to footing anchorage, the threading may be continuous spiral deformed ribbing provided by the bar deformations (e.g., Dywidag or Williams continuous threadbars) or may be cut into a reinforcing bar. If threads are cut into a reinforcing bar, the next larger bar number designation from that shown on the Plans shall be provided, at no additional cost.

Bar tendon couplers, if required, shall develop the ultimate tensile strength of the bars without evidence of any failure.

## **Reinforcing Bar Corrosion Protection:**

(Commentary: Corrosion protection requirements vary between Transportation Agencies. The most common and simplest tests utilized to measure the aggressiveness of the soil environment include electrical resistivity, pH, chloride, and sulfate. Per FHWA NHI-05-039, the ground is considered aggressive if any one of these indicators show critical values as detailed below:

PROPERTY	TEST DESIGNATION*	CRITICAL VALUES*
Resistivity	AASHTO T-288	below 3,000 ohm-cm
pН	AASHTO T-289	below 5 or above 10
Sulfates	AASHTO T-290	above 200 ppm
Chlorides	AASHTO T-291	above 100 ppm

^{*} Specifier should check test standards for latest updates and individual transportation agencies may have limits on critical values different than tabulated above. Standard specifications or test methods for any of the above items which are common to your agency can be referenced in lieu of the above listed AASHTO/ASTM references.

**Sheathing:** Smooth plastic sheathing, including joints, shall be watertight. Polyvinyl chloride (PVC) sheathing shall conform to ASTM D 1784, Class 13464-B.

**Water:** Water used in the grout mix shall conform to AASHTO T 26 and shall be potable, clean, and free from substances that may be injurious to cement and steel.

### 3.0 CONSTRUCTION REQUIREMENTS

### 3.1 Site Drainage Control.

The Contractor shall control and properly dispose of drill flush and construction related waste, including excess grout, in accord with the standard specifications and all applicable local codes and regulations. Provide positive control and discharge of all surface water that will affect construction of the micropile installation. Maintain all pipes or conduits used to control surface water during construction. Repair damage caused by surface water at no additional cost. Upon substantial completion of the Work, remove surface water control pipes or conduits from the site. Alternatively, with the approval of the Engineer, pipes or conduits that are left in place, may be fully grouted and abandoned or left in a way that protects the

structure and all adjacent facilities from migration of fines through the pipe or conduit and potential ground loss.

Immediately contact the Engineer if unanticipated existing subsurface drainage structures are discovered during excavation or drilling. Suspend work in these areas until remedial measures meeting the Engineer's approval are implemented. Cost of remedial measures or repair work resulting from encountering unanticipated subsurface drainage structures, will be paid for as Extra Work.

### 3.2 Excavation

Coordinate the work and the excavation so the micropile structures are safely constructed. Perform the micropile construction and related excavation in accordance with the Plans and approved submittals. No excavations steeper than those specified herein or shown on the Plans will be made above or below the micropile structure locations without written approval of the Engineer.

### 3.3 Micropile Allowable Construction Tolerances

- 1. Centerline of piling shall not be more than 75 mm from indicated plan location.
- 2. Pile shall be plumb within 2 percent of total-length plan alignment.
- 3. Top elevation of pile shall be plus 25 mm or minus 50 mm maximum from vertical elevation indicated.
- 4. Centerline of reinforcing steel shall not be more than 19 mm from indicated location

(Commentary: The tolerances provided in this Section are maxima. Depending on the structural requirements, the actual values set for a particular project may need to be lower.)

## 3.4 Micropile Installation

The micropile Contractor shall select the drilling method, the grouting procedure, and the grouting pressure used for the installation of the micropiles. The micropile Contractor shall also determine the micropile casing size, final drillhole diameter and bond length, and central reinforcement steel sizing necessary to develop the specified load capacities and load testing requirements. The micropile Contractor is also responsible for estimating the grout take. There will be no extra payment for grout overruns. (*Commentary:* Note, extra payment for grout takes is appropriate for micropiles in Karst. Otherwise, the bid price of these piles will be artificially high to cover risk of high grout loss.)

## 3.4.1 Drilling

The drilling equipment and methods shall be suitable for drilling through the conditions to be encountered, without causing damage to any overlying or adjacent structures or services. The drillhole must be open along its full length to at least the design minimum drillhole diameter prior to placing grout and reinforcement. (*Commentary: When micropile construction will occur in close proximity to settlement sensitive structures, recommend including the following sentence in the specification - Vibratory pile driving hammers shall not be used to advance casing.*)

Temporary casing or other approved method of pile drillhole support will be required in caving or unstable ground to permit the pile shaft to be formed to the minimum design drillhole diameter. The Contractor's proposed method(s) to provide drillhole support and to prevent detrimental ground movements shall be reviewed by the Engineer. Detrimental ground movement is defined as movement which requires remedial repair measures. Use of drilling fluid containing bentonite is not allowed. (Commentary: The specification verbiage related to drillhole support methods and difficulty of drilling may vary project to project depending on the subsurface conditions revealed by the subsurface investigation data. It is the micropile specialty contractor's responsibility to select the proper drilling equipment and methods for the site conditions. It is the owner's responsibility to provide the available subsurface information. For projects with difficult ground conditions, use of an "advisory specification" included in the contract documents is recommended).

Costs of removal or remedial measures due to encountering unanticipated subsurface obstructions will be paid for as Extra Work.

#### 3.4.2 Ground Heave or Subsidence.

During construction, the Contractor shall observe the conditions in the vicinity of the micropile construction site on a daily basis for signs of ground heave or subsidence. Immediately notify the Engineer if signs of movements are observed. Contractor shall immediately suspend or modify drilling or grouting operations if ground heave or subsidence is observed, if the micropile structure is adversely affected, or if adjacent structures are damaged from the drilling or grouting. If the Engineer determines that the movements require corrective action, the Contractor shall take corrective actions necessary to stop the movement or perform repairs. When due to the Contractor's methods or operations or failure to follow the specified/approved construction sequence, as determined by the Engineer, the costs of providing corrective actions will be borne by the Contractor. When due to differing site conditions, as determined by the Engineer, the costs of providing corrective actions will be paid as Extra Work.

# 3.4.3 Pipe Casing and Reinforcing Bars Placement and Splicing.

Reinforcement may be placed either prior to grouting or placed into the grout - filled drillhole before temporary casing (if used) is withdrawn. Reinforcement surface shall be free of deleterious substances such as soil, mud, grease or oil that might contaminate the grout or coat the reinforcement and impair bond. Pile cages and reinforcement groups, if used, shall be sufficiently robust to withstand the installation and grouting process and the withdrawal of the drill casings without damage or disturbance.

The Contractor shall check pile top elevations and adjust all installed micropiles to the planned elevations.

Centralizers and spacers (if used) shall be provided at 3-m centers maximum spacing. The upper and lower most centralizer shall be located a maximum of 1.5 m from the top and bottom of the micropile. Centralizers and spacers shall permit the free flow of grout without misalignment of the reinforcing bar(s) and permanent casing. The central reinforcement bars with centralizers shall be lowered into the stabilized drillhole and set. The reinforcing steel shall be inserted into the drill hole to the desired depth without difficulty. Partially inserted reinforcing bars shall not be driven or forced into the hole. Contractor shall redrill and reinsert reinforcing steel when necessary to facilitate insertion.

Lengths of casing and reinforcing bars to be spliced shall be secured in proper alignment and in a manner to avoid eccentricity or angle between the axes of the two lengths to be spliced. Splices and threaded joints shall meet the requirements of Materials Section 2.0. Threaded pipe casing joints shall be located at least two casing diameters (OD) from a splice in any reinforcing bar. When multiple bars are used, bar splices shall be staggered at least 0.3 meters.

### 3.4.4 Grouting.

Micropiles shall be primary grouted the same day the load transfer bond length is drilled. The Contractor shall use a stable neat cement grout or a sand cement grout with a minimum 28-day unconfined compressive strength of 28 MPa. Admixtures, if used, shall be mixed in accordance with manufacturer's recommendations. The grouting equipment used shall produce a grout free of lumps and undispersed cement. The Contractor shall have means and methods of measuring the grout quantity and pumping pressure during the grouting operations. The grout pump shall be equipped with a pressure gauge to monitor grout pressures. A second pressure gauge shall be placed at the point of injection into the pile top. The pressure gauges shall be capable of measuring pressures of at least 1 MPa or twice the actual grout pressures used, whichever is greater. The grout shall be kept in agitation prior to

mixing. Grout shall be placed within one hour of mixing. The grouting equipment shall be sized to enable each pile to be grouted in one continuous operation.

The grout shall be injected from the lowest point of the drill hole and injection shall continue until uncontaminated grout flows from the top of the pile. The grout may be pumped through grout tubes, casing, hollow-stem augers, or drill rods. Temporary casing, if used, shall be extracted in stages ensuring that, after each length of casing is removed the grout level is brought back up to the ground level before the next length is removed. The tremie pipe or casing shall always extend below the level of the existing grout in the drillhole. The grout pressures and grout takes shall be controlled to prevent excessive heave or fracturing of rock or soil formations. Upon completion of grouting, the grout tube may remain in the hole, but must be filled with grout.

Grout within the micropiles shall be allowed to attain the required design strength prior to being loaded.

If the Contractor elects to use a postgrouting system, Working Drawings and details shall be submitted to the Engineer for review in accordance with Section 1.8, Pre-installation Submittals.

# 3.4.5 Grout Testing

Grout within the micropile verification and proof test piles shall attain the minimum required 3-day compressive strength of 14 MPa prior to load testing. Previous test results for the proposed grout mix completed within one year of the start of work may be submitted for initial verification of the required compressive strengths for installation of pre-production verification test piles and initial production piles. During production, micropile grout shall be tested by the Contractor for compressive strength in accordance with AASHTO T106/ASTM C109 at a frequency of no less than one set of three 50-mm grout cubes from each grout plant each day of operation or per every 10 piles, whichever occurs more frequently. The compressive strength shall be the average of the 3 cubes tested.

Grout consistency as measured by grout density shall be deter	rmined by the Contra	ctor per
ASTM C 188/AASHTO T 133 or API RP-13B-1 at a frequence	ey of at least one test	per pile,
conducted just prior to start of pile grouting. The Baroid Mud	Balance used in acco	rdance
with API RP-13B-1 is an approved device for determining the	grout density of neat	cement
grout. The measured grout density shall be between	kg/m³ and	$kg/m^3$ .

Grout samples shall be taken directly from the grout plant. Provide grout cube compressive strength and grout density test results to the Engineer within 24 hours of testing. (Commentary: If the Engineer will perform the grout testing, revise this section accordingly).

## 3.5 Micropile Installation Records.

Contractor shall prepare and submit to the Engineer full-length installation records for each micropile installed. The records shall be submitted within one work shift after that pile installation is completed. The data shall be recorded on the micropile installation log. A separate log shall be provided for each micropile. (*Commentary: In addition to the expertise of the micropile specialty Contractor, the quality of the individual construction elements is directly related to the final product overall quality. As with other drilled pile systems, the actual load carrying capacity of a micropile can only be definitively proven by pile load tests. It is not practical or economical to test every pile installed. Therefore, inspection by the Contractor and Owner's Engineer is needed to assure that each individual micropile is well constructed and to justify load testing only a small number, e.g., 5%, of the total number of production piles installed.)* 

### 3.6 Pile Load Tests

Perform verification and proof testing of piles at the locations specified herein or designated by the Engineer. Perform compression load testing in accord with ASTM D1143, tension load testing in accord with ASTM D3689, and lateral load testing in accord with ASTM D3966, except as modified herein.

(Commentary: Specifier/design engineer needs to determine and write into this portion of the specification the number of required verification and proof tests. The total number of load tests and maximum test loads to be specified can vary on a project-by-project basis. They are dependent on ground type and variability, required pile capacity, pile loading type (i.e., static or seismic), total number of piles, criticality of the structure and available site access and work space. Guideline criteria for estimating the total number of verification and proof test piles are given in Chapter 7 of FHWA NHI-05-039. If pile capacity demands are greatest in compression, the piles should be load tested in compression. If the pile capacity demands are equal for both compression and tension, or greater in tension, it is recommended that tension testing alone be conducted, to reduce costs).

(Commentary: Specifier - Indicate here which types of load tests are required for the project).

### 3.6.1 Verification Load Tests

Perform pre-production verification pile load testing to verify the design of the pile system and the construction methods proposed prior to installing any production piles. ______ sacrificial verification test piles shall be constructed in conformance with the approved

Working Drawings. Verification test pile(s) shall be installed at the following locations

_____,

Verification load tests shall be performed to verify that the Contractor installed micropiles will meet the required compression and tension load capacities and load test acceptance criteria and to verify that the length of the micropile bond zone is adequate. The micropile verification load test results must verify the Contractor's design and installation methods, and be reviewed and accepted by the Engineer prior to beginning installation of production micropiles.

The drilling-and-grouting method, casing length and outside diameter, reinforcing bar lengths, and depth of embedment for the verification test pile(s) shall be identical to those specified for the production piles at the given locations. The verification test micropile structural steel sections shall be sized to safely resist the maximum test load. (Commentary: Note that if additional steel area is provided in the verification test, the measured deflection will be lower than production piles.)

The maximum verification and proof test loads applied to the micropile shall not exceed 80 percent of the structural capacity of the micropile structural elements, to include steel yield in tension, steel yield or buckling in compression, or grout crushing in compression. Any required increase in strength of the verification test pile elements above the strength required for the production piles shall be provided for in the contractor's bid price.

The jack shall be positioned at the beginning of the test such that unloading and repositioning during the test will not be required. When both compression and tension load testing is to be performed on the same pile, the pile shall be tested under compression loads prior to testing under tension loads.

### 3.6.2 Testing Equipment and Data Recording.

Testing equipment shall include dial gauges, dial gauge support, jack and pressure gauge, electronic load cell, and a reaction frame. The load cell is required only for the creep test portion of the verification test. (Commentary: The purpose and value of an electronic load cell is to measure small changes in load for load tests where the load is held for a long duration, such as during verification or creep testing. It is not intended to be used during proof testing, including the short term creep portion. Experience has proven that load cells have been problematic under field conditions, yet even with errors resulting from cell construction, off-center loading, and other effects, a load cell is very sensitive to small changes in load and is strongly recommended for creep testing.) The contractor shall provide a description of test setup and jack, pressure gauge and load cell calibration curves in accordance with the Submittals Section.

Design the testing reaction frame to be sufficiently rigid and of adequate dimensions such that excessive deformation of the testing equipment does not occur. Align the jack, bearing plates, and stressing anchorage such that unloading and repositioning of the equipment will not be required during the test.

Apply and measure the test load with a hydraulic jack and pressure gauge. The pressure gauge shall be graduated in 500 kPa increments or less. The jack and pressure gauge shall have a pressure range not exceeding twice the anticipated maximum test pressure. Jack ram travel shall be sufficient to allow the test to be done without resetting the equipment. Monitor the creep test load hold during verification tests with both the pressure gauge and the electronic load cell. Use the load cell to accurately maintain a constant load hold during the creep test load hold increment of the verification test.

Measure the pile top movement with a dial gauge capable of measuring to 0.025 mm. The dial gauge shall have a travel sufficient to allow the test to be done without having to reset the gauge. Visually align the gauge to be parallel with the axis of the micropile and support the gauge independently from the jack, pile or reaction frame. Use a minimum of two dial gauges when the test setup requires reaction against the ground or single reaction piles on each side of the test pile. (Commentary: Experience with testing piles reacting against the ground, or against single reaction piles on each side of the test pile, has resulted in racking and misalignment of the system on some projects. Two dial gauges are recommended for this test setup to determine if racking is occurring and to provide a more accurate average micropile head movement measurement).

The required load test data shall be recorded by the Engineer.

## 3.6.3 Verification Test Loading Schedule.

Test verification piles designated for compression or tension load testing to a maximum test load of 2.0 times the micropile Design Load shown on the Plans or Working Drawings.

(Commentary: The maximum test load shall be at least to the Design Load multiplied by the factor of safety used to estimate the bond length of the micropile. In some cases, e.g., potentially creeping ground, this factor of safety may be as high as 2.5.) The verification pile load tests shall be made by incrementally loading the micropile in accordance with the following cyclic load schedule for both compression and tension loading:

Step	Loading	Applied Load	Hold Time (min.)
1	Apply AL		2.5
		0.15 DL	2.5
2	Create 1	0.30 DL	2.5
2	Cycle 1	0.45 DL	2.5
		AL	1
		0.15 DL	1
		0.30 DL	1
		0.45 DL	2.5
3	Cyala 2	0.60 DL	2.5
3	Cycle 2	0.75 DL	2.5
		0.90 DL	2,5
		1.00 DL	2.5
		AL	1
	G 1 2	0.15 DL	1
		1.00 DL	1
4		1.15 DL	2.5
4	Cycle 3	1.30 DL	10 to 60 minutes
		1.45 DL	2.5
		AL	1
		0.15 DL	1
		1.45 DL	1
		1.60 DL	1
		1.75 DL	2.5
£	Create 4	1.90 DL	2.5
5	Cycle 4	2.00 DL	10
		1.50 DL	5
		1.00 DL	5
		0.50 DL	5
		AL	5

Pile top movement shall be measured at each load increment. The load-hold period shall start as soon as each test load increment is applied. The verification test pile shall be monitored for creep at the 1.30 Design Load (DL). Pile movement during the creep test shall be measured and recorded at 1, 2, 3, 4, 5, 6, 10, 20, 30, 50, and 60 minutes. The alignment

load shall not exceed 5 percent of the DL load. Dial gauges shall be reset to zero after the initial AL is applied.

The acceptance criteria for micropile verification load tests are:

- 1. The pile shall sustain the first compression or tension 1.0 DL test load with no more than _____mm total vertical movement at the top of the pile, relative to the position of the top of the pile prior to testing. (Commentary: Structural designer to determine maximum allowable total pile top structural axial displacement at 1.0 DL test load based on structural design requirements. The allowable displacement should also consider long term pile group settlements at the Design Load. Also, if the verification test pile has to be upsized structurally to accommodate the maximum required verification test load, this provision will not apply. Only the proof tested production piles will then be subject to this criterion.).
- 2. At the end of the 1.30 DL creep test load increment, test piles shall have a creep rate not exceeding 1 mm/log cycle time (1 to 10 minutes) or 2 mm/log cycle time (6 to 60 minutes or the last log cycle if held longer). The creep rate shall be linear or decreasing throughout the creep load hold period.
- 3. Failure does not occur at the 2.0 DL maximum test load. Failure is defined as load where the slope of the load versus head settlement curve first exceeds 0.15 mm/kN.

The Engineer will provide the Contractor written confirmation of the micropile design and construction within 3 working days of the completion of the verification load tests. This written confirmation will either confirm the capacities and bond lengths specified in the Working Drawings for micropiles or reject the piles based upon the verification test results.

## 3.6.4 Verification Test Pile Rejection

If a verification-tested micropile fails to meet the acceptance criteria, the Contractor shall modify the design, the construction procedure, or both. These modifications may include modifying the installation methods, increasing the bond length, or changing the micropile type. Any modification that necessitates changes to the structure shall require the Engineer's prior review and acceptance. Any modifications of design or construction procedures or cost of additional verification test piles and load testing shall be at the Contractor's expense. At the completion of verification testing, test piles shall be removed down to the elevation specified by the Engineer.

## 3.6.5 Proof Load Tests

Perform proof load tests on	the first set of production piles installed at each designated
substructure unit prior to the	e installation of the remaining production piles in that unit. The
first set of production piles	is the number required to provide the required reaction capacity
for the proof tested pile. The	ne initial proof test piles shall be installed at the following
substructure units	Proof testing shall be conducted at a frequency of
Locat	ion of additional proof test piles shall be as designated by the
Engineer. (Commentary: C	Guidance on the number of proof tests to be performed is providea
in Chapter 7 of FHWA NHI	7-05-039.)

# 3.6.6 Proof Test Loading Schedule

Test piles designated for compression or tension proof load testing to a maximum test load of 1.60 times the micropile Design Load shown on the Plans or Working Drawings. Proof tests shall be made by incrementally loading the micropile in accordance with the following schedule, to be used for both compression and tension loading:

Step	Loading	Applied Load	Hold Time (min.)
1	Apply AL		2.5
		0.15 DL	2.5
		0.30 DL	2.5
		0.45 DL	2.5
		0.60 DL	2.5
		0.75 DL	2.5
2	Load Cycle	0.90 DL	2.5
		1.00 DL	2.5
		1.15 DL	2.5
		1.30 DL	10 to 60 minutes
		1.45 DL	2.5
		1.60 DL	2.5
		1.30 DL	4
		1.00 DL	4
3		0.75 DL	4
	Unload Cycle	0.50 DL	4
		0.25 DL	4
		AL	4

Depending on performance, either a 10 minute or 60 minute creep test shall be performed at the 1.30DL Test Load. Where the pile top movement between 1 and 10 minutes exceeds 1 mm, the Maximum Test Load shall be maintained an additional 50 minutes. Movements shall be recorded at 1, 2, 3, 5, 6, 10, 20, 30, 50 and 60 minutes. The alignment load shall not exceed 5 percent of DL. Dial gauges shall be reset to zero after the initial AL is applied. The acceptance criteria for micropile proof load tests are:

- 1. The pile shall sustain the compression or tension 1.0 DL test load with no more than _____ mm total vertical movement at the top of the pile, relative to the position of the top of the pile prior to testing. (Commentary: Structural designer to determine maximum allowable total pile top structural axial displacement at 1.0 DL test load based on structural design requirements. The allowable displacement should also consider long term pile group settlements at the Design Load.)
- 2. At the end of the 1.30DL creep test load increment, test piles shall have a creep rate not exceeding 1 mm/log cycle time (1 to 10 minutes) or 2 mm/log cycle time (6 to 60 minutes). The creep rate shall be linear or decreasing throughout the creep load hold period.
- 3. Failure does not occur at the 1.60DL maximum test load. Failure is defined as load where the slope of the load versus head settlement curve first exceeds 0.15 mm/kN.

## 3.6.7 Proof Test Pile Rejection

If a proof-tested micropile fails to meet the acceptance criteria, the Contractor shall immediately proof test another micropile within that footing. For failed piles and further construction of other piles, the Contractor shall modify the design, the construction procedure, or both. These modifications may include installing replacement micropiles, incorporating piles at not more than 50% of the maximum load attained, postgrouting, modifying installation methods, increasing the bond length, or changing the micropile type. Any modification that necessitates changes to the structure design shall require the Engineer's prior review and acceptance. Any modifications of design or construction procedures, or cost of additional verification test piles and verification and/or proof load testing, or replacement production micropiles, shall be at the Contractor's expense.

## 4.0 METHOD OF MEASUREMENT.

Measurement will be made as follows for the quantity, as specified or directed by the Engineer:

- Mobilization will be measured on a lump-sum basis.
- Micropiles will be measured per each, installed, and accepted.
- Micropile verification load testing will be measured per each.
- Micropile proof load testing will be measured per each.

The final pay quantities will be the design quantity increased or decreased by any changes authorized by the Engineer.

#### 5.0 BASIS OF PAYMENT

The quantities accepted for payment will be paid for at the contract unit prices for the following items:

Pay Item	Unit
Mobilization and Demobilization	Lump Sum
Micropile Verification Load Test	Each
Micropile Proof Load Test	Each
Micropiles	Each*
Micropiles Variations in Length to Top of Rock	LF**
Unexpected Obstruction Drilling	Hour***

^{*}For the option where the contractor designs the footing and number of piles, the foundation system should be bid as lump sum and a schedule of values established for progress payments after award.

The contract unit prices for the above items will be full and complete payment for providing all design, materials, labor, equipment, and incidentals to complete the work.

Where verification test piles are designated as sacrificial, the micropile verification load test bid item shall include the cost of the sacrificial micropile.

The unit contract amount for "Micropiles" shall include the drilling, furnishing, and placing the reinforcing steel and casing, grouting, and pile top attachments. The micropile Contractor is also responsible for estimating the grout take. There will be no extra payment for grout overruns.

^{**}Where piles are founded in rock, micropiles will be paid on a per each basis assuming Rock at Elevation _____. Additional length or shorter length due to variations in the top of rock will be paid on an add or deduct lineal foot basis where the linear footage = Elevation ____ minus Elevation of As-Built Rock.

^{***}If "obstructions" are not defined in the Standard Specifications, a definition should be added.

#### SAMPLE PROBLEM NO. 1 – BRIDGE ABUTMENT FOUNDATION SUPPORT

The following sample problem illustrates the design of foundation support for a bridge abutment using micropiles. This sample problem is intended to illustrate the quantification of typical abutment loads and the design of a micropile foundation for non-seismic load groups. In the example, seismic loads are provided and the example could be repeated using these loads. Practitioners typically follow different procedures around the United States in the design of bridge abutments, and therefore this sample problem is not intended to depict a "standard abutment" or a "standard abutment design procedure." For simplicity, this example problem considers only a portion of the longitudinal forces and no transverse forces. Abutment designs, which include wind or seismic forces, for example, would have transverse as well as longitudinal forces. This example also does not illustrate construction load cases (e.g., full backfill prior to girder placement) that need to be incorporated into actual designs.

#### **Problem Statement**

The structure is a simply supported, single-span bridge, 30 meters long, supported on concrete retaining abutments. The superstructure consists of 5 AASHTO Type IV precast - prestressed concrete girders with a cast-in-place concrete deck.

The bridge abutment length is 10.5 meters. The abutment wall backfill material is medium dense sand with an angle of internal friction of 35 degrees and a unit weight of  $17.5 \text{ kN/m}^3$ . The unit weight of the concrete is  $23.6 \text{ kN/m}^3$ . Figure S1-1 shows the dimensions of the abutment. The pile details are shown on Figure S1-2.

A summary of loading applied to the bridge abutment is shown in Figure S1-3. All load values are per 1-meter length of the abutment. The seismic site coefficient is 0.1 g.

The foundation soil conditions are described in the boring log contained in Figure S1-4. These soils consist of 2.5 meters of loose sandy gravel underlain by moderately compressible soft, brown, fine sandy silt, which is 1.5 meters thick. The silt is underlain by dense to very dense gravel with cobbles and boulders that extends to a maximum depth of 30 meters. Ground water is 4 meters below the top of footing. Type B3 (pressure grouted through the casing during casing withdrawal) micropiles will be used. The bond length will be formed in the dense gravel.

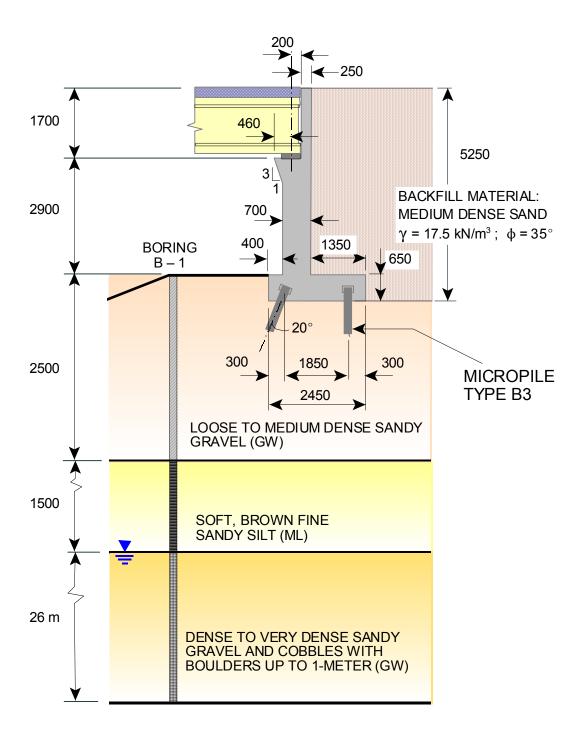


Figure S1-1. Sample Problem No. 1 - Abutment Section Detail (unless noted, all length dimensions in mm)

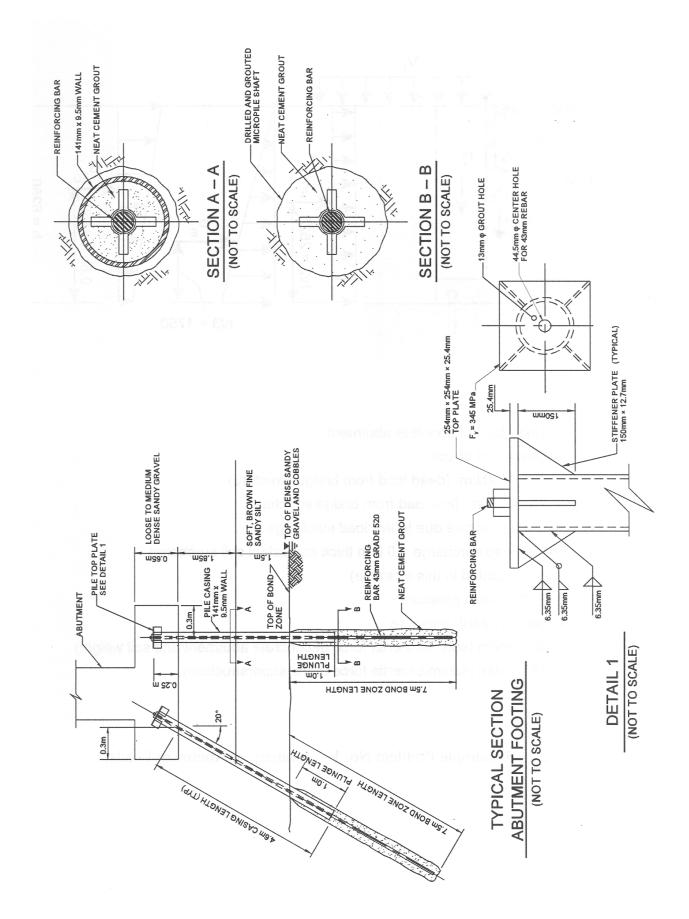
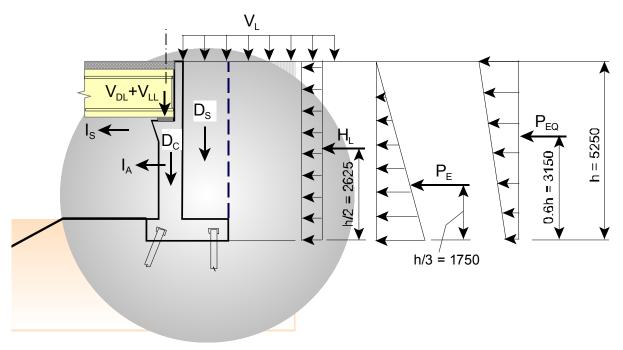


Figure S1-2. Sample Problem No. 1 – Pile Details



 $D_C$  = Dead load of concrete abutment

 $D_S$  = Dead load of soil

 $V_{DL}$  = 178.70 kN/m (dead load from bridge structure)

 $V_{LL}$  = 73.00 kN/m (live load from bridge structure)

H_L = Earth pressure due to live load surcharge V_L

V_L = Live load surcharge = 0.6 m thick equivalent soil surcharge (not included in this example)

 $P_E$  = Active earth pressure

 $P_{EQ}$  = Seismic earth pressure

I_A = 30.9 kN/m (seismic inertia force of concrete abutment and soil weight)

 $I_S$  = 26.8 kN/m (seismic inertia force of the superstructure)

Figure S1-3. Sample Problem No. 1 – Summary of Abutment Loads

6	FEDERAL HIGHWAY ADMINISTRATION VANCOUVER, WASHINGTON GEOTECHNICAL SECTION BORING LOG (METRIC L	v of applic		AUGER () (	BEGAN: 28/11/ COMPLETED: 2 DRILL: CME 8: DRILLER: Rod WEATHER: Wa	28/11/95 50 Terzagh	i
DЕРТН (m)	DESCRIPTION	SAMPLE SAMPLE#	BLOW	(Blo	enetration Resis ws per 0.3 m) 40 60	stance 80	DEPTH (m)
1	Loose to medium dense, gray sandy subrounded gravel (GW)	R-1	AASHTO SLD) of r				1
2		SPT-1	4-5-6	1 <b>1 1</b> 1 916	. 131 02 1.41		2-
	Soft brown, fine sandy silt (ML)	R-2	rob odzen i				
3-1	Ground Water Level	SPT-2	2-3-3	•			3-
4	Dense, gray sandy subrounded gravel and cobbles with boulders up to 1	R-3	or the do				4
5	meter (GW)  Drove sampler on boulder	SPT-3	20-25-50/1		•		5
	boulder	R-4	91%	ismulane na mezob			
6	Some seams at clean medium sand up to 150 mm thick.	SPT-4	20-22-25		•		6
7	boulder Description of the second of the sec	R-5	68%				7-
8-	Becomes very dense	land b	qot stiq ed				8
	boulder	SPT-5	28-34-50/30 78%				1
9	Note: Similar material encountered to maximum depth explored of 30 meters.	SPT-6	eliotol gar	roda (gora			9
10	rocedures.	R-7	25-34-41 63%	inolbiu	19,491, 10		10
	ECT: Micropile Example Problem #1	o joud o	/ii ,bsoi ba	की रहता वार्	BORING B		2 1
	ION. OFFSET:					eet: 1 o	f 1

Figure S1-4. Sample Problem No. 1 – Soil Boring Log

#### STEP 1 – ABUTMENT DESIGN LOADS

The magnitude and point of application for the active earth pressure, earth pressure due to live load surcharge, and seismic earth pressure is determined in this section. Calculations for the remaining components of the abutment loading are not included. The magnitude, point of application, and resulting moment on the abutment for the entire load components are summarized in Table S1-1. The moments are taken about the center point of the base of the abutment footing.

#### Active Earth Pressure - PE

Soil internal friction angle  $\phi = 35$  degrees Unit weight of soil  $\gamma_{soil} = 17.5 \text{ kN} / \text{m}^3$ 

Coefficient of active soil pressure  $K_a = \tan^2 \left[ 45^\circ - \frac{\varphi}{2} \right] = 0.271$  $K_a \gamma_{soil} = 4.74 \text{ kN} / \text{m}^3$ 

Resultant load  $P_E = 0.5 \times 4.74 \frac{kN}{m^3} \times (5.25m)^2 = 65.32 \ kN/m$ 

Moment about centroid  $65.32 \frac{kN}{m} \times \frac{5.25m}{3} = 114.31 \, kN - m/m$ 

# Earth Pressure Due to Live Load Surcharge - $H_{\rm L}$

Surcharge pressure  $K_a \times \gamma_{soil} \times 0.6m = 2.84 \text{ kPa}$ 

Surcharge load  $2.84 \text{ kN} \times 5.25 \text{m} = 14.91 \text{ kN} / \text{m}$ 

Moment about centroid  $14.91 \frac{kN}{m} \times \frac{5.25m}{2} = 39.1 \, kNm/m$ 

Table S1-1. Sample Problem No. 1- Summary of Abutment Loads Per Meter Length

			Load		Moment Arm		Moment*	
Load	Description	Туре	F _x (kN)	F _y (kN)	X (m)	Y (m)	M (kN-m)	
$D_c$	Dead load of concrete abutment	D		97.00	0.27		26.19	
$D_{S}$	Dead load of soil	E		108.68	-0.55		-59.77	
$V_{ m DL}$	Dead load from bridge superstructure	D		178.70	0.58		103.65	
$V_{LL}$	Live load from bridge superstructure	L		73.00	0.58		42.34	
$H_L$	Earth pressure due to live load surcharge	L	14.91			2.63	39.13	
P _E	Earth pressure	Е	65.32			1.75	114.31	
P _{EQ-H}	Seismic earth pressure	EQ	15.91			3.15	50.12	
$I_A$	Seismic inertial force of concrete & soil weight	EQ	30.9			2.35	72.50	
$I_{S}$	Seismic inertial force of the superstructure	EQ	26.8			3.55	95.14	

^{*}Moment is calculated about the center of the footing at its base.

## Seismic Earth Pressure - PEQ

See "Seismic Design of Bridges - Design Example No. 3" Publication No. FHWA-SA-97-008 for a description of the following Mononobe - Okabe lateral seismic earth over pressure and the seismic inertia forces from the abutment self-weight and the soil resting on the abutment footing.

Seismic acceleration coefficient: A = 0.10

Seismic coefficients  $k_h = 1.5 \times A = 0.15$  and  $k_v = 0$  (assumed value)

Reference AASHTO Sec. 6.4.3 (A) Div. 1A.

Slope of soil face:  $\beta = 0^{\circ}$ 

Backfill slope angle:  $i = 0^{\circ}$ 

Friction angle between soil and abutment:  $\delta = \frac{1}{2} \phi = 17.5^{\circ}$ 

Seismic inertia angle

$$\theta = \tan^{-1} \left[ \frac{k_h}{1 - k_v} \right] = 8.53^{\circ}$$

Seismic earth pressure coefficient

$$\Psi = \left[1 + \sqrt{\frac{\sin(\varphi + \delta) \times \sin(\varphi - \theta - i)}{\cos(\delta + \beta + \theta) \times \cos(i - \beta)}}\right]^{2} = 2.65$$

$$K_{AE} = \left[\frac{\cos^{2}(\varphi - \theta)}{\Psi \times \cos(\theta) \times \cos(\theta + \delta)}\right] = 0.34$$

Seismic earth pressure

$$K_{AE} \gamma_{soil} = 5.95 \text{ kN} / m^3$$

Resultant seismic force

$$P_{EQ} = \left[ 0.5 \times 5.95 \frac{kN}{m^3} \times (5.25m)^2 \right] - P_E = 16.68 \ kN / m$$

Since this force is at angle  $\delta$  to the horizontal,

$$P_{EQ-H} = 16.68 \frac{kN}{m} (\cos \delta) = 15.91 kN/m$$

To be conservative, neglect the vertical portion of  $P_{EQ}$  over the footing heel.

#### Seismic Inertia Forces

$$I_A = k_h (D_C + D_S) = 0.15 \times (97.0 + 108.68) = 30.9 \,\text{kN} / m$$

$$I_S = k_h(V_{DL}) = 0.15 \times 178.70 = 26.8kN/m$$

Moment about centroid:  $16.68 \frac{kN}{m} \times 0.6 \times 5.25 m = 52.54 \frac{kNm}{m}$ 

## STEP 2 – DETERMINE PILE DESIGN LOADS PER METER LENGTH

The Group I loads per AASHTO Table 3.22.1A are calculated from the abutment loads shown in Table 5-4.

 $F_y$  = sum of vertical loads

 $F_x$  = sum of horizontal loads

M = sum of moments about the center of the footing at its base.

$$F_v = D_C + D_S + V_{DL} + V_{LL}$$

$$F_v = 97.0 + 108.7 + 178.7 + 73.0 = 457.4 \text{ kN/m}$$

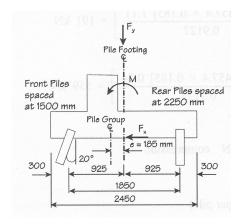
$$F_x = H_L + P_E$$

$$F_x = 15.0 + 65.3 = 80.3 \text{ kN/m}$$

$$M \; = \; D_C + D_S + V_{DL} + V_{LL} + H_L + P_E$$

$$M = 26.2 - 59.8 + 103.7 + 42.3 + 39.3 + 114.3 = 266.0 \text{ kN/m}$$

## **Determine Pile Group Properties Per Meter Length**



Centroid of Pile Group (from front pile)					
Front piles:	1/1.5	×	0.0	=	0.0
Rear piles:	1 / 2.25	×	1.85	=	0.822
Sum:	1.111				0.822

So centroid is (0.822/1.111) = 0.74 m from front pile.

$$e = \frac{1.85}{2} - 0.74 = 0.185 \, m$$

Pile Group I about centroid

$$I = \frac{1}{1.5} (0.74)^2 + \frac{1}{2.25} (1.11)^2 = 0.9127$$

Rear Pile Vertical Load = 
$$\left[ \frac{Fy}{1.111} - \frac{\left(M - F_y e\right) 1.11}{0.9127} \right]$$

Front Pile Vertical Load = 
$$\left[ \frac{Fy}{1.111} + \frac{\left( M - F_y e \right) 0.74}{0.9127} \right]$$

## **Group I Pile Design Loads**

Rear Pile Vertical Load = 
$$\left[ \frac{457.4}{1.111} - \frac{\left[ 266 - 457.4 \times 0.185 \right] 1.11}{0.9127} \right] = 191 kN$$

Front Pile Vertical Load = 
$$\left[ \frac{457.4}{1.111} + \frac{\left[ 266 - 457.4 \times 0.185 \right] 0.74}{0.9127} \right] = 559 kN$$

Front Pile Axial Load = 
$$\frac{559}{\cos(20^\circ)}$$
 = 595 kN compression

(Controlling Group 1, non-seismic, axial design load per pile)

A more refined analysis would utilize the vertical stiffness of the batter pile.

# STEP 3 – EVALUATE ALLOWABLE STRUCTURAL CAPACITY OF CASED LENGTH

A single pile design is used that can support the maximum compression load that acts on the front row of battered piles.

For the permanent casing reinforcement, a yield strength of 241 MPa is used for design. To maintain strain compatibility between the reinforcing bar and casing in the upper pile length, a yield strength ( $F_{y\text{-steel}}$ ) of 241 MPa is used for both members. The use of a higher strength casing, such as API N80 ( $F_y = 552$  MPa) would greatly increase the structural capacity of this section of the pile. These calculations do not address the capacity of the casing joint.

If the project incorporated a larger number of piles, savings could be realized by the use of separate designs for the front and rear piles. For example, a smaller casing size and a shorter bond length may be used on the rear piles due to the lower required capacity. The use of separate designs could increase the amount of load testing required at the start of the project, which the potential savings on a larger piling job could support. Consideration must also be given to maintaining simple pile construction. Mixing different reinforcing sizes and pile depths can occasionally lead to errors during pile installation. Also, if the overall stiffness (load versus pile top deflection) of the pile is changed, then the centroid and load per pile must be reevaluated.

## Pile Cased Length Allowable Load

Material dimensions and properties

Casing - Use 141 mm outside diameter x 9.5 mm wall thickness.

Reduce outside diameter by 1.6 mm to account for corrosion.

Casing outside diameter  $OD_{casing} = 141 \text{ mm} - 2 \text{ x } 1.6 \text{ mm} = 137.8 \text{ mm}$ 

Pile casing inside diameter  $ID_{casing} = 141 \text{ mm} - 2 \text{ x } 9.5 \text{ mm} = 122 \text{ mm}$ 

Pile casing steel area  $A_{ca \sin g} = \frac{\pi}{4} \left[ OD^2_{ca \sin g} - ID^2_{ca \sin g} \right] = 3,224 \, mm^2$ 

Casing yield strength  $F_{v-ca\sin g} = 241 \text{MP}a$ 

Radius of gyration 
$$r_{ca \sin g} = \frac{\sqrt{OD^2 + ID^2}}{4} = 46 \, mm$$

Reinforcing bar - Use 43 mm grade 520 steel reinforcing bar.

Bar area 
$$A_{bar} = 1,452 \text{ mm}^2$$

Bar steel yield strength 
$$F_{y-bar} = 520 \text{ MPa}$$

Grout area 
$$A_{grout} = \frac{\pi}{4} ID^2_{ca \sin g} - A_{bar} = 10,240 \text{ mm}^2$$

Grout compressive strength 
$$f'_{c-grout} = 34.5 MPa$$

For strain compatibility between casing and rebar, use for steel yield stress:

$$F_{y\text{-steel}}$$
 = the minimum of  $F_{y\text{-bar}}$  and  $F_{y\text{ casing}}$  = 241 MPa

#### Allowable Tension Load

$$P_{t-allowable} = 0.55 F_{v-steel} (A_{bar} + A_{ca \sin g}) = 620 \, kN$$

## **Allowable Compression Load**

$$P_{c-allowable} = \left[0.4 f_{c-grout}' \times A_{grout} + 0.47 F_{y-steel} \left(A_{bar} + A_{ca \sin g}\right)\right] = 671 kN$$

# STEP 4 – EVALUATE ALLOWABLE STRUCTURAL CAPACITY OF UNCASED LENGTH

## Pile Uncased Length Allowable Load

#### Material dimensions and properties

Soil conditions and the method of pile installation can affect the resulting diameter of the pile bond length. For this example, assume a drill-hole diameter of 50 mm greater than the casing outside diameter (OD).

Using a casing OD = 141mm

Therefore, Grout  $D_b = 141 \text{ mm} + 50 \text{ mm} = 191 \text{ mm}$  (0.191 m)

Bond length grout area 
$$A_{grout} = \frac{\pi}{4} D^2_b - A_{bar} = 27,200 \text{ } mm^2$$

### Allowable Tension Load

$$P_{t-allowable} = 0.55 F_{v-bar} \times A_{bar} = (0.55 \times 520 MPa \times 1,452 mm^2) = 415 kN$$

## Allowable Compression Load

$$\begin{split} P_{c-allowable} &= \left(0.4 \, f_c^{'} \times A_{grout} + 0.47 F_{y-bar} \times A_{bar}\right) \\ P_{c-allowable} &= \left(0.4 \times 34.5 \, MPa \times 27,200 \, mm^2 + 0.47 \times 520 \, MPa \times 1,452 \, mm^2\right) = 730 \, kN \end{split}$$

#### STEP 5 – EVALUATE ALLOWABLE GEOTECHNICAL CAPACITY

### Allowable Load – Geotechnical Capacity

The micropile bond length will be located in the dense to very dense sandy gravel with cobbles and boulders starting approximately 3.35 m below the bottom of footing elevation. The pile bond length shall be installed using a Type B pressure grouting methodology.

From Table 5-3 select an ultimate unit grout-to-ground bond strength  $\alpha_{bond}$  = 265 kPa. This represents an approximate average value for gravels.

The controlling non-seismic micropile loading is 595 kN per pile. Therefore, an allowable geotechnical bond load  $P_{G-allowable} \geq 595$  kN/pile must be provided to support the structural loading.

<u>Provide</u>: P_{G-allowable} ≥ 595 kN/pile

Compute the bond length, L_b, required to provide P_{G-allowable} as follows:

$$L_b = \frac{P_{G-allowable} \times FS}{\alpha_{bond} \times \pi \times D_b}$$

$$L_b = \frac{595 \, kN \times 2.0}{265 \, kPa \times \pi \times 0.191 \, m} = 7.48 \, m$$

Select Bond Length = 7.5 m

$$P_{G-allowable} = \frac{265 \, kPa}{2.0} \times 3.14 \times 0.191 \, m \times 7.5 \, m = 596 \, kN$$

## STEP 6 – VERIFY ALLOWABLE LOADS

The controlling axial design load for the pile is 595 kN (compression). The summary of the pile allowable loads is:

Structural Upper Cased Length = 671 kN (compression)

Structural Lower Uncased Length = 730 kN (compression)

Geotechnical Bond Length = 596 kN (compression)

The allowable loads are all greater than the 595 kN design load, therefore the pile axial design is OK.

The controlling lateral design load is 80.3 kN/m. Check to see if the batter piles carry lateral loads. The front row of piles are battered at 20° from vertical and each pile carries the following ratio of the vertical pile load as a lateral resisting load.

Lateral resisting load =  $559 kN \times \tan(20^\circ) = 204 kN$  per pile

The lateral design load per pile =  $80.3 \frac{kN}{m} \times (1.5m) = 120 \text{ kN per pile}$ 

The lateral resisting load is greater than the lateral design load therefore the pile lateral design is OK.

#### STEP 7 – ESTIMATE MICROPILE SETTLEMENT

Settlements resulting from consolidation of soil layers below the micropile group are not anticipated as these soils are not cohesive in nature. Herein, elastic settlements are calculated.

## **Casing Length Elastic Stiffness**

Front pile batter angle

$$\Phi_{batter} = 20^{\circ}$$

Max pile length from footing to top of gravel

$$L_{upper} = \frac{3.35 \ m}{\cos(\Phi_{batter})} = 3.6 \ m$$

Casing insertion into bond length

$$L_{insert} = 1.0 m$$

Pile casing length

$$L_{ca\sin g} = L_{upper} + L_{insert} = 4.6 \ m$$

Steel modulus of elasticity

$$E_{steel} = 200,000 \ MPa$$

Grout modulus of elasticity

$$E_{grout} = 31,000 MPa$$

Area of Grout

$$A_{crout} = 10,240 \ mm^2$$

$$A_{\text{steel}} = A_{\text{bar}} + A_{\text{casing}} = 1,452 \text{ mm}^2 + 3,224 \text{ mm}^2 = 4,676 \text{ mm}^2$$

Pile compression stiffness value

$$EA_{cased\ length} = A_{crout} \times E_{crout} + A_{steel} \times E_{steel} = 1,252,000\ kN$$

# **Uncased Length Elastic Stiffness**

Pile uncased length (bond length)

$$L_b = 7.5 \text{ m}$$

$$A_{\text{steel}} = A_{\text{bar}} = 1,452 \text{ mm}^2$$

$$A_{grout} = 27,200 \text{ mm}^2$$

Pile compression stiffness value

$$EA_{uncased\ length} = A_{grout} \times E_{grout} + A_{steel} \times E_{steel} = 1,133,000\,kN$$

## **Elastic Displacement**

Elastic displacement (cased length)

$$\Delta t_{elastic} = \frac{P_{compression} \times L_{ca \sin g}}{AE_{cased \ length}} = \frac{595 \, kN \times 4.6 \, m}{1,252,000 \, kN} = 2.2 \, mm$$

Elastic displacement (uncased length)

$$\Delta t_{elastic} = \frac{P_{compression} \times L_b}{AE_{uncased\ length}} = \frac{595 \, kN \times (1/2 \times 7.5 \, m)}{1,133,000 \, kN} = 2.0 \, mm$$

#### STEP 8 – MICROPILE TO FOOTING CONNECTION DESIGN

Design calculations are completed for the detail shown in Figure S1-5 for connection of the pile top to the abutment footing.

# **Required Design Loads and Dimensions**

Group I service load, compression  $P_{c-service} = 595 \text{ kN}$ 

Abutment concrete compressive strength  $f_c = 27.6 \text{ MPa}$ 

Casing outside diameter  $OD_{casing} = 141 \text{ mm}$ 

Pile area  $Area_{pile} = \frac{\pi}{4}OD^2_{ca\sin g} = 15,615 \text{ mm}^2$ 

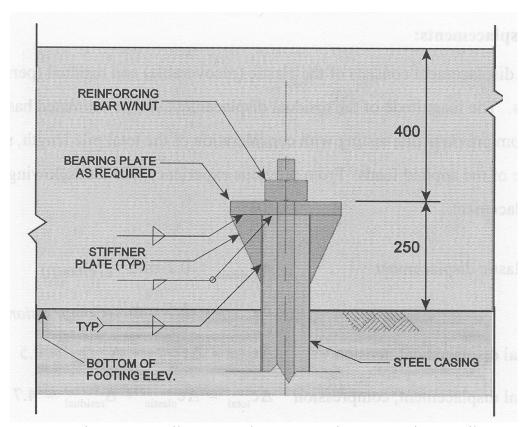
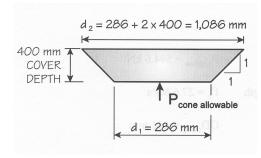


Figure S1-5. Pile Top to Abutment Footing Connection Detail

## **Required Plate Area**

Assume a 254 mm square plate  $Area_{plate} = Plate_{width}^2 = 64,516mm^2$ 

## **Check Cone Shear**



 $P_{cone allowable} \ge P_{c-service} = 595 \text{ kN}$ 

Equivalent diameter for 254 mm² plate, =  $\sqrt{\frac{4 \times 254^2}{\pi}}$  = 286mm

$$A_{CP} = \frac{\pi}{4} \left[ d_2^2 - d_1^2 \right] = \frac{\pi}{4} \left[ 1086^2 - 286^2 \right] = 862,053 \text{ mm}^2$$

Use ACI 349 Appendix B for cone shear

$$P_{\text{cone design strength}} = 4 \varphi \sqrt{f_c' p s i_{CP}} x A_{cp}$$

$$= 4 \varphi \sqrt{f_c' p s i (6.89476) \frac{kPa}{p s i}} x A_{cp}$$

$$= 10.5 \varphi \sqrt{f_c' kPa} \times A_{CP}$$

$$\begin{aligned} \text{P}_{\text{cone nominal strength}} &= 10.5 \ \varphi \ \sqrt{f_c'} \, kPa \times A_{CP} \\ &= 10.5 \ \sqrt{27.6 \ mPa} \left( \frac{1000 kPa}{mPa} \right) \times A_{CP} \times 10^{-6} \\ &= 1,504 \ kN \end{aligned}$$

$$P_{come\ allowable} = rac{P_{come\ noninal\ strength}}{FS}$$

$$FS = \frac{LF}{\varphi}$$

$$LF = Combined \ load \ factor = \frac{\gamma \left[ B_D Q_D + B_L Q_L + B_E Q_E \right]}{\left[ Q_D + Q_L + Q_E \right]}$$

Where: 
$$\gamma = 1.3$$
;  $B_D = 1$ ;  $B_L = 1.67$ ;  $B_E = 1.3$ 

and with 
$$Q_D = 0.62$$
;  $Q_L = 0.16$ ;  $Q_E = 0.22$ 

$$\frac{Q_D}{Q_D + Q_L + Q_E} = 0.62$$

$$\frac{Q_L}{Q_D + Q_L + Q_E} = 0.16$$

$$\frac{Q_E}{Q_D + Q_L + Q_E} = 0.22$$

$$LF = 1.3 [1.0 \times 0.62 + 1.67 \times 0.16 + 1.3 \times 0.22] = 1.53$$

 $\varphi = 0.65$  for unreinforced shear cone per ACI 349 Appendix B

$$FS = \frac{1.53}{0.65} = 2.35$$

$$P_{cone\ allowable} = \frac{1,504\ kN}{2.35} = 640\ kN > 594.6\ kN \dots OK$$

Note – edge distance limitations and other requirements of ACI 349 Appendix B must be satisfied.

## **Required Plate Thickness**

Actual bearing stress, compression 
$$Bearing_{compression} = \frac{P_{c-service}}{Area_{plate}} = 9.22 MPa$$

Plate bending moment for 10 mm width

$$M_{\text{max}} = 10 \text{ mm} \times \frac{1}{2} \left[ \frac{Plate_{width} - OD_{ca \sin g}}{2} \right]^2 \times Bearing_{compression} = 0.147 \text{ kNm}$$

Note - use of this cantilever moment was determined to be a conservative approximation of the maximum moment in the plate due to a compression pile load by comparison to a

more accurate formula shown in Roark and Young (1975). Plate bending from a tension pile load or with different plate support details must be further analyzed.

Allowable bending stress -  $F_v = 345 \text{ MPa}$  and  $F_b = 0.55 F_v$ 

Note - Allowable stresses should be increased by the appropriate % factor (AASHTO Table 3.22.1A column 14) depending on which load group produces controlling load condition. For this example, the Group I load produces the controlling condition (% = 100%).

$$S_{x-req} = \frac{M_{\text{max}}}{F_b} = 775 mm^3$$

Required plate thickness -  $t_{req} = \sqrt{\frac{6 S_{x-req}}{10 mm}} = 21.6 mm$ 

## Use 254 mm square x 25.4 mm thick top plate.

## **Required Weld Size:**

Tensile strength of E70 electrode,  $Fu_{weld} = 483 \text{ MPa}$ 

Minimum tensile strength of connected parts (ASTM A53 Grade B Casing)

$$Fu_{part} = 414 \text{ MPa}$$

Fillet weld strength  $\Phi F = 0.27 F u_{part} = 111.8 MPa$ 

Top weld size  $t_{weld-top} = 6.35mm$ 

Stiffener plate size  $t_{stiff} = 12.7 \text{ mm } W_{stiff} = 100 \text{ mm } L_{stiff} = 150 \text{ mm}$ 

Top weld strength  $L_{weld} = \pi OD_{casimg} - 4t_{stiff} + 8W_{stiff} = 1,190 \text{ mm}$ 

Top weld strength

$$P_{weld-top} = 0.707 \ t_{weld-top} \Phi F L_{weld} = 598 \ kN > 595 \ kN \dots OK$$

Stiffener plate side weld dimensions

$$t_{weld-side} = 6.35mm$$

$$L_{weld} = 8 L_{stiff} = 1,200 mm$$

Stiffener plate side weld strength

$$\begin{split} P_{weld-side} &= 0.707 \ t_{weld-side} \Phi F_{weld} L_{weld} = 603 \ kN \\ &> 0.707 \ t_{weld-top} \Phi F \times 8 \ W_{stiff} = 402 \ kN \ \dots \ OK \end{split}$$

Use 6.35 mm fillet weld for welding top and stiffener plates.

Note - this example ignored bending stresses on the welds which is considered appropriate for a compression pile load with the weld details shown. Weld bending stress must be analyzed for other conditions.

#### STEP 9 – CHECK STRUCTURAL CAPACITY TO RESIST TEST LOADS

The controlling axial design load for the pile is 595 kN (compression).

Verification Test Load = 
$$2.0 \times Design Load$$

$$= 2.0 \times 595 \text{ kN} = 1,190 \text{ kN}$$

Proof Test Load =  $1.6 \times \text{Design Load}$ 

$$= 1.6 \times 595 \text{ kN} = 952 \text{ kN}$$

Cased Length		<b>Uncased Length</b>		
OD*	= 141mm			
ID	= 122 mm (9.5 mm wall)			
A casing	$= 3,925 \text{ mm}^2$	A grout	$= 27,200 \text{ mm}^2$	
$F_{y ext{-casing}}$	= 241 MPa (use for casing and bar)	f'c-grout	= 34.5 MPa	
A bar	$= 1,452 \text{ mm}^2$	$A_{bar}$	$= 1,452 \text{ mm}^2$	
F _{y-bar}	= 520 MPa	F _{y-bar}	= 520 MPa	
A grout	$= 10,240 \text{ mm}^2$			
f'c-grout	= 34.5 MPa			

^{*} Do not reduce by 1.6 mm for corrosion.

## Pile Cased Length Allowable Load

$$P_{c-allowable} = \left[0.68 f'_{c-grout} A_{grout} + \frac{F_{y-ca \sin g}}{1.25} \left(A_{bar} + A_{ca \sin g}\right)\right]$$

$$P_{c-allowable} = \left[0.68 \times 34.5 MPa \times 10,240 \, mm^2 + \frac{241 MPa}{1.25} \left(1,452 \, mm^2 + 3,925 \, mm^2\right)\right] = 1,277 \, kN$$

## Pile Uncased Length Allowable Load

$$\begin{split} P_{c-allowable} &= 0.68 f^{'}{}_{c-grout} A_{grout} + 0.80 F_{y-bar} A_{bar} \\ \\ P_{c-allowable} &= 0.68 \times 34.5 \, MPa \times 27,200 \, mm^2 \\ &+ 0.80 \times 520 \, MPa \times 1,452 \, mm^2 = 1,242 \, kN \end{split}$$

The design pile is OK for the proof test at 952 kN and the verification test at 1,190 kN.

## STEP 10 - PREPARE DRAWINGS

The following detail drawings (Figures S1-6 and S1-7) show the pile design.

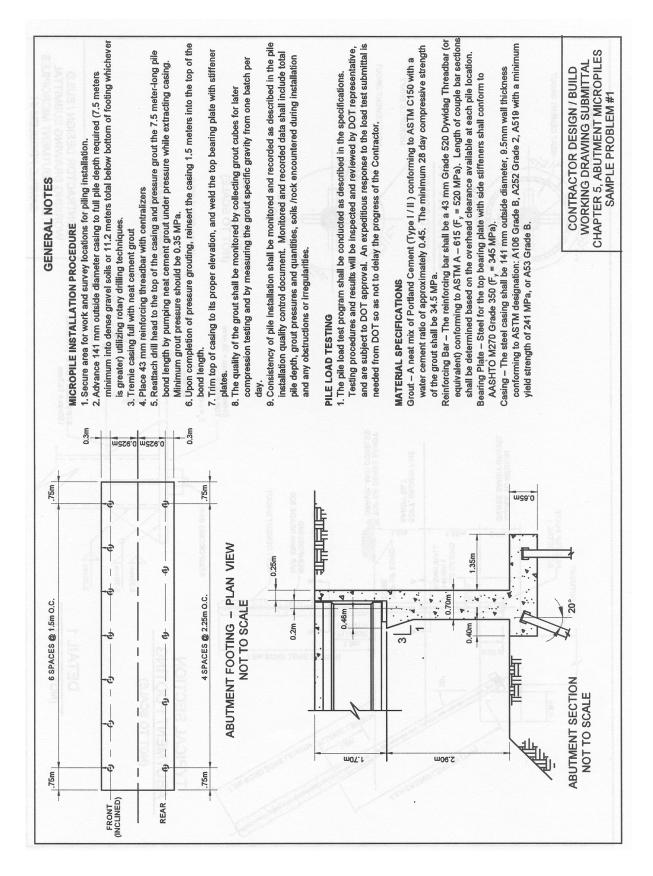


Figure S1-6. Page 1 of Sample Problem No.1 – Working Drawing Submittal

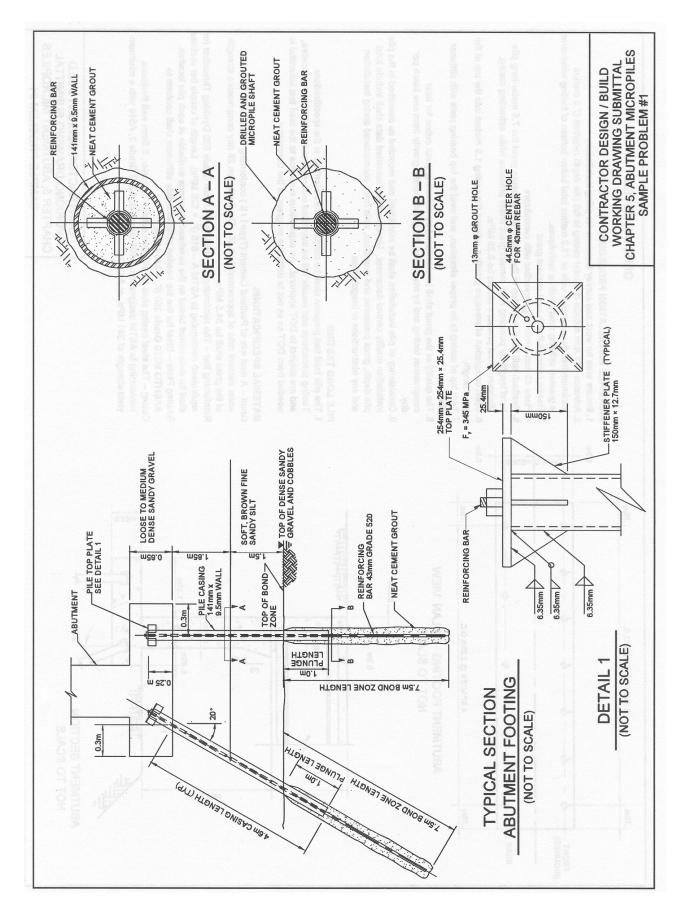


Figure S1-7. Page 2 of Sample Problem No. 1 – Working Drawing Submittal

#### SAMPLE PROBLEM NO. 2 – LATERALLY LOADED MICROPILE

Micropiles are being considered to support loads for a new multi-story building. The site is underlain by approximately 6 m of undocumented and variable fill overlying partially weathered rock. The soil matrix of the fill is characterized as loose to very dense silty to clayey sand. Approximately 3 m of new fill will be placed over the existing fill to establish foundation grades.

The micropile section shown in Figure S2-1 is proposed for the project. The micropiles are required to carry a design axial compression load of 1,423 kN and a design lateral groundline shear load of 44.48 kN.

Perform a laterally loaded pile analysis and evaluate:

- 1. structural capacity of the cased length of the micropile
- 2. reduced section modulus of the casing joint and proposed bending moment limit at the casing joints

## **Micropile Section Properties**

- 1. Casing outside diameter (OD) = 0.1969 m.
- 2. Casing wall thickness  $(t_w) = 0.0151 \text{ m}.$
- 3. Casing yield strength  $(F_v) = 552 \text{ MPa}$
- 4. Grout compressive strength  $(f'_c) = 27.6 \text{ MPa}$

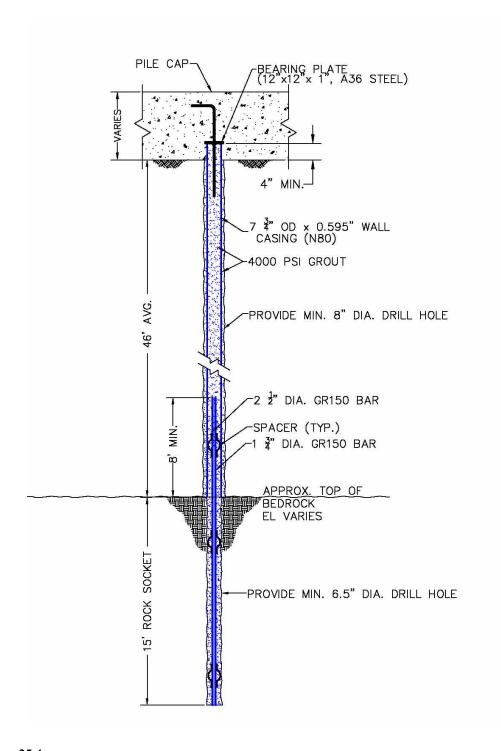
Determine: (1) casing area,  $A_{casing}$ ; (2) casing moment of inertia,  $I_{casing}$ ; (3) casing section modulus,  $S_{casing}$ ; and (4) area of grout,  $A_{grout}$ .

$$A_{ca\sin g} = \frac{\pi}{4} \left( OD^2 - ID^2 \right) = \frac{\pi}{4} \left( 0.1969^2 m^2 - \left( 0.1969 - 2(0.0151) \right)^2 m^2 \right) = 0.00863 m^2$$

$$I_{ca\sin g} = \frac{\pi}{64} \left( OD^4 - ID^4 \right) = \frac{\pi}{64} \left( 0.1969^4 in.^4 - \left( 0.1969 - 2(0.0151) \right)^4 m.^4 \right) = 0.00003587 m^4$$

$$S_{ca\sin g} = \frac{I_{ca\sin g}}{OD/2} = \frac{0.00003587 \, m.^4}{(0.1969 \, m/2)} = 0.000364 \, m^3$$

$$A_{grout} = \frac{\pi}{4}(OD^2) - A_{ca\sin g} = \frac{\pi}{4}(0.1969^2 m^2) - 0.00863 m^2 = 0.0218 m^2$$



1 in. = 25.4 mm 1 ksi = 6.89 MPa

Figure S2-1. Micropile Detail for Sample Problem 2.

#### **Laterally Loaded Pile Analysis**

The computer program LPILE is used to evaluate the maximum bending moment in the cased length of the micropile. For the purposes of this example, both 50% fixity and fixed head (100% fixity) conditions are analyzed. The micropile cap will be embedded 0.91 m below the ground surface. For the analysis, a 0.305-m embedment depth was conservatively assumed.

For the analysis, a 12.2-m length of the micropile was modeled. Default LPILE p-y curves for sand above the water table were used to model the soil profile. The upper 3.35 m of the profile was modeled with a soil friction angle of 32 degrees and the remaining portion of the profile (representing the existing fill layer) was modeled with a soil friction angle of 30 degrees. Other soil parameters are provided in the LPILE output file.

## **LPILE Analysis Results**

The results of the LPILE analysis are provided below and the bending moment diagram and lateral deflection profile are provided in Figures S2-2 and S2-3.

Axial Load (kN)	Fixity Condition	Pile Head Deflection (mm)	Maximum Shear Load (kN)	Maximum Bending Moment (kN-m)
1,423	100%	3.3	44.48	-37.3
1,423	50%	8.4	44.48	27.2

## **Structural Capacity Evaluation (Eq. 5-3)**

$$\frac{f_a}{F_a} + \frac{f_b}{\left(1 - \frac{f_a}{F_e'}\right)} F_b \leq 1.0$$

Where

$$f_a = \frac{P_c}{A_{ca \sin g}} = \frac{1,423 \, kN}{0.00863 \, m^2} = 164.89 \, MPa$$

$$f_b = \frac{M_{\text{max}}}{S_{ca \sin a}} = \frac{37.3 \, kN - m}{0.000364 \, m^3} = 102.47 \, MPa$$

$$F_a = 0.47 F_y = 0.47 (552 MPa) = 259.44 MPa$$
  
 $F_b = 0.55 F_y = 0.55 (552 MPa) = 303.6 MPa$ 

Assume buckling potential is negligible,  $F'_e >>> f_a$ 

Therefore,

$$\frac{164.89 MPa}{259.44 MPa} + \frac{102.47 MPa}{303.6 MPa} = 0.97 < 1.0 OK$$

## **Structural Capacity Evaluation (Eq. 5-6)**

$$\frac{P_c}{P_{c-allowable}} + \frac{M_{\text{max}}}{M_{allowable}} \le 1.0$$

Where

$$P_{c-allowable} = \left[0.4 f_c' \times A_{grout} + 0.47 F_y A_{ca \sin g}\right]$$
  
= 0.4(27.6 MPa)(0.0218 m²)+0.47(552 MPa)(0.00863 m²)=2,479 kN

$$M_{allowable} = 0.55 F_v S_{ca \sin g} = 0.55 (552 MPa) (0.000364 m^3) = 110.5 kN - m.$$

Therefore,

$$\frac{1,423 \, kN}{2,479 \, kN} + \frac{37.3 \, kN - m}{110.5 \, kN - m} = 0.91 < 1.0 \quad OK$$

#### Section Modulus at the Joint (Eq. 5-26)

$$S_{jo \text{ int}} = \frac{I_{jo \text{ int}}}{(OD - t_w)/2} = \frac{\frac{\pi}{64} ((OD - t_w)^4 - ID^4)}{(OD - t_w)/2} = \frac{\frac{\pi}{64} ((0.1969 \, m - 0.0151 \, m)^4 - (0.1667 \, m^4)}{(0.1969 \, m - 0.0151 \, m)/2} = 0.000173 \, m^3$$

## Maximum Bending Moment at the Joint (Eq. 5-27)

$$M_{\max(jo\,\text{int})} = S_{jo\,\text{int}} \times \left(1 - \frac{f_a}{F_a}\right) \times \left(1 - \frac{f_a}{F_e}\right) F_b = 0.000173\,\text{m}^3 \times \left(1 - \frac{164.89\,\text{MPa}}{259.44\,\text{MPa}}\right) \times 303.6\,\text{MPa} = 19.2\,\text{kN} - \text{m}$$

Using the reduced section modulus at a joint indicates that the combined stress criterion can only be satisfied at the location of a threaded connection (i.e., joint) if the maximum

bending moment is 19.2 kN-m or less. This result indicates that threaded connections should not be placed from the bottom of the pile cap to approximately 0.5 m below the ground surface where the micropile-footing connection achieves 100% fixity. For the 50% fixity condition, positive bending moments greater than 19.2 kN-m are computed between a depth of approximately 0.75 to 2.1 m.

Alternatively, if the maximum bending moment needs to be resisted over these depths, the following options could be considered: (1) use a larger casing (with a larger cross sectional area of steel) over this depth range; or (2) place an additional steel casing at least over this length. On projects where a second casing is used, the design should require that joints from the two casings be staggered by at least 1 m.

For the 50% fixity case, a 3-m long casing could be used at the ground surface so that the first threaded connection would be located in an area where acceptable bending resistance could be developed.

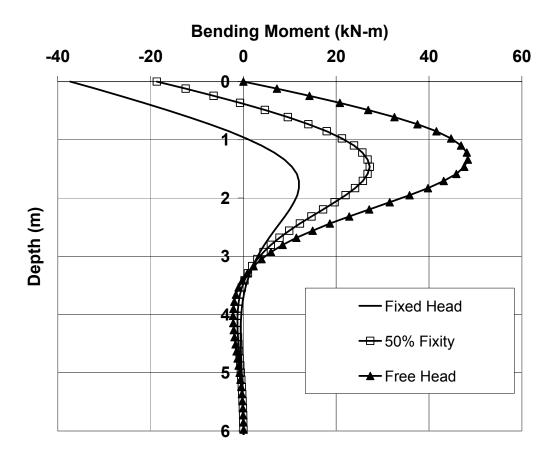


Figure S2-2. Bending Moment Diagram for Sample Problem No. 2.

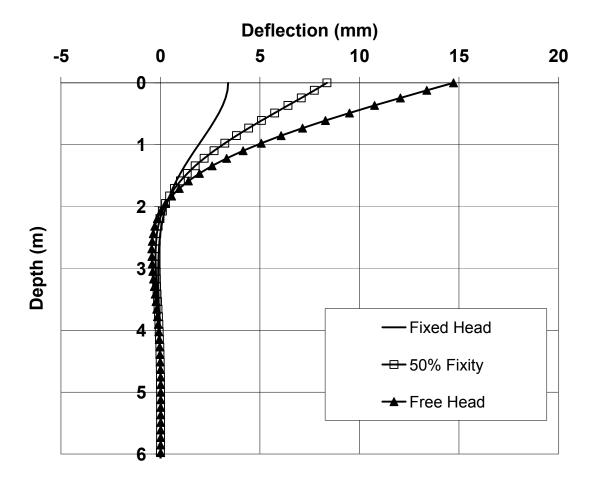


Figure S2-3. Lateral Deflection Profile for Sample Problem No. 2.

# LPILE ANALYSIS RESULTS

**FOR** 

**SAMPLE PROBLEM 2** 

LPILE Plus for Windows, Version 4.0 (4.0.8)

Analysis of Individual Piles and Drilled Shafts
Subjected to Lateral Loading Using the p-y Method

(c) Copyright ENSOFT, Inc., 1985-2003 All Rights Reserved

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This program is licensed to:

Paul Sabatini GeoSyntec

Path to file locations: G:\CWP\CHE8123 - NHI Micropiles\400 - Technical\402 -

Revised Manual\Draft 100% Manual\Ch. 5\LPILE Analysis\

Name of input data file: 004SI.lpd
Name of output file: 004SI.lpo
Name of plot output file: 004SI.lpp
Name of runtime file: 004SI.lpp

______

Time and Date of Analysis

-----

Date: May 24, 2005 Time: 16:51:45

Problem Title

FIODIEM IICIE

Micropile Manual - Sand Profile

-----

Program Options

Units Used in Computations - SI Units, meters, kilopascals

Basic Program Options:

Analysis Type 3:

- Computation of Nonlinear Bending Stiffness and Ultimate Bending Moment Capacity with Pile Response Computed Using Nonlinear EI

Computation Options:

- Only internally-generated p-y curves used in analysis
- Analysis does not use p-y multipliers (individual pile or shaft action only)
- Analysis assumes no shear resistance at pile tip
- Analysis includes automatic computation of pile-top deflection vs. pile embedment length
- No computation of foundation stiffness matrix elements
- Output pile response for full length of pile
- Analysis assumes no soil movements acting on pile
- Additional p-y curves computed at specified depths

Solution Control Parameters:

- Number of pile increments = 100 - Maximum number of iterations allowed = 100 - Deflection tolerance for convergence = 2.5400E-07 m - Maximum allowable deflection = 2.5400E+00 m

## Printing Options:

- Values of pile-head deflection, bending moment, shear force, and soil reaction are printed for full length of pile.
- Printing Increment (spacing of output points) = 1

_____

## Pile Structural Properties and Geometry

______

Pile Length = 12.19 m

Depth of ground surface below top of pile = -.30 m

Slope angle of ground surface = .00 deg

Structural properties of pile defined using 2 points

Point	Depth	Pile	Moment of	Pile	Modulus of
	X	Diameter	Inertia	Area	Elasticity
	m	m	m**4	Sq. m	kN/Sq. m
1	0.0000	.19685000	3.58667E-05	.008626	199947980.000
2	14.5000	.19685000	3.58667E-05	.008626	199947980.000

Please note that because this analysis makes computations of ultimate moment capacity and pile response using nonlinear bending stiffness that the above values of moment of inertia and modulus of are not used for any computations other than total stress due to combined axial loading and bending.

______

Soil and Rock Layering Information

The soil profile is modelled using 2 layers

Layer 1 is sand, p-y criteria by Reese et al., 1974 Distance from top of pile to top of layer = -.305 m Distance from top of pile to bottom of layer = 3.048 m p-y subgrade modulus k for top of soil layer = 24430.244 kN/ m**3 p-y subgrade modulus k for bottom of layer = 24430.244 kN/ m**3

Layer 2 is sand, p-y criteria by Reese et al., 1974 Distance from top of pile to top of layer = 3.048 m Distance from top of pile to bottom of layer = 12.192 m p-y subgrade modulus k for top of soil layer = 16286.830 kN/ m**3 p-y subgrade modulus k for bottom of layer = 16286.830 kN/ m**3

(Depth of lowest layer extends .00 m below pile tip)

Effective Unit Weight of Soil vs. Depth

Distribution of effective unit weight of soil with depth is defined using  $\ 4$  points

Point	Depth X	Eff. Unit Weight
No.	m	kN/ m**3
1	30	18.83843
2	3.05	18.83843
3	3.05	17.64407
4	12.19	17.64407

#### ______

#### Shear Strength of Soils

Distribution of shear strength parameters with depth defined using 4 points

Point No.	Depth X m	Cohesion c kN/ m**2	Angle of Friction Deq.	E50 or k rm	RQD %
		KN/ III Z	Deg.		
1	305	.00000	32.00		
2	3.048	.00000	32.00		
3	3.048	.00000	30.00		
4	12.192	.00000	30.00		

#### Notes:

- (1) Cohesion = uniaxial compressive strength for rock materials.
- (2) Values of E50 are reported for clay strata.
- (3) Default values will be generated for E50 when input values are 0. (4) RQD and  $k_r$ m are reported only for weak rock strata.

Loading Type ______

Static loading criteria was used for computation of p-y curves

Pile-head Loading and Pile-head Fixity Conditions

Number of loads specified = 5

Load Case Number 1

Pile-head boundary conditions are Shear and Slope (BC Type 2)

Shear force at pile head = 44.482 kNSlope at pile head = .000 m/mSlope at pile head = Axial load at pile head = 1423.431 kN

(Zero slope for this load indicates fixed-head condition)

Load Case Number 2

Pile-head boundary conditions are Shear and Moment (BC Type 1)

Shear force at pile head = 44.482 kN

Bending moment at pile head = .000 m- kN

Axial load at pile head = 1423.431 kN

(Zero moment at pile head for this load indicates a free-head condition)

Load Case Number 3

Pile-head boundary conditions are Shear and Rotational Stiffness (BC Type 3)

Shear force at pile head = 44.482 kN Rotational stiffness = 88964.449 m-Axial load at pile head = 1423.431 kN 88964.449 m- kN

Load Case Number 4

Pile-head boundary conditions are Shear and Rotational Stiffness (BC Type 3)

Shear force at pile head = 44.482 kNRotational stiffness = 889644.490 m- kNAxial load at pile head = 1423.431 kN

#### Load Case Number 5

Non-zero moment at pile head for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment) condition.

Output of p-y Curves at Specified Depths

p-y curves are generated and printed for verification at 7 depths.

Depth No.	Depth Below Pile Head m	Depth Below Ground Surface m
1	.000	.305
2	2.020	2.325
3	4.690	4.995
4	4.710	5.015
5	9.990	10.295
6	10.010	10.315
7	12.192	12.497

Depth of ground surface below top of pile = -.30 m

An unreasonable input value for yield strength of reinforcing steel has been specified. The input value is either smaller than 262,000 kN/m2 or larger than 551,600 kN/m2. You should check you input for correctness.

```
**** WARNING ****
```

An unreasonable input value for concrete cover thickness has been specified. The input value is either smaller than 0.02 meters or larger than 0.2 meters. You should check your input for correctness.

Computations of Ultimate Moment Capacity and Nonlinear Bending Stiffness

#### Pile Description:

The sectional shape is a circular shaft with steel casing.

```
Outside Diameter = .1969 m Wall thickness of steel shell = .0151 m Cross-sectional area of shell = .00863 m**2 Moment of inertia of steel shell = 3.58702E-05 m**4
```

## Material Properties:

```
Compressive Strength of Concrete = 27579.034 kN/ m**2
Yield Stress of Reinforcement = 27579. kN/ m**2
Steel shell or core yield stress = 551581. kN/ m**2

Modulus of Elasticity of Reinforcement = 199948000. kN/ m**2
Cover Thickness (edge to bar center) = .000 m
```

Number of Reinforcing Bars = 1 Area of Single Bar = .00000 m**2 Number of Rows of Reinforcing Bars = 1 Ultimate Axial Squash Load Capacity = 5270.58 kN

Distribution and Area of Steel Reinforcement

Row	Area of	Distance to
Number	Reinforcement	Centroidal Axis
	m**2	m
1	.000000	.0000

Axial Thrust Force = .00 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
1.61543650	8206.417	.00019685	.00001640	.09842200
2.90699392	8204.183	.00035433	.00002952	.09842200
4.19784752	8201.948	.00051181	.00004264	.09842200
5.48799731	8199.714	.00066929	.00005576	.09842200
6.77744329	8197.479	.00082677	.00006888	.09842200
8.06618545	8195.244	.00098425	.00008200	.09842200
9.35422380	8193.010	.00114173	.00009512	.09842200
10.642	8190.775	.00129921	.00010824	.09842200
10.924	7499.209	.00145669	.00011327	.09287117
12.105	7499.108	.00161417	.00012553	.09288319
13.286	7499.006	.00177165	.00013780	.09289520
14.466	7498.500	.00192913	.00015006	.09290121
15.646	7498.397	.00208661	.00016234	.09291322
16.827	7498.295	.00224409	.00017462	.09292524
18.007	7498.192	.00240157	.00018690	.09293725
19.187	7497.684	.00255906	.00019917	.09294326
20.367	7497.581	.00271654	.00021146	.09295528
21.548	7497.478	.00287402	.00022375	.09296729
22.728	7497.375	.00303150	.00023605	.09297931
23.907	7496.866	.00318898	.00024833	.09298531
25.088	7496.762	.00334646	.00026064	.09299733
26.268	7496.658	.00350394	.00027294	.09300934
27.448	7496.554	.00366142	.00028526	.09302136
28.628	7496.450	.00381890	.00029757	.09303337
29.807	7495.940	.00397638	.00030986	.09303938
38.654 47.499	7494.751 7493.562	.00515748	.00040234	.09312348
56.340	7492.380	.00751969	.00058788	.09329169
65.179	7491.214	.00870079	.00058788	.09337579
74.016	7490.072	.00988189	.00077422	.09345990
82.855	7489.387	.01106299	.00077422	.09355001
91.693	7488.762	.01224409	.00096149	.09364012
100.537	7488.652	.01342520	.00105553	.09373624
109.382	7488.664	.01460630	.00114980	.09383235
118.136	7482.927	.01578740	.00124306	.09385038
126.884	7477.638	.01696850	.00133646	.09387441
135.737	7478.784	.01814961	.00143145	.09398254
144.598	7480.243	.01933071	.00152669	.09409067
153.504	7483.692	.02051181	.00162256	.09421683
162.450	7488.599	.02169291	.00171886	.09434899
171.554	7499.959	.02287402	.00181643	.09452320
181.768	7556.318	.02405512	.00192092	.09496775
190.497	7548.547	.02523622	.00201690	.09503383
199.203	7540.624	.02641732	.00211304	.09509991
207.887	7532.571	.02759843	.00220867	.09514196
216.202	7512.356	.02877953	.00230320	.09514196
223.884	7472.618	.02996063	.00239574	.09507588
228.487	7337.017	.03114173	.00247204	.09449317
232.667	7198.231	.03232283	.00254929	.09398254
236.784	7067.337	.03350394	.00263238	.09368217

240.174	6924.418	.03468504	.00271455	.09337579
243.147	6779.298	.03586614	.00279815	.09312949
245.703	6632.145	.03704724	.00288206	.09290722
247.960	6486.275	.03822835	.00296751	.09273901
250.011	6343.943	.03940945	.00305375	.09260084
251.825	6204.036	.04059055	.00313918	.09245066
253.433	6067.107	.04177165	.00322600	.09234252
254.956	5935.730	.04295276	.00331258	.09223439
256.253	5806.259	.04413386	.00339969	.09214428
257.514	5682.756	.04531496	.00348631	.09204816
258.584	5561.408	.04649606	.00357383	.09197607
259.626	5445.491	.04767717	.00366089	.09189798
266.840	5461.521	.04885827	.00374982	.09186193
267.799	5351.757	.05003937	.00384047	.09186193

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 248.732 m- kN

Axial Thrust Force = 444.82 kN

Bending Moment kN-m	Bending Stiffness kN-m2	Bending Curvature rad/m	Maximum Strain m/m	Neutral Axis Position m
1.59641069	8109.766	.00019685	.00021404	1.10243780
2.87353417	8109.752	.00035433	.00022719	.65629032
4.15065210	8109.736	.00051181	.00024034	.48470288
5.42776291	8109.716	.00066929	.00025350	.39387121
6.70486558	8109.694	.00082677	.00026666	.33764809
7.98195810	8109.669	.00098425	.00027983	.29942310
9.25904000	8109.642	.00114173	.00029301	.27174708
10.536	8109.610	.00129921	.00030619	.25078731
11.813	8109.575	.00145669	.00031938	.23436312
13.090	8109.543	.00161417	.00033256	.22114086
14.367	8109.501	.00177165	.00034577	.21027951
15.644	8109.460	.00192913	.00035897	.20119034
16.933	8114.997	.00208661	.00037169	.19324257
18.216	8117.216	.00224409	.00038490	.18662843
19.414	8083.775	.00240157	.00039833	.18097548
20.715	8094.734	.00255906	.00041140	.17587521
21.918	8068.234	.00271654	.00042454	.17139370
23.319	8113.629	.00287402	.00043745	.16732070
24.592	8112.165	.00303150	.00045098	.16387847
25.869	8112.108	.00318898	.00046422	.16068254
26.853	8024.180	.00334646	.00047669	.15755870
27.976	7984.229	.00350394	.00048897	.15466314
29.265	7992.743	.00366142	.00050220	.15227220
30.576	8006.552	.00381890	.00051480	.14991730
31.519	7926.605	.00397638	.00052712	.14767655
40.618	7875.591	.00515748	.00062325	.13595614
49.161	7755.812	.00633858	.00071659	.12816456
58.415	7768.317	.00751969	.00081316	.12325052
66.923	7691.622	.00870079	.00090617	.11926162
75.868	7677.494	.00988189	.00100140	.11645016
85.876	7762.426	.01106299	.00110135	.11466597
92.645	7566.527	.01224409	.00118687	.11204675
103.624	7718.590	.01342520	.00129208	.11135590
110.324	7553.198	.01460630	.00137732	.10940950
118.090	7479.987	.01578740	.00147068	.10826810
130.093	7666.740	.01696850	.00157887	.10815997
136.846	7539.876	.01814961	.00166478	.10683834
144.490	7474.616	.01933071	.00175488	.10589518
152.218	7420.983	.02051181	.00184584	.10510221
160.622	7404.371	.02169291	.00194965	.10498807
169.126	7393.816	.02287402	.00205580	.10498807
182.567 188.707	7589.521 7477.637	.02405512	.00215675	.10477180 .10381062
196.615	7442.638	.02641732	.00233268	.10341413

204.416	7406.814	.02759843	.00242603	.10301765
212.036	7367.603	.02877953	.00252277	.10277134
219.353	7321.374	.02996063	.00262432	.10270526
226.068	7259.311	.03114173	.00273039	.10278937
231.848	7172.897	.03232283	.00283997	.10297559
236.792	7067.588	.03350394	.00295038	.10317384
241.025	6948.953	.03468504	.00306085	.10336007
244.630	6820.653	.03586614	.00317025	.10350424
247.638	6684.389	.03704724	.00327777	.10358835
250.262	6546.509	.03822835	.00338410	.10363641
252.618	6410.091	.03940945	.00349103	.10369648
254.611	6272.667	.04059055	.00359565	.10369648
256.423	6138.679	.04177165	.00370028	.10369648
258.080	6008.462	.04295276	.00380594	.10372051

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 238.693 m- kN

Axial Thrust Force = 1645.84 kN

Bending	Bending	Bending	Maximum	Neutral Axis
Moment	Stiffness	Curvature	Strain	Position
kN-m	kN-m2	rad/m	m/m	m
Moment	Stiffness	Curvature	Strain	Position
94.717	7735.752	.01224409	.00179186	.16145749
103.868	7736.770	.01342520	.00189309	.15612293
112.002	7668.060	.01460630	.00198917	.15129900
122.167	7738.241	.01578740	.00209217	.14763450
130.935 139.679 146.230 155.542 162.189 170.646 175.764 180.600 188.135	7716.336 7695.962 7564.663 7583.033 7476.597 7460.258 7306.735 7156.368 7121.651	.01696850 .01814961 .01933071 .02051181 .02169291 .02287402 .02405512 .02523622 .02641732	.00219303 .00228615 .00238336 .00248623 .00259016 .00269161 .00279548 .00293046 .00304746	.14703436 .14435446 .14107443 .13840715 .13632259 .13451437 .13278424 .13132445 .13123433 .13047140

```
      191.931
      6954.404
      .02759843
      .00316879
      .12993073

      195.595
      6796.323
      .02877953
      .00329230
      .12951021

      199.081
      6644.766
      .02996063
      .00341967
      .12925190

      202.390
      6499.001
      .03114173
      .00355037
      .12911973

      205.538
      6358.908
      .03232283
      .00368405
      .12908970

      208.542
      6224.398
      .03350394
      .00382068
      .12914977
```

Ultimate Moment Capacity at a Concrete Strain of 0.003 = 185.078 m- kN

p-y Curve in Sand Computed Using Reese Criteria

```
Soil Layer Number =
Depth below pile head =
Depth below ground surface =
Equivalent Depth (see note) =
                                                .000 m
.305 m
.305 m
Pile Diameter = .197 m

Angle of Friction = 32.000 deg.

Avg. Eff. Unit Weight = 18.83843 kN/ m**3

k = 24430.244 kN/m3
                                               1.7329
A (static)
                                                 1.2487
B (static)
Pst
                                                  7.324 kN/ m
Psd
                                      =
                                                 41.611 kN/ m
                                                 7.324 kN/ m
12.692 kN/ m
Ps
                                      _
pu
                                       =
                                              53.9219
Cbar
                                       =
                                                  3.2237
n
                                       =
                                               864.7227
m
                                                  .0008
                                       =
уk
уm
                                       =
                                                   .0033 m
                                                   .0074
yu
                                                              m
                                               1.00000
p-multiplier
y-multiplier
                                               1.00000
```

If  $\operatorname{Psd} \mathrel{<=} \operatorname{Pst}$  then actual depth is used in place of equivalent depth in computations.

у, m	p, kN/m
.0000	.000
.0003	2.036
.0005	4.072
.0008	5.949
.0011	6.504
.0014	6.971
.0016	7.376
.0019	7.737
.0022	8.065
.0025	8.365
.0027	8.643
.0030	8.902
.0033	9.146
.0074	12.692
.2042	12.692
.4011	12.692
.5979	12.692

p-y Curve in Sand Computed Using Reese Criteria

```
Soil Layer Number = 1
Depth below pile head = 2.020 m
Depth below ground surface = 2.325 m
Equivalent Depth (see note) = 2.325 m
Pile Diameter = .197 m
```

```
Angle of Friction = 32.000 deg.

Avg. Eff. Unit Weight = 18.83843 \text{ kN/m**3}

k = 24430.244 \text{ kN/m3}
                                        .8800
A (static)
                                           .5000
B (static)
                                =
                                      257.686 kN/ m
317.379 kN/ m
Pst
                                =
Psd
                                =
                                       257.686 kN/ m
Ps
                                        226.764 kN/ m
pu
Cbar
                                =
                                      4171.9895
                                         1.6447
n
                                     23877.0680
                                      .0013
yk
                                                    m
ym
                                =
                                           .0033
                                                    m
                                           .0074
yu
                                                    m
                                         1.00000
p-multiplier
                                =
y-multiplier
                                         1.00000
```

If Psd  $\mathrel{<=}$  Pst then actual depth is used in place of equivalent depth in computations.

y, m p, kN/m	ı
.0000 .000	
.0003 15.528	
.0005 31.056	
.0008 46.584	
.0011 62.112	
.0014 75.665	
.0016 84.535	
.0019 92.841	
.0022 100.693	
.0025 108.168	
.0027 115.324	
.0030 122.204	
.0033 128.843	
.0074 226.764	
.2042 226.764	
.4011 226.764	
.5979 226.764	

p-y Curve in Sand Computed Using Reese Criteria

```
Depth below pile head = 4.690 m

Depth below ground surface = 4.995 m

Equivalent Depth (see note) = 5.449 m

Pile Diameter = .197 m

Angle of Friction = 30.000 deg.

Avg. Eff. Unit Weight = 18.44579 kN/ m**3

k = 16286.830 kN/m²
Soil Layer Number
                                                .8800
A (static)
                                         =
B (static)
                                                       .5000
                                                1099.854 kN/ m
Pst
Psd
                                                   521.333 kN/ m
                                                  521.333 kN/ m
Ps
                                          =
                                                  458.773 kN/ m
                                         =
                                                8440.4724
Cbar
                                                    1.6447
n
                                         =
                                               48306.3849
m
уk
                                         =
                                                    .0025
                                                       .0033
уm
                                                                  m
                                         =
                                                       .0074
yu
                                                                  m
p-multiplier
                                                  1.00000
                                                  1.00000
y-multiplier
```

If Psd <= Pst then actual depth is used in place of equivalent depth in computations.

у <b>,</b> т	p, kN/ m
.0000	.000
.0003	24.265
.0005	48.529
.0008	72.794
.0011	97.058
.0014	121.323
.0016	145.587
.0019	169.852
.0022	194.116
.0025	218.381
.0027	233.315
.0030	247.235
.0033	260.666
.0074	458.773
.2042	458.773
.4011	458.773
.5979	458.773

p-y Curve in Sand Computed Using Reese Criteria

```
p-y Curve in Sand Computed:

Soil Layer Number = 2
Depth below pile head = 4.710 m
Depth below ground surface = 5.015 m
Equivalent Depth (see note) = 5.469 m
Pile Diameter = .197 m
Angle of Friction = 30.000 deg.
Avg. Eff. Unit Weight = 18.44260 kN/ m**3
k = 16286.830 kN/m3
= .8800
 B (static)
                                                                .5000
                                                       1107.556 kN/ m
                                                =
 Pst.
 Psd
                                                         523.330 kN/ m
                                                          523.330 kN/ m
 Ps
                                                _
                                                           460.530 kN/ m
 pu
                                                =
 Cbar
                                                     8472.8005
                                                =
                                                            1.6447
 n
 m
                                                       48491.4045
                                                             .0025
 уk
                                                                          m
 уm
                                                _
                                                               .0033 m
                                                               .0074
 yu
                                                                             m
                                                          1.00000
 p-multiplier
 y-multiplier
                                                          1.00000
```

If Psd <= Pst then actual depth is used in place of equivalent depth in computations.

у, m	p, kN/m
.0000 .0003 .0005 .0008 .0011 .0014 .0016 .0019 .0022 .0025 .0027	.000 24.354 48.707 73.061 97.414 121.768 146.122 170.475 194.829 219.183 234.209 248.182 261.665
.0074	460.530

.2042	460.530
.4011	460.530
5979	460 530

p-y Curve in Sand Computed Using Reese Criteria

```
Soil Layer Number = 2
Depth below pile head = 9.990 m
Depth below ground surface = 10.295 m
Partivalent Depth (see note) = 10.749 m
197 m
                                                      9.990 m
Equivalent Depth (see note) = 10.1

Pile Diameter = 197 m

Angle of Friction = 30.000 deg.

Avg. Eff. Unit Weight = 18.03305 kN/m

= 16286.830 kN/m3
                                                  18.03305 kN/ m**3
                                                    .8800
A (static)
                                          =
B (static)
                                          =
                                                         .5000
                                                  4085.048 kN/ m
1050.477 kN/ m
Pst
Psd
                                                  1050.477 kN/ m
Ps
                                                     924.420 kN/ m
pu
Cbar
                                           =
                                                17007.4142
                                                     1.6447
n
                                                 97336.5779
                                                    .0026
                                           =
уk
                                                                    m
уm
                                           =
                                                        .0033
                                                                    m
                                                        .0074
yu
                                                                    m
p-multiplier
                                           =
                                                     1.00000
y-multiplier
                                                     1.00000
```

If Psd  $\mathrel{<=}$  Pst then actual depth is used in place of equivalent depth in computations.

y, m	p, kN/m
.0000	.000
.0003	47.865
.0005	95.729
.0008	143.594
.0011	191.459
.0014	239.324
.0016	287.188
.0019	335.053
.0022	382.918
.0025	430.783
.0027	470.126
.0030	498.174
.0033	525.239
.0074	924.420
.2042	924.420
.4011	924.420
.5979	924.420

p-y Curve in Sand Computed Using Reese Criteria

```
Soil Layer Number = 2
Depth below pile head = 10.010 m
Depth below ground surface = 10.315 m
Equivalent Depth (see note) = 10.769 m
Pile Diameter = .197 m
Angle of Friction = 30.000 deg.
Avg. Eff. Unit Weight = 18.03229 kN/ m**3 k = 16286.830 kN/m3
A (static) = .8800
B (static) = .5000
```

```
Pst
                                  4099.902 kN/ m
                                    1052.474 kN/ m
1052.474 kN/ m
                             =
Psd
Ps
                                     926.177 kN/ m
                             =
pu
Cbar
                             =
                                  17039.7421
                                      1.6447
                             =
n
                             =
                                  97521.5966
m
                                      .0026
yk
                                       .0033
уm
                                               m
yu
                                        .0074
p-multiplier
                                     1.00000
                                     1.00000
y-multiplier
```

If  $\operatorname{Psd} \mathrel{<=} \operatorname{Pst}$  then actual depth is used in place of equivalent depth in computations.

у <b>,</b> т	p, kN/m
.0000	.000
.0003	47.954
.0005	95.908
.0008	143.861
.0011	191.815
.0014	239.769
.0016	287.723
.0019	335.677
.0022	383.630
.0025	431.584
.0027	471.020
.0030	499.121
.0033	526.237
.0074	926.177
.2042	926.177
.4011	926.177
.5979	926.177

p-y Curve in Sand Computed Using Reese Criteria

```
Soil Layer Number
Soil Layer Number - 2
Depth below pile head = 12.192 m
Depth below ground surface = 12.497 m
Equivalent Depth (see note) = 12.951 m
Equivalent Depth (see note) = 12.001 ...
Pile Diameter = .197 m

Angle of Friction = 30.000 deg.

Avg. Eff. Unit Weight = 17.96451 kN/ m**3

16286.830 kN/m3
                                                      .8800
A (static)
B (static)
                                         =
                                                       .5000
Pst
                                                  5882.580
                                                                 kN/ m
                                                                 kN/ m
                                                 1270.322
Psd
                                         =
                                                1270.322 kN/ m
Ps
                                         =
                                                  1117.883
                                                                 kN/ m
pu
                                              20566.7358
Cbar
                                         =
                                                    1.6447
n
                                         = 117707.2342
m
                                                      .0026
yk
                                                                   m
                                                       .0033
уm
                                                                   m
                                         =
                                                       .0074
yu
                                                    1.00000
p-multiplier
                                         =
y-multiplier
                                                    1.00000
```

If  $\operatorname{Psd} \mathrel{<=} \operatorname{Pst}$  then actual depth is used in place of equivalent depth in computations.

у, т	p, kN/m
.0000	.000
.0003	57.670
.0005	115.340
.0008	173.010
.0011	230.680
.0014	288.350
.0016	346.020
.0019	403.690
.0022	461.360
.0025	519.030
.0027	568.515
.0030	602.432
.0033	635.161
.0074	1117.883
.2042	1117.883
.4011	1117.883
.5979	1117.883

Computed Values of Load Distribution and Deflection

for Lateral Loading for Load Case Number 1

Pile-head boundary conditions are Shear and Slope (BC Type 2) Specified shear force at pile head = 44.482 kN Specified slope at pile head = 0.000E+00 m/m Specified axial load at pile head = 1423.431 kN

(Zero slope for this load indicates fixed-head conditions)

Depth X m	Deflect. Y m	Moment M kN- m	Shear V kN	Slope S Rad.	Total Stress kN/ m**2	Flx. Rig. EI kN- m**2	Soil Res p kN/ m
0.000 .122 .244 .366 .488 .610 .732 .853 .975 1.097 1.219 1.341 1.463 1.585 1.707 1.829 1.951 2.073 2.195 2.316 2.438	m003403 .003367 .003271 .003125 .002939 .002721 .002481 .002228 .001969 .001711 .001460 .001222 .001001 7.99E-04 4.62E-04 3.27E-04 2.15E-04 1.22E-04 4.89E-05 -7.63E-06 -4.95E-05		44.4822 43.1608 41.5111 39.6064 37.5126 35.1507 32.3918 29.2195 25.6391 21.7048 17.4867 13.0688 8.5461 4.0222 -8.16E-02 -3.4043 -5.9714 -7.8304 -9.6917 -9.8515	Rad7.11E-18 -5.38E-04 -9.92E-04 -001365 -001658 -001202 -002102 -002102 -002005 -001885 -001735 -001565 -001383 -001197 -001015 -8.41E-04 -6.79E-04 -5.33E-04 -4.04E-04	kN/ m**2	kN- m**2	kN/ m
2.682 2.804 2.926 3.048 3.170 3.292 3.414 3.536	-4.93E-05 -7.88E-05 -9.76E-05 -1.08E-04 -1.11E-04 -1.10E-04 -1.04E-04 -9.60E-05 -8.60E-05 -7.53E-05	5.5544 4.5209 3.5854 2.7669 2.0436 1.4193 .8933 .4618 .1186	-9.0475 -8.2451 -7.2740	-2.92E-04 -1.97E-04 -1.19E-05 -5.67E-05 -7.52E-06 2.97E-05 5.65E-05 7.44E-05 8.49E-05 8.93E-05	1.83E+05 1.80E+05 1.77E+05 1.75E+05 1.73E+05 1.71E+05 1.69E+05 1.67E+05 1.66E+05	7879.588 7879.606 7879.622 7879.635 7879.645 7879.657 7879.657 7879.657	5.750 7.414 8.517 6.909 7.022 6.874 6.522 6.019 5.414

3.780	-6.43E-05	1444	-1.7395	8.91E-05	1.65E+05	7879.657	4.750
3 901	-5.35E-05	3365	-1.2022	8.54E-05	1.66E+05	7879.657	4.063
	-4.34E-05	4672	7483	7.92E-05	1.66E+05	7879.657	3.383
4.145	-3.42E-05	5464	3754	7.14E-05	1.67E+05	7879.657	2.733
4.267	-2.60E-05	5835	-7.89E-02	6.26E-05	1.67E+05	7879.657	2.131
	-1.89E-05	5874	.1478		1.67E+05		1.588
				5.36E-05		7879.657	
4.511	-1.30E-05	5661	.3125	4.46E-05	1.67E+05	7879.657	1.113
4.633	-8.06E-06	5267	.4234	3.62E-05	1.66E+05	7879.657	.707571
	-4.14E-06	4754	.4893	2.84E-05	1.66E+05	7879.657	.371913
4.877	-1.12E-06	4173	.5182	2.15E-05	1.66E+05	7879.657	.103024
4.999	1.11E-06	3565	.5181	1.55E-05	1.66E+05	7879.657	104035
5.121	2.67E-06	2963	.4962	1.05E-05	1.66E+05	7879.657	255553
5.243	3.67E-06	2392	.4588	6.35E-06	1.66E+05	7879.657	358621
5.364	4.22E-06	1867	.4113	3.06E-06	1.66E+05	7879.657	420666
5.486	4.41E-06	1399	.3583	5.33E-07	1.65E+05	7879.657	449073
5.608	4.35E-06	-9.95E-02	.3034	-1.32E-06	1.65E+05	7879.657	450887
5.730		-6.55E-02		-2.60E-06	1.65E+05	7879.657	432598
5.852		-3.77E-02	.1988	-3.39E-06	1.65E+05	7879.657	399996
5.974	3.27E-06	-1.58E-02	.1526	-3.81E-06	1.65E+05	7879.657	358083
6.096	2.79E-06	7.85E-04	.1118	-3.93E-06	1.65E+05	7879.657	311050
6.218	2.31E-06	1.28E-02		-3.82E-06	1.65E+05	7879.657	262281
6.340	1.85E-06	2.08E-02	4.78E-02	-3.56E-06	1.65E+05	7879.657	214403
6.462	1.44E-06	2.57E-02	2.44E-02	-3.20E-06	1.65E+05	7879.657	169348
6.584	1.07E-06	2.79E-02	6.23E-03	-2.79E-06	1.65E+05	7879.657	128437
6.706	7.61E-07		-7.24E-03		1.65E+05	7879.657	092472
6.828	5.00E-07	2.70E-02	-1.66E-02	-1.93E-06	1.65E+05	7879.657	061825
6.949	2.91E-07	2.48E-02	-2.26E-02	-1.53E-06	1.65E+05	7879.657	036527
7.071	1.28E-07	2.20E-02	-2.59E-02	-1.16E-06	1.65E+05	7879.657	016356
7.193	6.99E-09		-2.69E-02		1.65E+05		-9.05E-04
	-7.87E-08	1.57E-02	-2.63E-02	-5.81E-07	1.65E+05	7879.657	.010349
7.437	-1.35E-07	1.26E-02	-2.46E-02	-3.62E-07	1.65E+05	7879.657	.017992
7.559	-1.67E-07	9.82E-03	-2.21E-02	-1.88E-07	1.65E+05	7879.657	.022627
	-1.81E-07		-1.92E-02		1.65E+05	7879.657	.024844
	-1.81E-07		-1.62E-02	4.04E-08	1.65E+05	7879.657	.025193
7.925	-1.71E-07	3.34E-03	-1.32E-02	1.06E-07	1.65E+05	7879.657	.024170
8.047	-1.55E-07	1.89E-03	-1.04E-02	1.47E-07	1.65E+05	7879.657	.022203
	-1.35E-07			1.67E-07	1.65E+05	7879.657	.019652
	-1.14E-07			1.73E-07	1.65E+05	7879.657	.016810
8.412	-9.31E-08	-6.53E-04	-3.71E-03	1.67E-07	1.65E+05	7879.657	.013904
8.534	-7.33E-08	-1.03E-03	-2.19E-03	1.54E-07	1.65E+05	7879.657	.011101
	-5.55E-08			1.36E-07	1.65E+05	7879.657	.008517
	-4.01E-08			1.17E-07	1.65E+05	7879.657	.006226
8.900	-2.71E-08	-1.30E-03	5.48E-04	9.63E-08	1.65E+05	7879.657	.004265
9.022	-1.66E-08	-1.22E-03	9.69E-04	7.68E-08	1.65E+05	7879.657	.002644
	-8.38E-09		1.21E-03	5.89E-08	1.65E+05	7879.657	.001351
	-2.22E-09		1.32E-03	4.32E-08	1.65E+05	7879.657	3.63E-04
9.388	2.15E-09	-7.86E-04	1.32E-03	2.98E-08	1.65E+05	7879.657	-3.55E-04
9.510	5.04E-09	-6.32E-04	1.24E-03	1.88E-08	1.65E+05	7879.657	-8.43E-04
9.632	6 74E-09	-4.89E-04	1.12E-03	1.01E-08	1.65E+05	7879.657	001140
9.754		-3.62E-04	9.76E-04		1.65E+05	7879.657	001286
9.876		-2.53E-04		-1.20E-09	1.65E+05	7879.657	001317
9.997	7.22E-09	-1.62E-04	6.60E-04	-4.40E-09	1.65E+05	7879.657	001265
10.119	6.53E-09	-9.01E-05	5.12E-04	-6.35E-09	1.65E+05	7879.657	001157
10.241		-3.50E-05		-7.32E-09	1.65E+05	7879.657	001016
10.363	4.75E-09	5.09E-06		-7.55E-09	1.65E+05		-8.60E-04
10.485	3.83E-09	3.24E-05	1.70E-04	-7.26E-09	1.65E+05	7879.657	-7.02E-04
10.607	2.98E-09	4.91E-05	9.39E-05	-6.63E-09	1.65E+05	7879.657	-5.51E-04
10.729	2.21E-09	5.75E-05		-5.81E-09	1.65E+05		-4.14E-04
10.851	1.56E-09		-8.21E-06		1.65E+05		-2.95E-04
10.973	1.02E-09	5.72E-05	-3.81E-05	-4.00E-09	1.65E+05	7879.657	-1.95E-04
11.095	5.86E-10	5.18E-05	-5.68E-05	-3.15E-09	1.65E+05	7879.657	-1.13E-04
			-6.67E-05		1.65E+05		-4.88E-05
11.71/	2.5(IE-III						3.26E-07
11.217	2.50E-10	2 647 05		-I./SE-U9	1.65E+05	7879.657	J.∠७೬-U/
11.339	-1.65E-12	3.64E-05		1 00	1 65	B050	
11.339 11.460	-1.65E-12 -1.85E-10	2.81E-05	-6.74E-05		1.65E+05	7879.657	3.68E-05
11.339 11.460	-1.65E-12	2.81E-05			1.65E+05 1.65E+05	7879.657 7879.657	
11.339 11.460 11.582	-1.65E-12 -1.85E-10 -3.15E-10	2.81E-05 2.04E-05	-6.74E-05 -6.13E-05	-9.09E-10	1.65E+05	7879.657	3.68E-05 6.33E-05
11.339 11.460 11.582 11.704	-1.65E-12 -1.85E-10 -3.15E-10 -4.06E-10	2.81E-05 2.04E-05 1.35E-05	-6.74E-05 -6.13E-05 -5.24E-05	-9.09E-10 -6.47E-10	1.65E+05 1.65E+05	7879.657 7879.657	3.68E-05 6.33E-05 8.25E-05
11.339 11.460 11.582 11.704 11.826	-1.65E-12 -1.85E-10 -3.15E-10 -4.06E-10 -4.72E-10	2.81E-05 2.04E-05 1.35E-05 7.82E-06	-6.74E-05 -6.13E-05 -5.24E-05 -4.15E-05	-9.09E-10 -6.47E-10 -4.82E-10	1.65E+05 1.65E+05 1.65E+05	7879.657 7879.657 7879.657	3.68E-05 6.33E-05 8.25E-05 9.68E-05
11.339 11.460 11.582 11.704 11.826 11.948	-1.65E-12 -1.85E-10 -3.15E-10 -4.06E-10 -4.72E-10 -5.24E-10	2.81E-05 2.04E-05 1.35E-05 7.82E-06 3.56E-06	-6.74E-05 -6.13E-05 -5.24E-05 -4.15E-05 -2.89E-05	-9.09E-10 -6.47E-10 -4.82E-10 -3.94E-10	1.65E+05 1.65E+05 1.65E+05 1.65E+05	7879.657 7879.657 7879.657 7879.657	3.68E-05 6.33E-05 8.25E-05 9.68E-05 1.08E-04
11.339 11.460 11.582 11.704 11.826 11.948	-1.65E-12 -1.85E-10 -3.15E-10 -4.06E-10 -4.72E-10	2.81E-05 2.04E-05 1.35E-05 7.82E-06 3.56E-06	-6.74E-05 -6.13E-05 -5.24E-05 -4.15E-05	-9.09E-10 -6.47E-10 -4.82E-10 -3.94E-10	1.65E+05 1.65E+05 1.65E+05	7879.657 7879.657 7879.657	3.68E-05 6.33E-05 8.25E-05 9.68E-05
11.339 11.460 11.582 11.704 11.826 11.948 12.070	-1.65E-12 -1.85E-10 -3.15E-10 -4.06E-10 -4.72E-10 -5.24E-10	2.81E-05 2.04E-05 1.35E-05 7.82E-06 3.56E-06	-6.74E-05 -6.13E-05 -5.24E-05 -4.15E-05 -2.89E-05 -1.51E-05	-9.09E-10 -6.47E-10 -4.82E-10 -3.94E-10	1.65E+05 1.65E+05 1.65E+05 1.65E+05	7879.657 7879.657 7879.657 7879.657	3.68E-05 6.33E-05 8.25E-05 9.68E-05 1.08E-04

## Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 1:

```
Pile-head deflection = .00340258 m

Computed slope at pile head = -7.11419E-18

Maximum bending moment = -37.293 kN- m

Maximum shear force = 44.482 kN

Depth of maximum bending moment = 0.000 m

Depth of maximum shear force = 0.000 m

Number of iterations = 10

Number of zero deflection points = 5
```

_____

Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 2

_____

(Zero moment for this load indicates free-head conditions)

Depth	Deflect.	Moment	Shear	Slope	Total	Flx. Rig.	Soil Res
X	Y	M	V	S	Stress	EI	p
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
0.000 .122 .244 .366 .488 .610 .732 .853 .975 1.097 1.219 1.341 1.463 1.585 1.707 1.829 1.951 2.073 2.195 2.316 2.438 2.560 2.682 2.804 2.926	=		44.4822 42.6455 40.2756 37.3520 33.7804 29.3418 23.8529 17.5993 10.9265 3.9683 -3.1475 -10.2836 -17.2581 -23.8505 -29.8236 -34.4167 -37.0790 -38.0263 -37.5242 -35.8446 -33.2530				_
3.170	-3.48E-04	2.2250	-12.1440	3.15E-04	1.71E+05	7879.650	22.293
3.292	-3.08E-04	.8524	-9.5469	3.39E-04	1.67E+05	7879.657	20.311
3.414	-2.66E-04	2206	-7.2079	3.44E-04	1.66E+05	7879.657	18.059
3.536	-2.24E-04	-1.0245	-5.1518	3.34E-04	1.68E+05	7879.657	15.669
3.658	-1.84E-04	-1.5928	-3.3887	3.14E-04	1.69E+05	7879.656	13.253

3.780	-1.47E-04	-1.9598	-1.9163	2.86E-04	1.70E+05	7879.653	10.900
3.901	-1.14E-04	-2.1595	7226	2.55E-04	1.71E+05	7879.651	8.682
4.023	-8.54E-05	-2.2244	.2121	2.21E-04	1.71E+05	7879.650	6.650
	-6.06E-05	-2.1844	.9125	1.87E-04	1.71E+05	7879.650	4.839
	-3.99E-05	-2.0666	1.4065	1.54E-04	1.71E+05	7879.652	3.265
4.389	-2.31E-05	-1.8948	1.7236	1.23E-04	1.70E+05	7879.653	1.937
4.511	-9.89E-06	-1.6890	1.8935	9.53E-05	1.70E+05	7879.655	.848990
4.633	1.35E-07	-1.4661	1.9445	7.09E-05	1.69E+05	7879.657	011839
4.755	7.39E-06	-1.2395	1.9033	5.00E-05	1.68E+05	7879.657	664099
4.877	1.23E-05	-1.0194	1.7939	3.25E-05	1.68E+05	7879.657	-1.131
4.999	1.53E-05	8133	1.6374	1.83E-05	1.67E+05	7879.657	-1.436
5.121	1.68E-05	6264	1.4519	7.17E-06	1.67E+05	7879.657	-1.607
5.243	1.71E-05	4618	1.2523	-1.25E-06	1.66E+05	7879.657	-1.668
5.364	1.65E-05	3206		-7.31E-06	1.66E+05	7879.657	-1.643
5.486	1.53E-05	2031		-1.14E-05	1.66E+05	7879.657	-1.554
5.608	1.37E-05	1081	.6742	-1.38E-05	1.65E+05	7879.657	-1.421
5.730	1.19E-05	-3.39E-02	.5107	-1.49E-05	1.65E+05	7879.657	-1.260
5.852	1.01E-05	2.16E-02	.3677	-1.50E-05	1.65E+05	7879.657	-1.085
5.974	8.28E-06	6.09E-02		-1.43E-05	1.65E+05	7879.657	907652
	6.59E-06	8.66E-02					
6.096				-1.32E-05	1.65E+05	7879.657	735564
6.218	5.06E-06	.1011		-1.17E-05	1.65E+05	7879.657	575335
6.340	3.73E-06	.1068	4.76E-03	-1.01E-05	1.65E+05	7879.657	431104
6.462	2.60E-06	.1058	-4.01E-02	-8.47E-06	1.65E+05	7879.657	305266
6.584	1.66E-06		-7.09E-02		1.65E+05	7879.657	198795
6.706	9.17E-07		-8.98E-02		1.65E+05	7879.657	111541
6.828	3.44E-07		-9.92E-02		1.65E+05	7879.657	042518
6.949	-7.85E-08	6.81E-02	1012	-2.94E-06	1.65E+05	7879.657	.009850
7.071	-3.72E-07	5.63E-02	-9.77E-02	-1.98E-06	1.65E+05	7879.657	.047503
7.193	-5.60E-07	4.50E-02	-9.03E-02	-1.19E-06	1.65E+05	7879.657	.072569
	-6.63E-07		-8.06E-02		1.65E+05	7879.657	.087215
	-7.01E-07		-6.96E-02		1.65E+05	7879.657	.093536
7.559	-6.90E-07	1.78E-02	-5.82E-02	2.25E-07	1.65E+05	7879.657	.093476
7.681	-6.46E-07	1.13E-02	-4.71E-02	4.50E-07	1.65E+05	7879.657	.088769
7.803	-5.80E-07	6.12E-03	-3.67E-02	5.85E-07	1.65E+05	7879.657	.080917
	-5.03E-07		-2.75E-02	6.48E-07	1.65E+05	7879.657	.071172
		-8.01E-04		6.59E-07	1.65E+05	7879.657	.060544
		-2.83E-03		6.31E-07	1.65E+05	7879.657	.049814
8.291	-2.68E-07	-4.12E-03	-7.25E-03	5.77E-07	1.65E+05	7879.657	.039556
8.412	-2.02E-07	-4.80E-03	-3.00E-03	5.08E-07	1.65E+05	7879.657	.030163
	-1.45E-07		1.72E-04	4.32E-07	1.65E+05	7879.657	.021877
	-9.66E-08		2.41E-03	3.55E-07	1.65E+05	7879.657	.014816
	-5.80E-08		3.86E-03	2.82E-07	1.65E+05	7879.657	.009004
8.900	-2.79E-08	-4.07E-03	4.68E-03	2.15E-07	1.65E+05	7879.657	.004391
9.022	-5.53E-09	-3.49E-03	5.00E-03	1.57E-07	1.65E+05	7879.657	8.81E-04
9.144		-2.90E-03	4.95E-03	1.07E-07	1.65E+05	7879.657	001655
9.266		-2.32E-03	4.65E-03	6.67E-08	1.65E+05	7879.657	003360
9.388		-1.79E-03	4.17E-03	3.48E-08	1.65E+05	7879.657	004382
9.510	2.91E-08	-1.32E-03	3.61E-03	1.08E-08	1.65E+05	7879.657	004862
9.632	2.91E-08	-9.14E-04	3.01E-03	-6.49E-09	1.65E+05	7879.657	004932
9.754	2.75E-08	-5.81E-04	2.43E-03	-1.81E-08	1.65E+05	7879.657	004706
9.876		-3.16E-04		-2.50E-08	1.65E+05	7879.657	004285
9.997		-1.14E-04		-2.83E-08			
					1.65E+05	7879.657	003748
10.119	1.78E-08	3.23E-05		-2.90E-08	1.65E+05	7879.657	003159
10.241	1.43E-08	1.32E-04		-2.77E-08	1.65E+05	7879.657	002567
10.363	1.11E-08	1.93E-04	3.40E-04	-2.52E-08	1.65E+05	7879.657	002007
10.485	8.19E-09	2.23E-04		-2.20E-08	1.65E+05	7879.657	001500
10.607	5.72E-09		-3.00E-05		1.65E+05	7879.657	001059
10.729	3.69E-09		-1.37E-04		1.65E+05		-6.90E-04
10.851	2.08E-09		-2.03E-04		1.65E+05		-3.93E-04
10.973	8.48E-10	1.77E-04	-2.37E-04	-8.71E-09	1.65E+05	7879.657	-1.62E-04
11.095	-4.72E-11		-2.46E-04		1.65E+05	7879.657	9.11E-06
	-6.63E-10		-2.37E-04		1.65E+05	7879.657	1.29E-04
	-1.05E-09		-2.17E-04		1.65E+05		
						7879.657	2.08E-04
	-1.27E-09		-1.89E-04		1.65E+05	7879.657	2.53E-04
	-1.36E-09	4.62E-05	-1.57E-04	-3.86E-10	1.65E+05	7879.657	2.74E-04
11.704	-1.37E-09	2.91E-05	-1.23E-04	1.97E-10	1.65E+05	7879.657	2.77E-04
	-1.31E-09		-8.98E-05	5.47E-10	1.65E+05	7879.657	2.69E-04
	-1.23E-09		-5.78E-05	7.26E-10	1.65E+05	7879.657	2.55E-04
	-1.14E-09		-2.78E-05	7.95E-10	1.65E+05	7879.657	2.37E-04
12.192	-1.04E-09	0.0	0.0	8.08E-10	1.65E+05	7879.657	2.19E-04

## Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 2:

```
Pile-head deflection = .01472369 m

Computed slope at pile head = -.01099103

Maximum bending moment = 48.361 kN- m

Maximum shear force = 44.482 kN

Depth of maximum bending moment = 1.34112000 m

Depth of maximum shear force = 0.000 m

Number of iterations = 16

Number of zero deflection points = 5
```

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Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 3

Pile-head boundary conditions are Shear and Rotational Stiffness (BC Type 3) Specified shear force at pile head =  $44.482 \, \text{kN}$  Specified rotational stiffness =  $88964.449 \, \text{m-kN/rad}$  Specified axial load at pile head =  $1423.431 \, \text{kN}$ 

Depth	Deflect.	Moment	Shear	Slope	Total	Flx. Rig.	Soil Res
X	У	M	V	S	Stress	EI	р
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
0.000	.003792	-35.7869	44.4822	-4.02E-04	2.63E+05	7855.921	-9.588
.122	.003709	-30.3169	43.1143	-9.15E-04	2.48E+05	7855.921	-12.853
.244	.003569	-24.9563	41.4085	001344	2.34E+05	7855.921	-15.128
.366	.003381	-19.7533	39.4373	001691	2.19E+05	7875.828	-17.208
.488	.003156	-14.7531	37.2627	001958	2.06E+05	7879.377	-18.465
.610	.002904	-9.9877	34.8067	002149	1.92E+05	7879.515	-21.824
.732	.002632	-5.5199	31.9438	002269	1.80E+05	7879.606	-25.140
.853	.002351	-1.4109	28.6613	002323	1.69E+05	7879.657	-28.706
.975	.002066	2.2751	24.9689	002316	1.71E+05	7879.649	-31.866
1.097	.001786	5.4813	20.9246	002256	1.80E+05	7879.607	-34.478
1.219	.001516	8.1604	16.6026	002150	1.87E+05	7879.557	-36.420
1.341	.001261	10.2761	12.0911	002008	1.93E+05	7879.508	-37.587
1.463	.001026	11.8056	7.4896	001837	1.97E+05	7879.468	-37.898
1.585	8.13E-04	12.7400	2.9059	001647	2.00E+05	7879.440	-37.294
1.707	6.25E-04	13.0858	-1.2391	001447	2.01E+05	7879.429	-30.701
1.829	4.61E-04	12.9402	-4.5741	001246	2.01E+05	7879.434	-24.007
1.951	3.21E-04	12.4029	-7.1154	001050	1.99E+05	7879.450	-17.681
2.073	2.05E-04	11.5696		-8.64E-04	1.97E+05	7879.475	-11.882
2.195	1.10E-04	10.5285	-10.0518	-6.93E-04	1.94E+05	7879.502	-6.723
2.316	3.55E-05	9.3592	-10.6001	-5.40E-04	1.91E+05	7879.531	-2.273
	-2.15E-05	8.1310		-4.04E-04	1.87E+05	7879.558	1.439
2.560	-6.31E-05	6.9024	-10.2940	-2.88E-04	1.84E+05	7879.583	4.416
	-9.17E-05	5.7209		-1.90E-04	1.81E+05	7879.603	6.691
	-1.09E-04	4.6235		-1.10E-04	1.78E+05	7879.620	8.316
	-1.19E-04	3.6373		-4.64E-05	1.75E+05	7879.634	9.360
	-1.21E-04	2.7804	-6.5974	3.28E-06	1.73E+05	7879.644	7.491
	-1.18E-04	2.0274	-5.6813	4.05E-05	1.71E+05	7879.652	7.537
	-1.11E-04	1.3810	-4.7757	6.68E-05	1.69E+05	7879.657	7.319
	-1.01E-04	.8397	-3.9090	8.40E-05	1.67E+05	7879.657	6.897
	-9.04E-05	.3987	-3.1029	9.36E-05	1.66E+05	7879.657	6.327
3.658	-7.87E-05	5.06E-02	-2.3724	9.71E-05	1.65E+05	7879.657	5.658

3.780	-6.68E-05	2135	-1.7265	9.58E-05	1.66E+05	7879.657	4.936
3.901	-5.53E-05	4037	-1.1698	9.10E-05	1.66E+05	7879.657	4.197
4.023	-4.46E-05	5303	7023	8.38E-05	1.66E+05	7879.657	3.472
	-3.49E-05	6040	3210	7.50E-05	1.67E+05	7879.657	2.784
	-2.63E-05		-2.02E-02	6.55E-05	1.67E+05	7879.657	2.151
4.389	-1.89E-05	6316	.2075	5.57E-05	1.67E+05	7879.657	1.584
4.511	-1.27E-05	6034	.3705	4.61E-05	1.67E+05	7879.657	1.090
4 633	-7.65E-06	5573	.4779	3.71E-05	1.67E+05	7879.657	.671482
	-3.64E-06	4997	.5388	2.90E-05	1.66E+05	7879.657	.327315
4.877	-5.86E-07	4360	.5620	2.17E-05	1.66E+05	7879.657	.053792
4.999	1.65E-06	3702	.5558	1.55E-05	1.66E+05	7879.657	154750
5.121	3.19E-06	3058	.5278	1.02E-05	1.66E+05	7879.657	305287
5.243	4.15E-06	2451	.4845	5.98E-06	1.66E+05	7879.657	405540
5.364	4.65E-06	1898	.4315		1.66E+05	7879.657	463495
5.486	4.79E-06	1408	.3736	6.34E-08	1.65E+05	7879.657	487017
5.608	4.66E-06	-9.87E-02	.3144	-1.79E-06	1.65E+05	7879.657	483553
5.730	4.35E-06	-6.35E-02	.2569	-3.04E-06	1.65E+05	7879.657	459915
5.852		-3.50E-02		-3.81E-06	1.65E+05	7879.657	422140
5.974				-4.18E-06			375413
		-1.27E-02			1.65E+05	7879.657	
6.096	2.90E-06	4.12E-03	.1118	-4.24E-06	1.65E+05	7879.657	324044
6.218	2.39E-06	1.61E-02	7.55E-02	-4.08E-06	1.65E+05	7879.657	271489
6.340	1.91E-06	2.40E-02	4.56E-02	-3.78E-06	1.65E+05	7879.657	220402
6.462	1.47E-06	2.85E-02		-3.37E-06	1.65E+05	7879.657	172713
6.584	1.08E-06		3.15E-03		1.65E+05	7879.657	129714
6.706	7.58E-07		-1.04E-02		1.65E+05	7879.657	092161
6.828	4.89E-07		-1.97E-02		1.65E+05	7879.657	060368
6.949	2.73E-07	2.62E-02	-2.54E-02	-1.56E-06	1.65E+05	7879.657	034304
7.071	1.07E-07	2.30E-02	-2.84E-02	-1.18E-06	1.65E+05	7879.657	013682
	-1.52E-08		-2.91E-02		1.65E+05	7879.657	.001968
	-1.01E-07		-2.82E-02		1.65E+05	7879.657	.013226
	-1.55E-07		-2.61E-02		1.65E+05	7879.657	.020730
7.559	-1.85E-07	1.00E-02	-2.33E-02	-1.70E-07	1.65E+05	7879.657	.025129
7.681	-1.97E-07	7.38E-03	-2.01E-02	-3.56E-08	1.65E+05	7879.657	.027051
	-1.94E-07		-1.68E-02	6.11E-08	1.65E+05	7879.657	.027077
	-1.82E-07		-1.36E-02				
				1.26E-07	1.65E+05	7879.657	.025725
	-1.63E-07		-1.06E-02	1.65E-07	1.65E+05	7879.657	.023443
8.169	-1.42E-07	6.19E-04	-7.91E-03	1.83E-07	1.65E+05	7879.657	.020603
8.291	-1.19E-07	-2.25E-04	-5.58E-03	1.86E-07	1.65E+05	7879.657	.017505
8.412	-9.63E-08	-8.07E-04	-3.64E-03	1.78E-07	1.65E+05	7879.657	.014379
	-7.53E-08			1.63E-07	1.65E+05	7879.657	.011394
	-5.65E-08			1.43E-07	1.65E+05	7879.657	.008665
8.778	-4.03E-08	-1.43E-03	6.39E-05	1.22E-07	1.65E+05	7879.657	.006263
8.900	-2.68E-08	-1.40E-03	7.03E-04	9.98E-08	1.65E+05	7879.657	.004221
9.022	-1.60E-08	-1.29E-03	1.12E-03	7.90E-08	1.65E+05	7879.657	.002545
	-7.56E-09		1.34E-03	6.01E-08	1.65E+05	7879.657	.001219
	-1.31E-09		1.43E-03	4.36E-08	1.65E+05	7879.657	2.14E-04
9.388	3.07E-09	-8.17E-04	1.41E-03	2.97E-08	1.65E+05	7879.657	-5.08E-04
9.510	5.92E-09	-6.52E-04	1.32E-03	1.83E-08	1.65E+05	7879.657	-9.90E-04
9.632	7.53E-09	-5.00E-04	1.18E-03	9.38E-09	1.65E+05	7879.657	001275
9.754		-3.66E-04	1.02E-03		1.65E+05	7879.657	001405
9.876		-2.52E-04		-2.11E-09	1.65E+05	7879.657	001418
9.997		-1.58E-04		-5.29E-09	1.65E+05	7879.657	001348
10.119		-8.43E-05		-7.16E-09	1.65E+05	7879.657	001222
10.241	5.95E-09	-2.81E-05	3.85E-04	-8.03E-09	1.65E+05	7879.657	001065
10.363	4.94E-09	1.23E-05	2.65E-04	-8.15E-09	1.65E+05	7879.657	-8.95E-04
10.485	3.96E-09	3.94E-05		-7.75E-09	1.65E+05		-7.25E-04
10.607	3.05E-09	5.56E-05		-7.02E-09	1.65E+05		-5.64E-04
10.729	2.25E-09	6.33E-05		-6.10E-09	1.65E+05		-4.20E-04
10.851	1.56E-09	6.46E-05	-1.57E-05	-5.11E-09	1.65E+05	7879.657	-2.95E-04
10.973	1.00E-09	6.13E-05	-4.54E-05	-4.13E-09	1.65E+05	7879.657	-1.91E-04
11.095	5.54E-10	5.49E-05	-6.35E-05	-3.24E-09	1.65E+05		-1.07E-04
11.217	2.12E-10		-7.26E-05		1.65E+05		-4.13E-05
	-4.26E-11		-7.46E-05		1.65E+05	7879.657	8.40E-06
	-2.25E-10		-7.13E-05		1.65E+05	7879.657	4.48E-05
11.582	-3.52E-10	2.11E-05	-6.43E-05	-8.78E-10	1.65E+05	7879.657	7.07E-05
11.704	-4.39E-10	1.40E-05	-5.45E-05	-6.06E-10	1.65E+05	7879.657	8.91E-05
	-5.00E-10		-4.29E-05		1.65E+05	7879.657	1.02E-04
	-5.45E-10		-2.97E-05		1.65E+05		1.13E-04
						7879.657	
	-5.84E-10		-1.54E-05		1.65E+05	7879.657	1.22E-04
12.192	-6.21E-10	0.0	0.0	-3.03E-10	1.65E+05	7879.657	1.31E-04

## Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 3:

```
Pile-head deflection = .00379184 m

Computed slope at pile head = -.00040226

Maximum bending moment = -35.787 kN- m

Maximum shear force = 44.482 kN

Depth of maximum bending moment = 0.000 m

Depth of maximum shear force = 0.000 m

Number of iterations = 10

Number of zero deflection points = 5
```

Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 4

Pile-head boundary conditions are Shear and Rotational Stiffness (BC Type 3) Specified shear force at pile head =  $44.482 \, \text{kN}$  Specified rotational stiffness =  $889644.490 \, \text{m-kN/rad}$  Specified axial load at pile head =  $1423.431 \, \text{kN}$ 

	Depth	Deflect.		Shear	Slope	Total	Flx. Rig.	Soil Res
	Χ	У	M	V	S	Stress	EI	p
_	m 	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
	0.000	.003443	-37.1359	44.4822	-4.17E-05	2.67E+05	7844.262	-9.286
	.122	.003403	-31.7243	43.1559	-5.77E-04	2.52E+05	7844.262	-12.470
	.244	.003302	-26.4125	41.5004	001029	2.38E+05	7844.262	-14.687
	.366	.003152	-21.2478	39.5888	001398	2.23E+05	7872.070	-16.671
	.488	.002961	-16.2738	37.4864	001689	2.10E+05	7880.216	-17.817
	.610	.002740	-11.5209	35.1146	001904	1.97E+05	7879.476	-21.090
	.732	.002497	-7.0506	32.3448	002048	1.84E+05	7879.580	-24.346
	.853	.002241	-2.9233	29.1609	002125	1.73E+05	7879.643	-27.883
	.975	.001979	.7975	25.5688	002141	1.67E+05	7879.657	-31.043
	1.097	.001719	4.0546	21.6230	002104	1.76E+05	7879.629	-33.685
	1.219	.001466	6.8002	17.3941	002020	1.84E+05	7879.585	-35.687
	1.341	.001226	8.9970	12.9665	001897	1.90E+05	7879.540	-36.945
	1.463	.001003	10.6205	8.4356	001746	1.94E+05	7879.499	-37.380
	1.585	8.01E-04	11.6599	3.9055	001573	1.97E+05	7879.472	-36.932
	1.707	6.20E-04	12.1190	2025	001389	1.98E+05	7879.458	-30.457
	1.829	4.62E-04	12.0928	-3.5263		1.98E+05	7879.459	-24.069
	1.951	3.27E-04	11.6763	-6.0907	001018	1.97E+05		-17.997
	2.073	2.13E-04	10.9610		-8.43E-04	1.95E+05	7879.491	-12.400
	2.195	1.21E-04	10.0319	-9.1501	-6.81E-04	1.93E+05	7879.514	-7.391
	2.316	4.75E-05	8.9661		-5.34E-04	1.90E+05	7879.540	-3.043
		-9.08E-06	7.8309		-4.04E-04	1.87E+05	7879.565	.608417
	2.560	-5.09E-05	6.6837	-9.6803	-2.91E-04	1.83E+05	7879.587	3.563
		-8.01E-05	5.5716		-1.97E-04	1.80E+05	7879.605	5.848
		-9.88E-05	4.5314		-1.18E-04	1.77E+05	7879.622	7.508
		-1.09E-04	3.5907		-5.56E-05	1.75E+05	7879.635	8.604
		-1.12E-04	2.7682		-6.39E-06	1.73E+05	7879.645	6.970
		-1.11E-04	2.0419	-5.5047	3.08E-05	1.71E+05	7879.652	7.076
		-1.05E-04	1.4152	-4.6515	5.76E-05	1.69E+05	7879.657	6.920
		-9.65E-05	.8877	-3.8297		1.67E+05	7879.657	6.561
		-8.65E-05	.4552	-3.0609	8.58E-05	1.66E+05		6.051
	3.658	-7.56E-05	.1115	-2.3604	9.02E-05	1.65E+05	7879.657	5.440

	-6.45E-05	1516	-1.7381	8.98E-05	1.65E+05	7879.657	4.770
3.901	-5.37E-05	3435	-1.1988	8.60E-05	1.66E+05	7879.657	4.077
4.023	-4.35E-05	4738	7434	7.97E-05	1.66E+05	7879.657	3.392
	-3.43E-05	5524	3697	7.18E-05	1.67E+05	7879.657	2.738
	-2.61E-05		-7.28E-02	6.29E-05	1.67E+05	7879.657	2.133
4.389	-1.89E-05	5920	.1540	5.38E-05	1.67E+05	7879.657	1.588
4.511	-1.29E-05	5700	.3185	4.48E-05	1.67E+05	7879.657	1.111
4 633	-8.01E-06	5299	.4291	3.63E-05	1.66E+05	7879.657	.703775
	-4.09E-06	4779	.4944	2.85E-05	1.66E+05	7879.657	.367242
4.877	-1.07E-06	4192	.5228	2.16E-05	1.66E+05	7879.657	.097879
4.999	1.17E-06	3579	.5221	1.55E-05	1.66E+05	7879.657	109326
5.121	2.72E-06	2973	.4995	1.05E-05	1.66E+05	7879.657	260736
5.243	3.72E-06	2398	.4614	6.31E-06	1.66E+05	7879.657	363506
5.364	4.26E-06	1870	.4134	3.01E-06	1.66E+05	7879.657	425121
5.486	4.45E-06	1400	.3598	4.84E-07	1.65E+05	7879.657	453017
5.608	4.38E-06	-9.94E-02	.3045	-1.37E-06	1.65E+05	7879.657	454280
5.730	4.12E-06	-6.53E-02	. 2503	-2.64E-06	1.65E+05	7879.657	435433
5.852		-3.75E-02		-3.44E-06	1.65E+05	7879.657	402292
5.974	3.28E-06	-1.55E-02	.1528	-3.85E-06	1.65E+05	7879.657	359878
6.096	2.80E-06	1.13E-03	.1118	-3.96E-06	1.65E+05	7879.657	312394
6.218	2.32E-06	1.31E-02	7.67E-02	-3.85E-06	1.65E+05	7879.657	263232
6.340	1.86E-06	2.12E-02		-3.58E-06	1.65E+05	7879.657	215021
6.462	1.44E-06	2.60E-02		-3.22E-06	1.65E+05	7879.657	169692
6.584	1.08E-06		5.91E-03		1.65E+05	7879.657	128565
6.706	7.60E-07	2.84E-02	-7.57E-03	-2.36E-06	1.65E+05	7879.657	092436
6.828	4.99E-07	2.71E-02	-1.70E-02	-1.93E-06	1.65E+05	7879.657	061670
6.949	2.89E-07		-2.29E-02		1.65E+05	7879.657	036294
7.071	1.26E-07		-2.61E-02		1.65E+05	7879.657	
							016076
7.193	4.67E-09		-2.71E-02		1.65E+05		-6.05E-04
7.315	-8.10E-08	1.58E-02	-2.65E-02	-5.81E-07	1.65E+05	7879.657	.010649
7.437	-1.37E-07	1.27E-02	-2.48E-02	-3.61E-07	1.65E+05	7879.657	.018277
7.559	-1.69E-07	9.84E-03	-2.23E-02	-1.87E-07	1.65E+05	7879.657	.022887
	-1.82E-07		-1.93E-02		1.65E+05	7879.657	.025073
	-1.82E-07		-1.63E-02	4.25E-08	1.65E+05	7879.657	.025389
7.925	-1.72E-07	3.34E-03	-1.32E-02	1.08E-07	1.65E+05	7879.657	.024331
8.047	-1.56E-07	1.88E-03	-1.04E-02	1.48E-07	1.65E+05	7879.657	.022331
8.169	-1.36E-07	7.52E-04	-7.82E-03	1.69E-07	1.65E+05	7879.657	.019751
	-1.15E-07			1.74E-07	1.65E+05	7879.657	.016882
	-9.34E-08			1.68E-07	1.65E+05	7879.657	.013953
8.534	-7.35E-08	-1.05E-03	-2.17E-03	1.55E-07	1.65E+05	7879.657	.011131
8.656	-5.56E-08	-1.25E-03	-9.75E-04	1.37E-07	1.65E+05	7879.657	.008532
8.778	-4.01E-08	-1.33E-03	-7.50E-05	1.17E-07	1.65E+05	7879.657	.006229
	-2.71E-08			9.67E-08	1.65E+05	7879.657	.004260
	-1.65E-08		9.85E-04	7.70E-08	1.65E+05	7879.657	.002633
9.144	-8.29E-09	-1.10E-03	1.23E-03	5.91E-08	1.65E+05	7879.657	.001338
9.266	-2.13E-09	-9.48E-04	1.33E-03	4.32E-08	1.65E+05	7879.657	3.48E-04
9.388	2.25E-09	-7.89E-04	1.33E-03	2.98E-08	1.65E+05	7879.657	-3.71E-04
9 510	5.13E-09	-6 34E-04	1.25E-03	1.88E-08	1.65E+05		-8.58E-04
9.632		-4.90E-04	1.13E-03	1.01E-08	1.65E+05	7879.657	
9.754		-3.62E-04	9.81E-04		1.65E+05	7879.657	001299
9.876	7.67E-09	-2.52E-04	8.21E-04	-1.29E-09	1.65E+05	7879.657	001328
9.997	7.27E-09	-1.62E-04	6.62E-04	-4.50E-09	1.65E+05	7879.657	001274
10.119		-8.94E-05		-6.44E-09	1.65E+05	7879.657	001164
10.241		-3.43E-05		-7.40E-09	1.65E+05	7879.657	001021
10.363	4.77E-09	5.84E-06	2.65E-04	-7.61E-09	1.65E+05	7879.657	-8.64E-04
10.485	3.84E-09	3.31E-05	1.70E-04	-7.31E-09	1.65E+05	7879.657	-7.04E-04
10.607	2.98E-09	4.98E-05	9.32E-05	-6.67E-09	1.65E+05	7879.657	-5.52E-04
10.729	2.22E-09	5.81E-05	3.43E-05	-5.84E-09	1.65E+05		-4.15E-04
10.851	1.56E-09		-8.99E-06		1.65E+05		-2.95E-04
10.973	1.02E-09		-3.88E-05		1.65E+05		-1.94E-04
11.095	5.82E-10		-5.75E-05		1.65E+05		-1.12E-04
11.217	2.46E-10	4.47E-05	-6.73E-05	-2.41E-09	1.65E+05	7879.657	-4.80E-05
	-5.93E-12		-7.01E-05		1.65E+05	7879.657	1.17E-06
	-1.89E-10		-6.78E-05		1.65E+05	7879.657	3.76E-05
	-3.19E-10		-6.16E-05		1.65E+05	7879.657	6.40E-05
11.704	-4.10E-10	1.35E-05	-5.26E-05	-6.42E-10	1.65E+05	7879.657	8.32E-05
11.826	-4.75E-10	7.84E-06	-4.16E-05	-4.77E-10	1.65E+05	7879.657	9.74E-05
11.948	-5.26E-10	3.57E-06	-2.90E-05	-3.89E-10	1.65E+05	7879.657	1.09E-04
	-5.70E-10		-1.51E-05		1.65E+05	7879.657	1.19E-04
14.192	-6.12E-10	0.0	0.0	-3.47E-10	1.65E+05	7879.657	1.29E-04

## Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 4:

```
Pile-head deflection = .00344303 m

Computed slope at pile head = -.00004174

Maximum bending moment = -37.136 kN- m

Maximum shear force = 44.482 kN

Depth of maximum bending moment = 0.000 m

Depth of maximum shear force = 0.000 m

Number of iterations = 10

Number of zero deflection points = 5
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Computed Values of Load Distribution and Deflection for Lateral Loading for Load Case Number 5

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Non-zero moment for this load case indicates the pile-head may rotate under the applied pile-head loading, but is not a free-head (zero moment )condition.

Depth X	Deflect. Y	Moment M	Shear V	Slope S	Total Stress	Flx. Rig. EI	Soil Res
m	m	kN- m	kN	Rad.	kN/ m**2	kN- m**2	kN/ m
0.000	.008366	-18.6425	44.4822	005045	2.16E+05	7879.449	-12.692
.122		-12.4130	42.6455	005285	1.99E+05	7879.449	-17.437
.244		-6.4094	40.3063	005431	1.83E+05	7879.449	-20.935
.366		6998	37.5515	005486	1.67E+05	7879.657	-24.256
.488	.005740	4.6512	34.4402	005455	1.78E+05	7879.620	-26.783
.610	.005079	9.5916	30.9157	005345	1.91E+05	7879.525	-31.034
.732	.004436	14.0449	26.8966	005162	2.04E+05	7879.401	-34.896
.853	.003820	17.9417	22.4119	004915	2.14E+05	7879.417	-38.672
.975	.003238	21.2156	17.5017	004612	2.23E+05	7872.199	-41.876
1.097	.002696	23.8100	12.2492	004263	2.30E+05	7879.577	-44.288
1.219	.002199	25.6821	6.7662	003880	2.35E+05	7871.866	-45.656
1.341	.001750	26.8065	1.1874	003473	2.39E+05	7860.126	-45.859
1.463	.001352	27.1771	-4.3393	003054	2.40E+05	7857.847	-44.803
1.585	.001005	26.8086	-9.6556	002636	2.39E+05	7860.113	-42.406
1.707		25.7375	-14.3645	002228	2.36E+05	7871.103	-34.840
1.829		24.0794	-17.9549	001843	2.31E+05	7879.547	-24.057
1.951	2.60E-04	21.9990	-20.2933	001486	2.25E+05	7875.595	-14.303
2.073	9.91E-05	19.6470	-21.5162	001164	2.19E+05	7875.660	-5.757
	-2.42E-05	17.1565		-8.79E-04	2.12E+05	7880.563	1.480
	-1.15E-04	14.6420		-6.33E-04	2.05E+05	7879.380	7.380
	-1.79E-04	12.1979		-4.25E-04	1.98E+05	7879.456	11.971
	-2.19E-04	9.8990		-2.55E-04	1.92E+05	7879.517	15.328
	-2.41E-04	7.8013		-1.18E-04	1.86E+05	7879.565	17.563
	-2.48E-04	5.9437		-1.12E-05	1.81E+05	7879.599	18.810
	-2.43E-04	4.3498	-11.8527		1.77E+05	7879.625	19.213
	-2.31E-04	3.0298	-9.8084	1.25E-04	1.73E+05	7879.642	14.322
	-2.13E-04	1.9146	-8.1051	1.64E-04	1.70E+05	7879.653	13.619
	-1.91E-04	.9966	-6.5065	1.86E-04	1.68E+05	7879.657	12.605
	-1.67E-04	.2634	-5.0445	1.96E-04	1.66E+05	7879.657	11.377
	-1.43E-04	3014	-3.7401	1.96E-04	1.66E+05	7879.657	10.021
3.658	-1.20E-04	7165	-2.6044	1.88E-04	1.67E+05	7879.657	8.609

3.780	-9.75E-05	-1.0017	-1.6405	1.75E-04	1.68E+05	7879.657	7.204
3.901	-7.71E-05	-1.1771	8445	1.58E-04	1.68E+05	7879.657	5.854
	-5.90E-05	-1.2624	2075	1.39E-04	1.68E+05	7879.657	4.596
							3.456
	-4.33E-05	-1.2759	.2833	1.19E-04	1.69E+05	7879.657	
	-2.99E-05	-1.2346	.6434	9.98E-05	1.68E+05	7879.657	2.451
4.389	-1.89E-05	-1.1536	.8896	8.13E-05	1.68E+05	7879.657	1.588
4.511	-1.01E-05	-1.0459	1.0393	6.43E-05	1.68E+05	7879.657	.868339
	-3.27E-06	9225	1.1098	4.90E-05	1.68E+05	7879.657	.286930
4.755	1.84E-06	7924	1.1172	3.58E-05	1.67E+05	7879.657	165391
4.877	5.46E-06	6625	1.0766	2.45E-05	1.67E+05	7879.657	500797
4.999	7.82E-06	5384	1.0013	1.52E-05	1.66E+05	7879.657	733351
5.121	9.17E-06	4236	.9031	7.78E-06	1.66E+05	7879.657	878038
5.243	9.72E-06	3209	.7917	2.03E-06	1.66E+05	7879.657	949962
5.364	9.66E-06	2313		-2.25E-06	1.66E+05	7879.657	963702
5.486	9.17E-06	1555	.5594	-5.24E-06	1.65E+05	7879.657	932834
5.608	8.39E-06	-9.31E-02	.4495	-7.16E-06	1.65E+05	7879.657	869593
5.730		-4.34E-02		-8.22E-06	1.65E+05	7879.657	784673
5.852		-5.23E-03		-8.59E-06	1.65E+05	7879.657	687122
5.974	5.33E-06	2.27E-02	.1814	-8.46E-06	1.65E+05	7879.657	584349
6.096	4.32E-06	4.20E-02	.1164	-7.96E-06	1.65E+05	7879.657	482185
6.218	3.39E-06	5.39E-02	6.36E-02	-7.22E-06	1.65E+05	7879.657	385002
6.340	2.56E-06	6.00E-02		-6.34E-06	1.65E+05	7879.657	295877
6.462	1.84E-06		-9.20E-03		1.65E+05	7879.657	216761
6.584	1.24E-06		-3.15E-02		1.65E+05	7879.657	148666
6.706	7.56E-07	5.53E-02	-4.61E-02	-3.57E-06	1.65E+05	7879.657	091855
6.828	3.72E-07	4.96E-02	-5.45E-02	-2.76E-06	1.65E+05	7879.657	046004
6.949	8.26E-08		-5.80E-02		1.65E+05	7879.657	010372
			-5.76E-02				.016068
	-1.26E-07				1.65E+05	7879.657	
	-2.66E-07		-5.46E-02		1.65E+05	7879.657	.034506
7.315	-3.51E-07	2.32E-02	-4.96E-02	-5.17E-07	1.65E+05	7879.657	.046200
7.437	-3.93E-07	1.75E-02	-4.36E-02	-2.03E-07	1.65E+05	7879.657	.052399
	-4.01E-07		-3.71E-02		1.65E+05	7879.657	.054286
			-3.06E-02				
	-3.85E-07			1.93E-07	1.65E+05	7879.657	.052941
	-3.54E-07		-2.43E-02	2.98E-07	1.65E+05	7879.657	.049311
7.925	-3.13E-07	2.41E-03	-1.86E-02	3.56E-07	1.65E+05	7879.657	.044204
8.047	-2.67E-07	3.98E-04	-1.36E-02	3.77E-07	1.65E+05	7879.657	.038282
8.169	-2.21E-07	-1.04E-03	-9.33E-03	3.72E-07	1.65E+05	7879.657	.032070
		-2.01E-03		3.49E-07	1.65E+05	7879.657	.025964
		-2.58E-03		3.13E-07	1.65E+05	7879.657	.020248
8.534	-9.98E-08	-2.84E-03	-8.21E-04	2.71E-07	1.65E+05	7879.657	.015106
8.656	-6.94E-08	-2.87E-03	7.49E-04	2.27E-07	1.65E+05	7879.657	.010644
8.778	-4.44E-08	-2.74E-03	1.82E-03	1.84E-07	1.65E+05	7879.657	.006902
	-2.46E-08		2.48E-03	1.43E-07	1.65E+05	7879.657	.003874
	-9.52E-09		2.80E-03	1.07E-07	1.65E+05	7879.657	.001517
9.144	1.47E-09	-1.85E-03	2.88E-03	7.58E-08	1.65E+05	7879.657	-2.36E-04
9.266	8.97E-09	-1.51E-03	2.78E-03	4.99E-08	1.65E+05	7879.657	001465
9.388	1.36E-08	-1.19E-03	2.55E-03	2.91E-08	1.65E+05	7879.657	002253
9.510		-8.95E-04	2.25E-03	1.30E-08	1.65E+05	7879.657	002686
9.632		-6.42E-04	1.91E-03	1.07E-09	1.65E+05	7879.657	002842
9.754	1.63E-08	-4.29E-04	1.57E-03	-7.21E-09	1.65E+05	7879.657	002794
9.876	1.50E-08	-2.56E-04	1.24E-03	-1.25E-08	1.65E+05	7879.657	002604
9.997		-1.22E-04		-1.54E-08	1.65E+05	7879.657	002324
10.119		-2.17E-05		-1.65E-08	1.65E+05	7879.657	001997
10.241	9.23E-09	4.89E-05		-1.63E-08	1.65E+05	7879.657	001654
10.363	7.29E-09	9.47E-05	2.73E-04	-1.52E-08	1.65E+05	7879.657	001320
10.485	5.52E-09	1.21E-04	1.31E-04	-1.36E-08	1.65E+05	7879.657	001011
10.607	3.98E-09	1.31E-04	2.44E-05	-1.16E-08	1.65E+05	7879.657	-7.37E-04
10.729	2.69E-09		-5.12E-05		1.65E+05		-5.03E-04
10.851	1.64E-09		-1.01E-04		1.65E+05		-3.11E-04
10.973	8.29E-10		-1.29E-04		1.65E+05		-1.58E-04
11.095	2.19E-10	9.27E-05	-1.42E-04	-4.28E-09	1.65E+05	7879.657	-4.24E-05
11.217	-2.15E-10	7.57E-05	-1.42E-04	-2.98E-09	1.65E+05	7879.657	4.20E-05
	-5.07E-10		-1.33E-04		1.65E+05	7879.657	9.99E-05
	-6.87E-10		-1.19E-04		1.65E+05	7879.657	1.37E-04
	-7.85E-10		-1.01E-04		1.65E+05	7879.657	1.58E-04
11.704	-8.24E-10	1.96E-05	-8.08E-05	-1.73E-10	1.65E+05	7879.657	1.67E-04
	-8.27E-10		-6.03E-05	6.37E-11	1.65E+05	7879.657	1.69E-04
	-8.09E-10		-3.98E-05	1.86E-10	1.65E+05	7879.657	1.67E-04
	-7.81E-10		-1.96E-05	2.33E-10	1.65E+05	7879.657	1.63E-04
12.192	-7.52E-10	0.0	0.0	2.43E-10	1.65E+05	7879.657	1.59E-04

#### Output Verification:

Computed forces and moments are within specified convergence limits.

Output Summary for Load Case No. 5:

Pile-head deflection = .00836608 m

Computed slope at pile head = -.00504485

Maximum bending moment = 27.177 kN- m

Maximum shear force = 44.482 kN Depth of maximum bending moment = 1.46304000 m

Depth of maximum shear force = 0.000 m

Number of iterations = 13

Number of zero deflection points = 5

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## Summary of Pile-head Response

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Definition of symbols for pile-head boundary conditions:

y = pile-head displacment, m
M = pile-head moment, kN- m
V = pile-head shear force, kN

V = pile-head shear force, kN S = pile-head slope, radians

R = rotational stiffness of pile-head, m- kN/rad

BC	Bou	ndary	Ε	Boundary	Axial	Pile Head	Maximum	Maximum
Type	Cond	ition	Co	ondition	Load	Deflection	Moment	Shear
		1		2	kN	m	m- kN	kN
2	$\nabla =$	44.482	S=	0.000	1423.4310	.003403	-37.2932	44.4822
1	$\nabla =$	44.482	M=	0.000	1423.4310	.014724	48.3615	44.4822
3	$\nabla =$	44.482	R=	88964.449	1423.4310	.003792	-35.7869	44.4822
3	$\nabla =$	44.482	R=	8.90E+05	1423.4310	.003443	-37.1359	44.4822
1	∨=	44.482	M=	-18.642	1423.4310	.008366	27.1771	44.4822

Pile-head Deflection vs. Pile Length

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Boundary Condition Type 2, Shear and Slope

Shear = 44. kN Slope = .00000 Axial Load = 1423. kN

Pile	Pile Head	Maximum	Maximum
Length	Deflection	Moment	Shear
m	m	m- kN	kN
12.192 11.582 10.973 10.363 9.754 9.144 8.534 7.925 7.315 6.706	.00340258 .00340004 .00339741 .00339593 .00339785 .00339393 .00339252 .00339051 .00338887	-37.293 -37.279 -37.272 -37.273 -37.294 -37.277 -37.271 -37.270 -37.266 -37.267	44.482 44.482 44.482 44.482 44.482 44.482 44.482 44.482 44.482